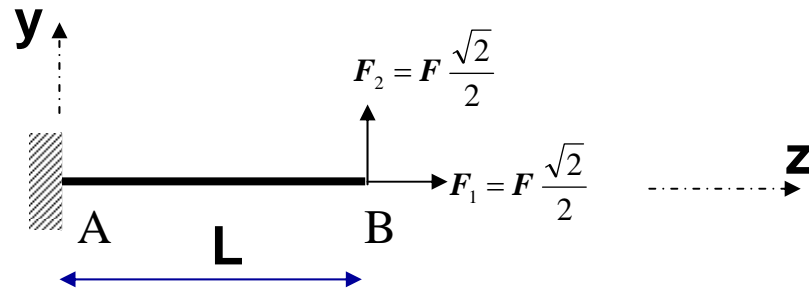


Determinar los desplazamientos que experimenta la sección B de la ménsula de la figura utilizando el teorema de Castigliano



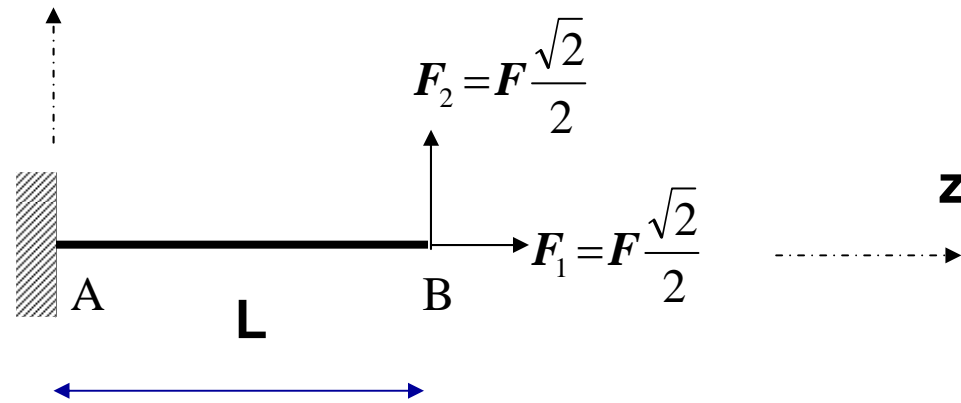
$$\frac{\partial U}{\partial F_j} = d_i$$

$$U = \frac{1}{2} \int_{z=0}^{z=L} \left[\frac{N^2(z)}{EA} + \frac{M^2(z)}{EI_x} + \frac{Q_y^2(z)}{G\Omega_c} + \frac{M_z^2(z)}{GK} \right] dz$$

$$N = F_1 = F \frac{\sqrt{2}}{2} \quad Q_y = F_2 = F \frac{\sqrt{2}}{2}$$

$$M(z) = F_2 \cdot (L - z) = F \frac{\sqrt{2}}{2} (L - z) \quad M_z = 0$$

$$U = \frac{1}{2} \left[\frac{F_1^2}{EA} \cdot L + \frac{F_2^2}{EI_x} \cdot \frac{L^3}{3} + \frac{F_2^2}{G\Omega_c} \cdot L \right]$$



$$U = \frac{1}{2} \left[\frac{F_1^2}{EA} \cdot L + \frac{F_2^2}{EI_x} \cdot \frac{L^3}{3} + \frac{F_2^2}{G\Omega_c} \cdot L \right]$$

$$d_1 = \frac{\partial U}{\partial F_1} = \frac{F_1}{EA} \cdot L = \frac{\sqrt{2}F \cdot L}{2EA}$$

$$d_2 = \frac{\partial U}{\partial F_2} = \frac{F_2}{EI_x} \cdot L^3 + \frac{F_2}{E\Omega_c} \cdot L = \frac{\sqrt{2}F \cdot L^3}{2EI_x} + \frac{\sqrt{2}F \cdot L}{2E\Omega_c}$$