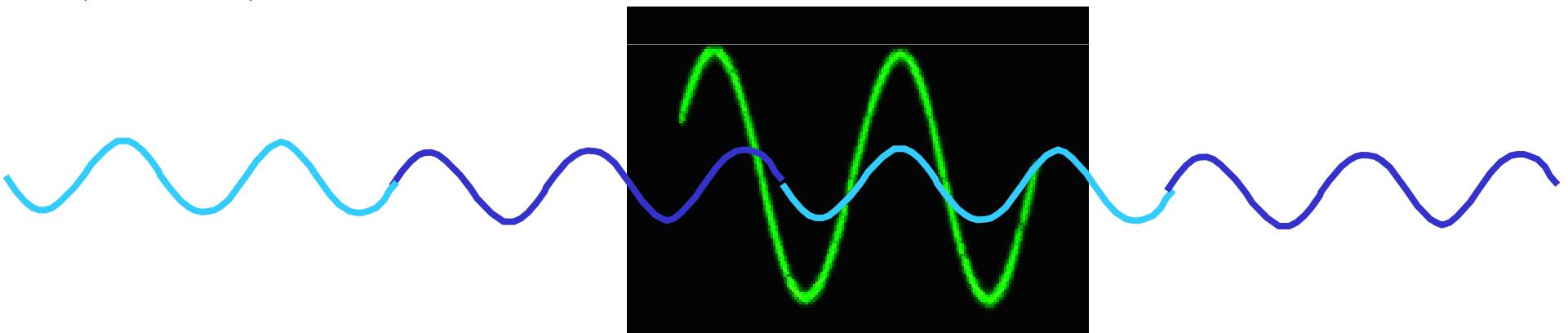


# ***(Analog) Electronics***

## **Lesson III**

### **(Linear) Oscillators**



**Murphy's Law of Electronics:**

**Amplifiers oscillate and oscillators amplify**

**What are we going to talk about?**

## Linear Electronic Oscillators

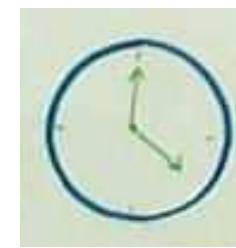
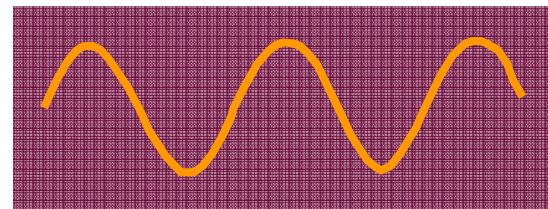
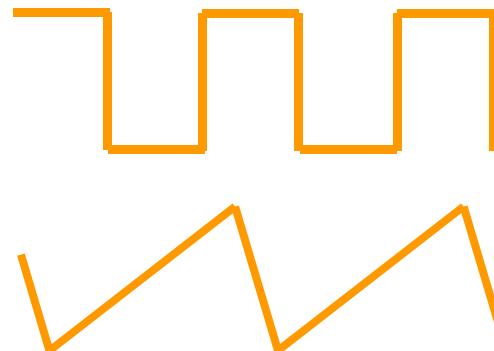
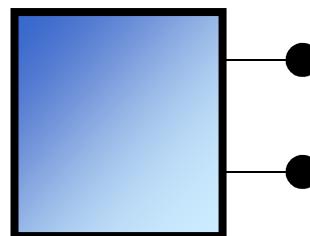
Circuits that

produces an electronic signal (volts or amps),

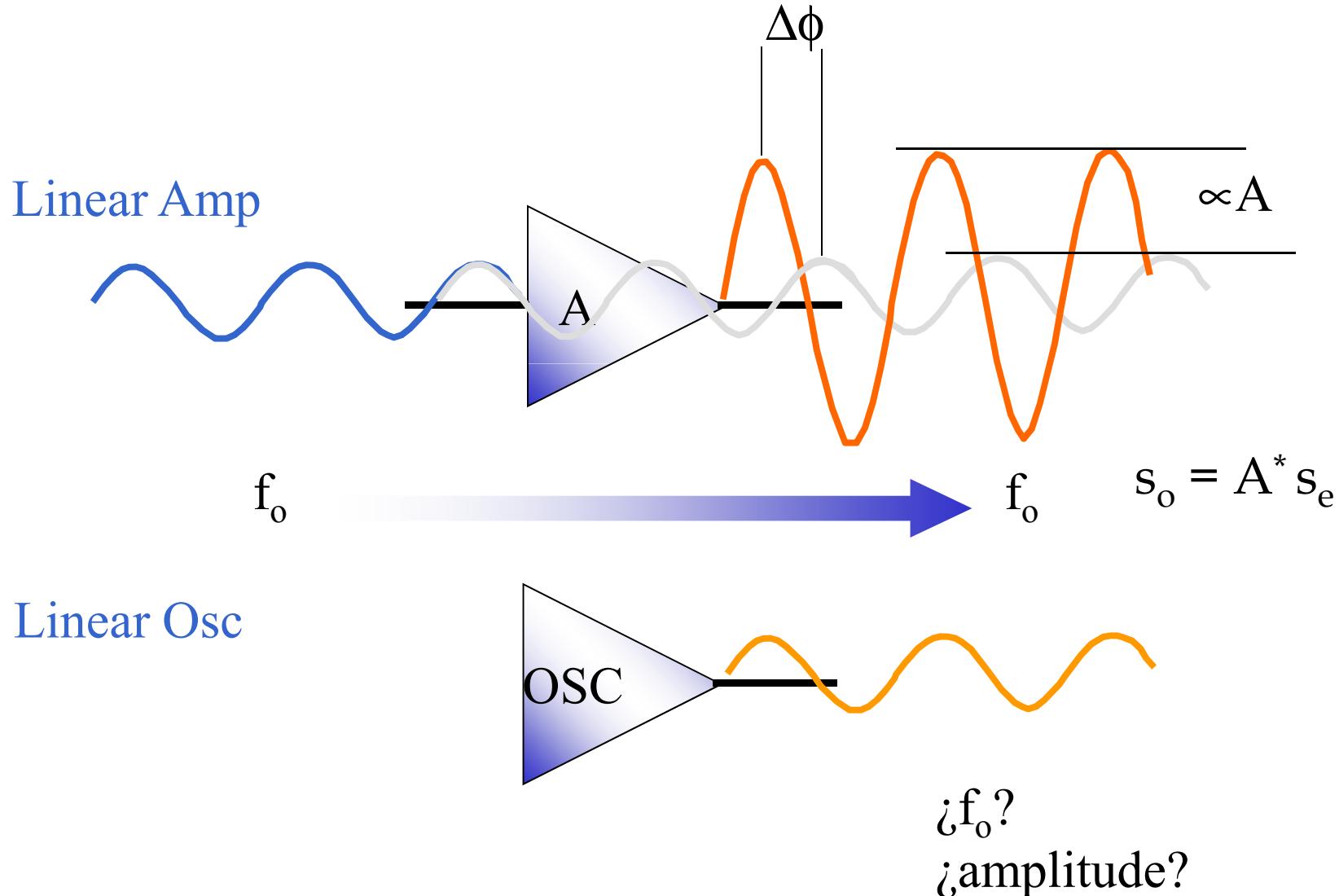
which varies in time (with temporal dependence)

without need of an input.

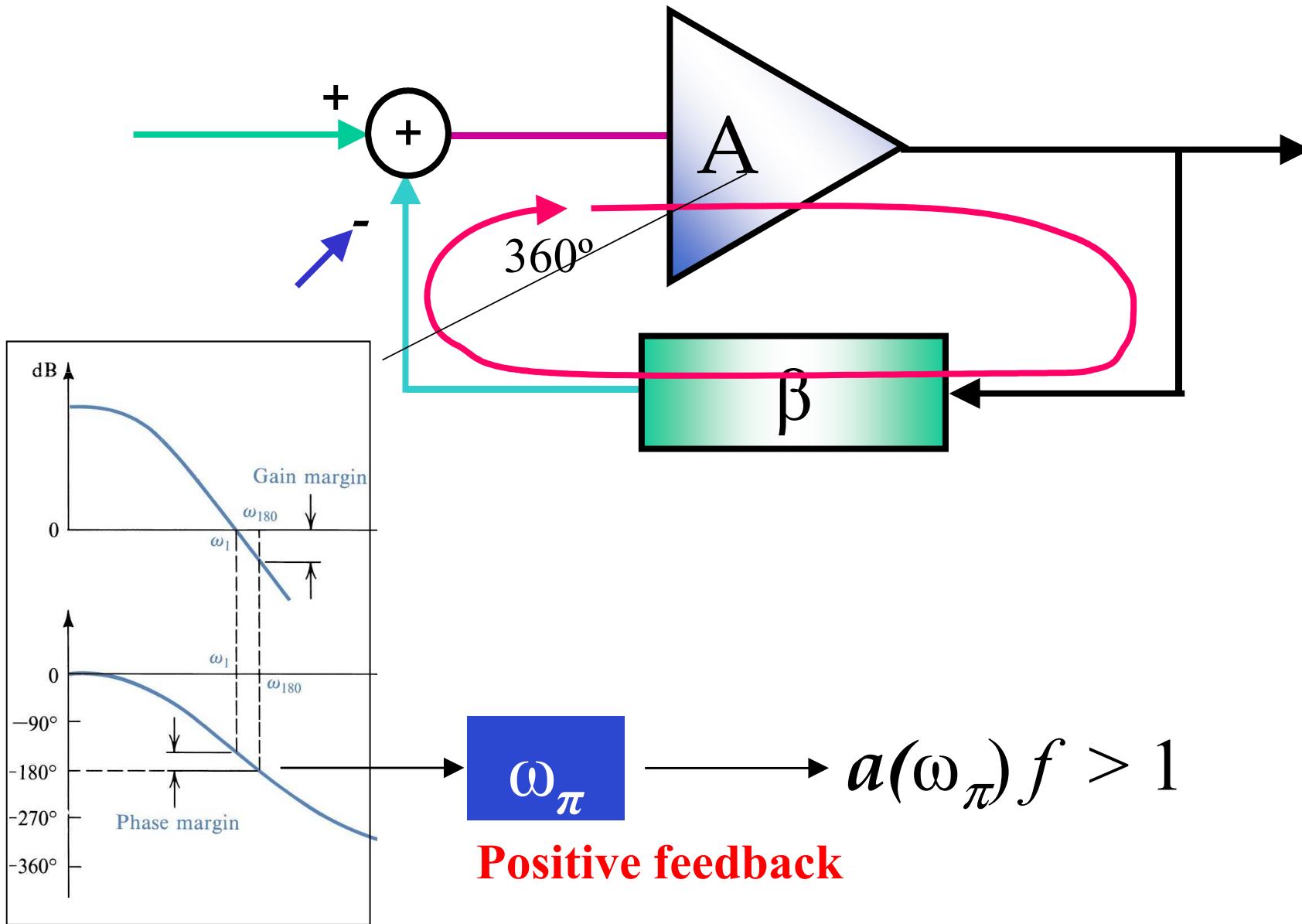
# Is there a need for this?



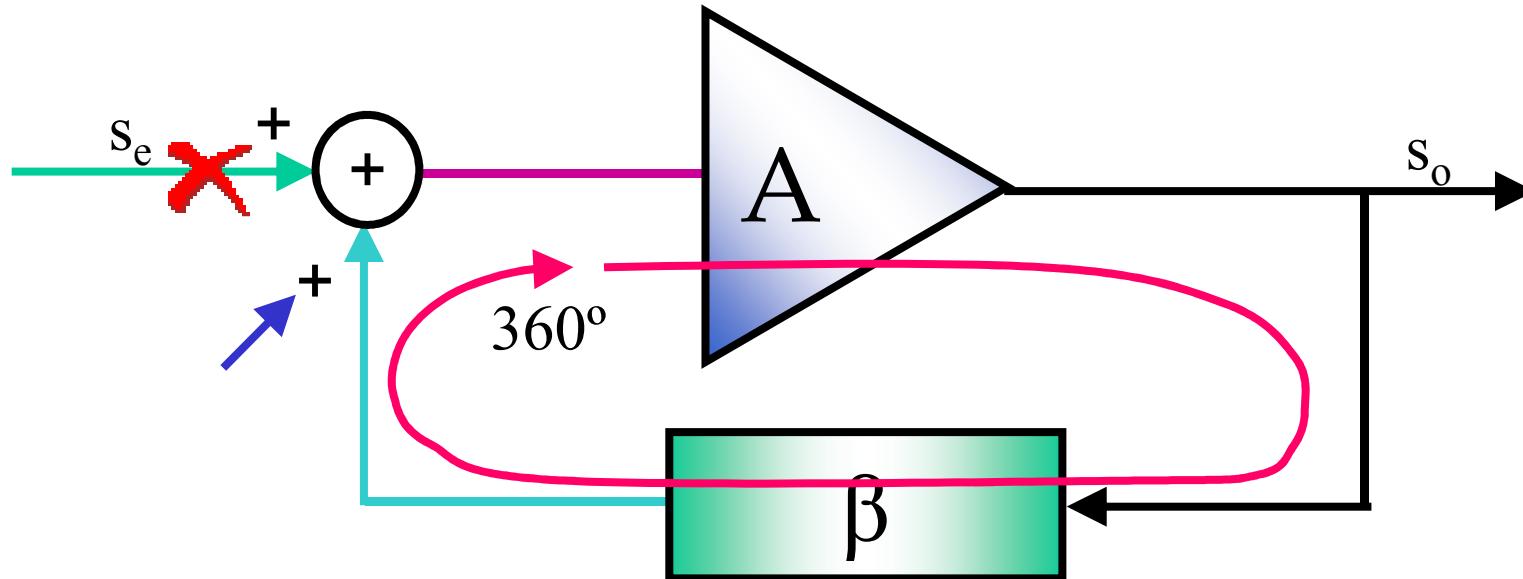
## Amplifier vs. Oscillator



# Oscillation in an Amplifier



## The Oscillator Feedback Loop



$$A_f(s) = \frac{A(s)}{1 - A(s)\beta(s)}$$

{What happens when  $A\beta = 1$ ?

There can be an output signal,  $s_o$ , without input,  $s_e$ .

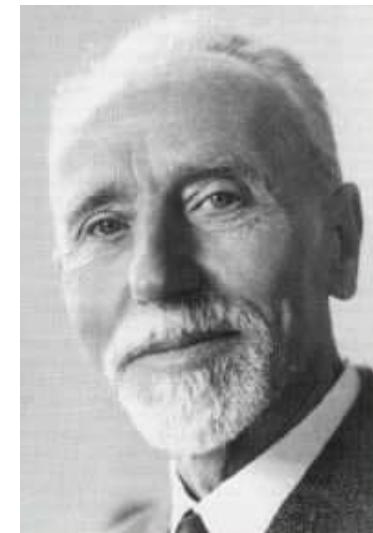
*¿Aβ = 1?*

$$A\beta = 1$$

$$A\beta = 1 e^{j0}$$

$f_o$   
amplitude

Barkhausen  
Criterion



## Conditions for Oscillation

$$|A\beta| = 1$$

**Gain Condition**

$$\begin{array}{ccc} \text{Amp GAIN} & = & \text{Feedback Net LOSS} \\ A & = & \beta \end{array}$$

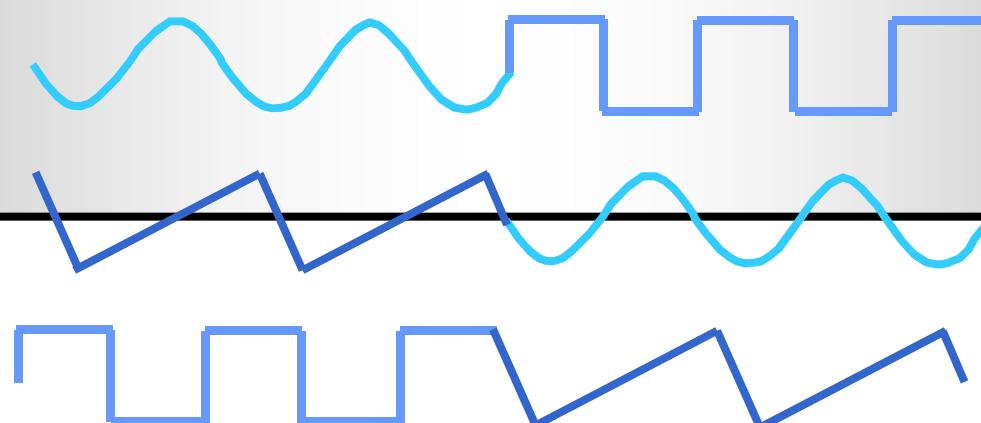
$$|A\beta| = e^{j0}$$

**Phase Condition**

Total phase change in the LOOP = 0 /  $2\pi$

For a unique  $f_o$

## ELEMENTS FOR OSCILLATION



# Electronic Oscillator Basics (I)



**Basic Amplifier ,...**

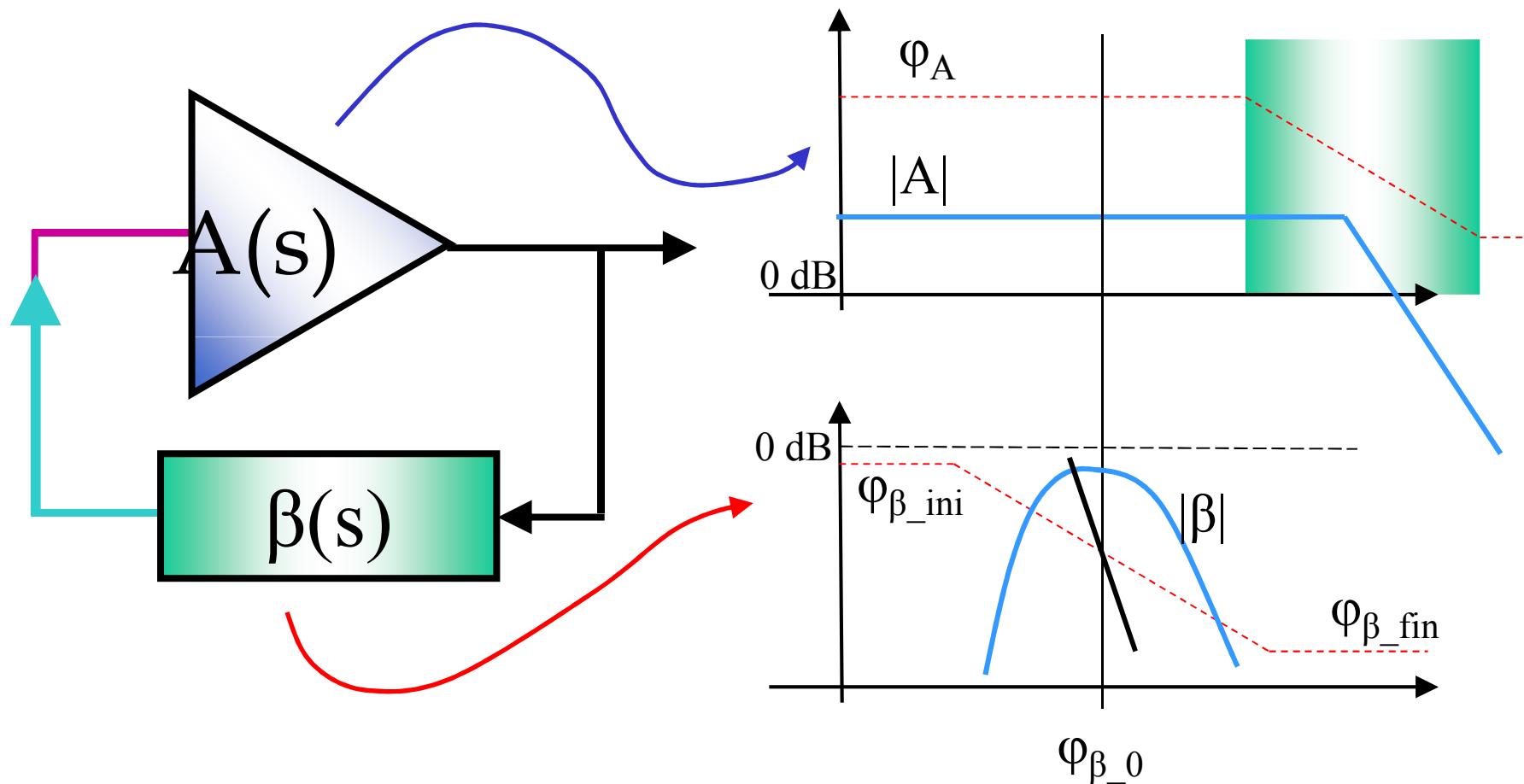
providing for **GAIN** (with a given phase change).



**Feedback Network,...**

**SELECTIVE WITH FREQUENCY** to determine the oscillation frequency, introducing **LOSSES**.

## Electronic Oscillator Basics (II)



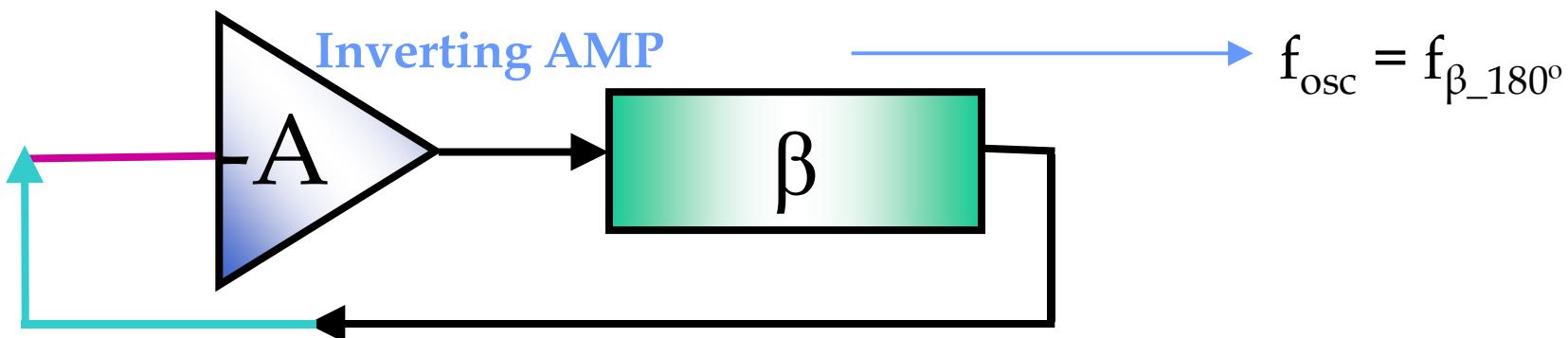
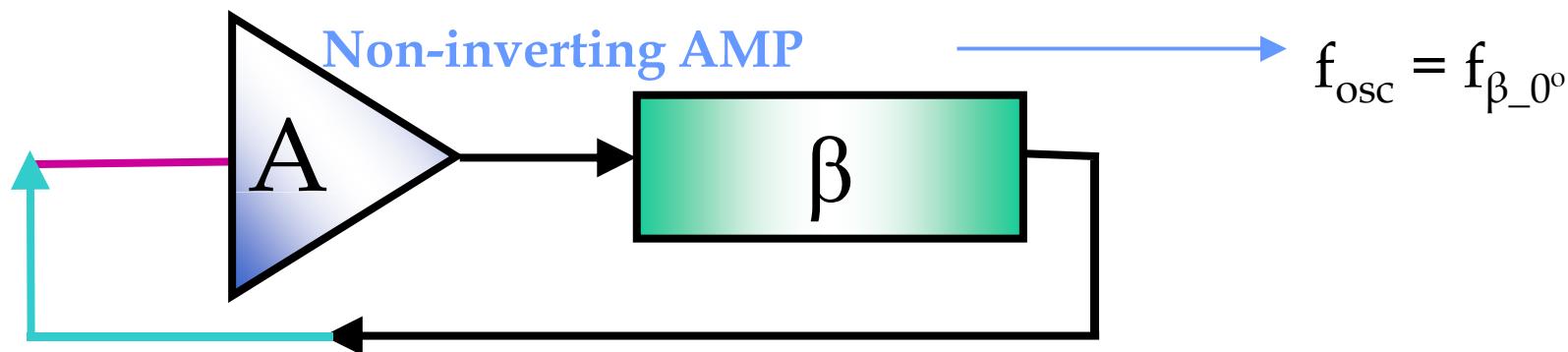
$$\Phi_A + \Phi_{\beta_0} = 2\pi, 0$$

$$|A| = 1 / |\beta|$$

## Phase Condition

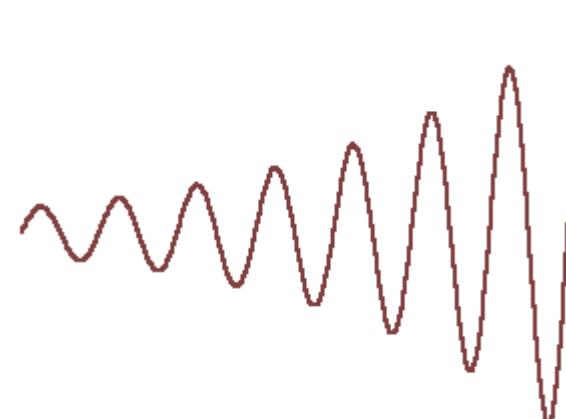
$$|A\beta| = e^{j0}$$

Total phase change in the loop = 0 or  $2\pi$

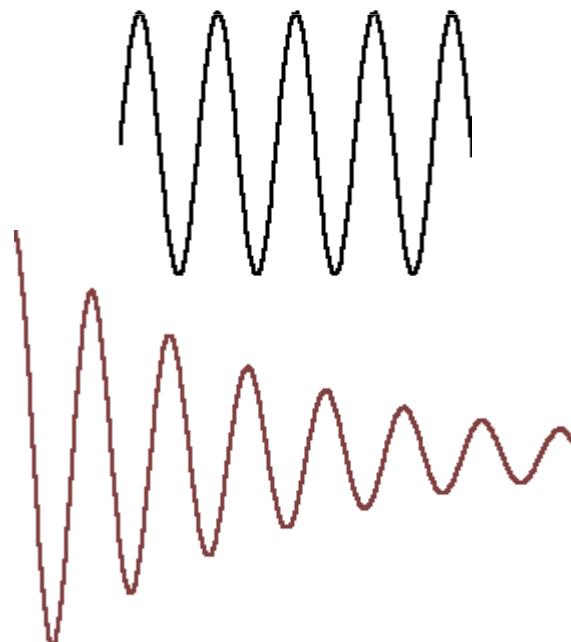


## Gain Condition (I)

$$|A| > 1/|\beta|$$



$$|A| = 1/|\beta|$$

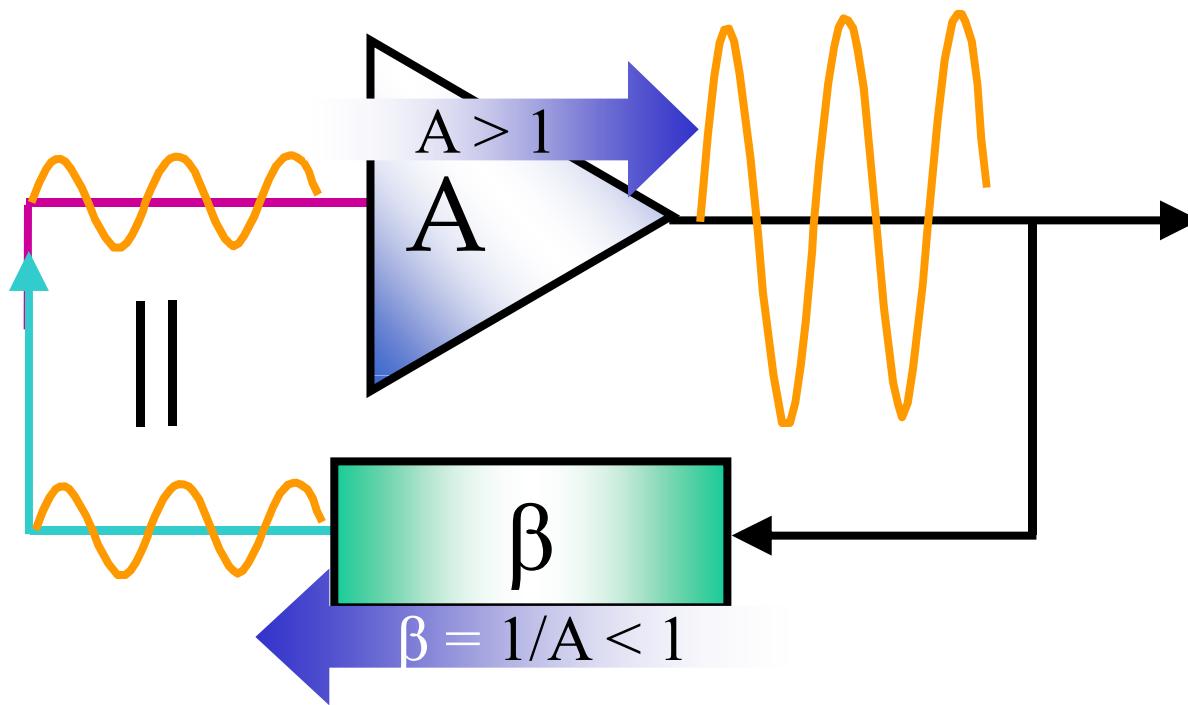


$$|A| < 1/|\beta|$$

## Gain Condition (II)

### Relation with stability

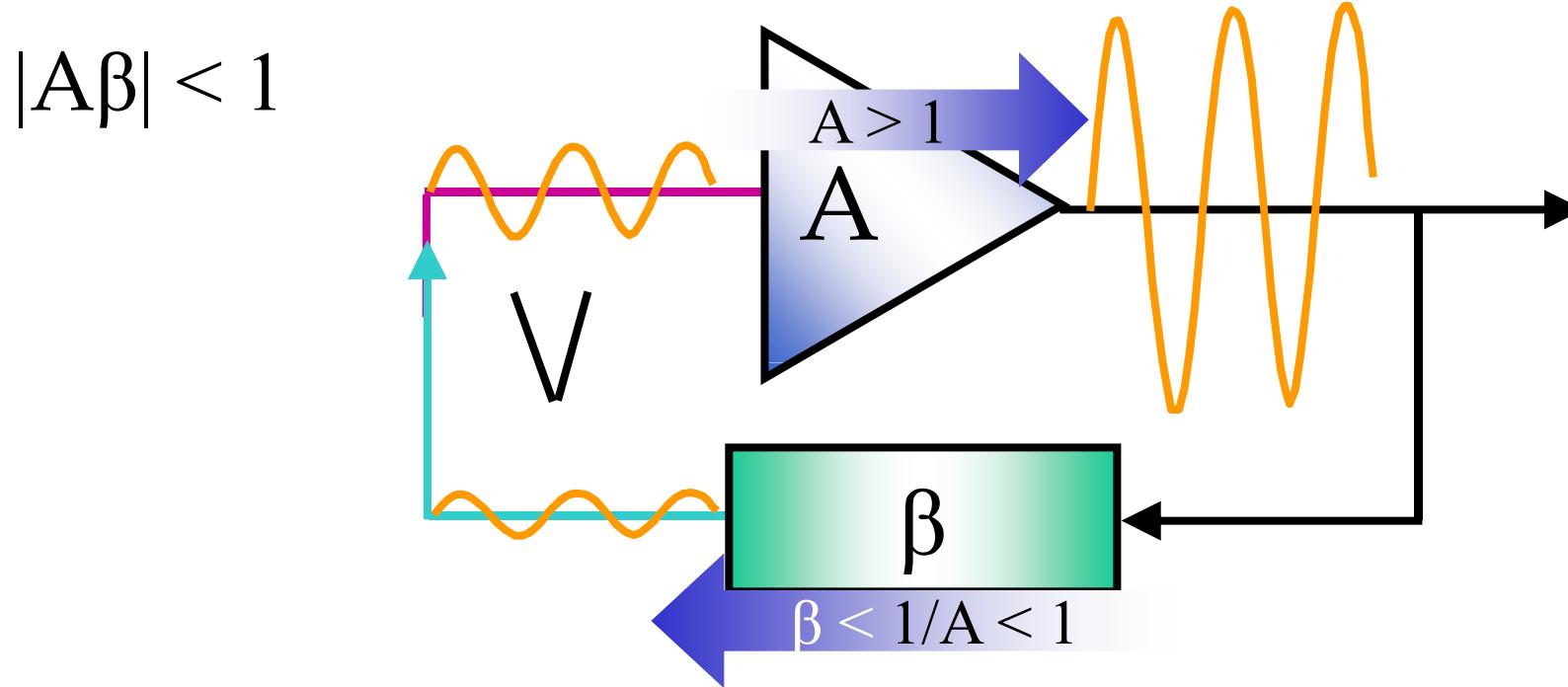
$$|A\beta| = 1$$



Sustained oscillations

## Gain Condition (III)

Relation with stability

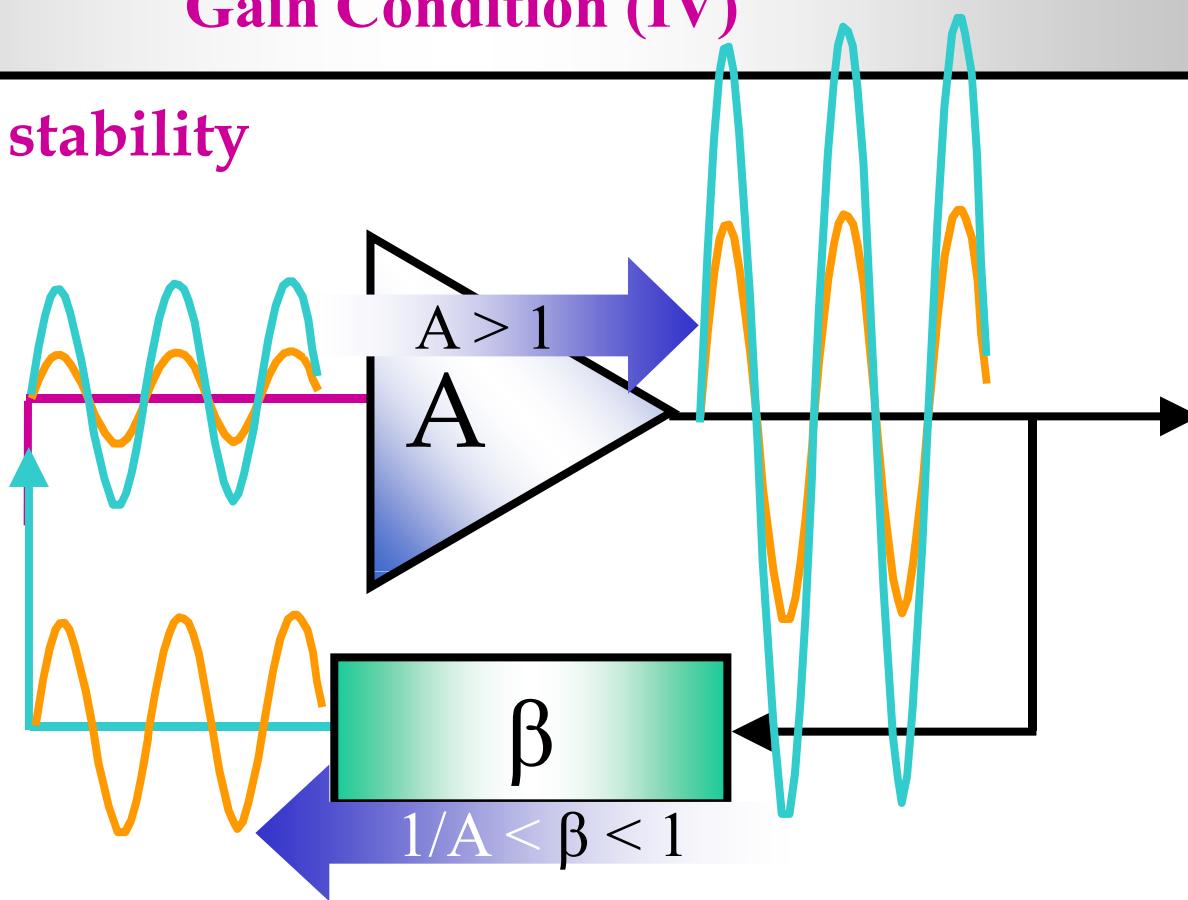


Decay of the oscillation = STABLE

## Gain Condition (IV)

Relation with stability

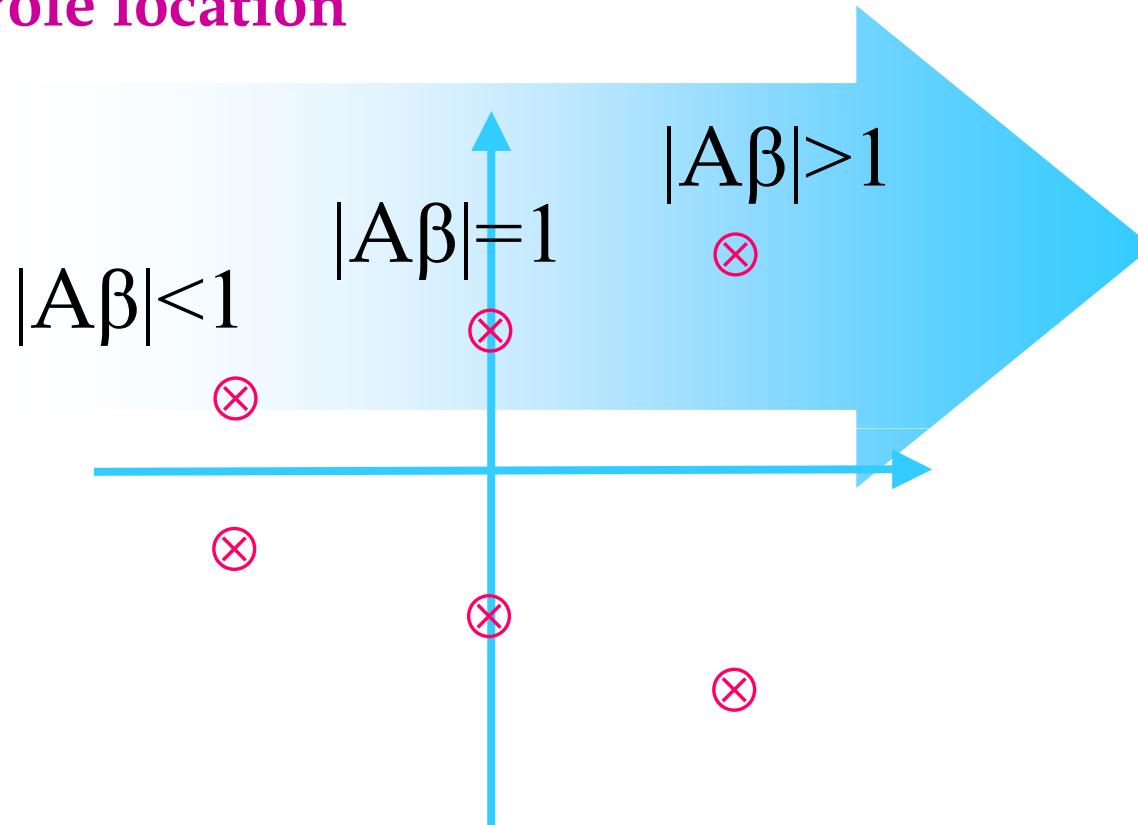
$$|A\beta| > 1$$



Exponential growth = UNSTABLE

## Gain Condition (V)

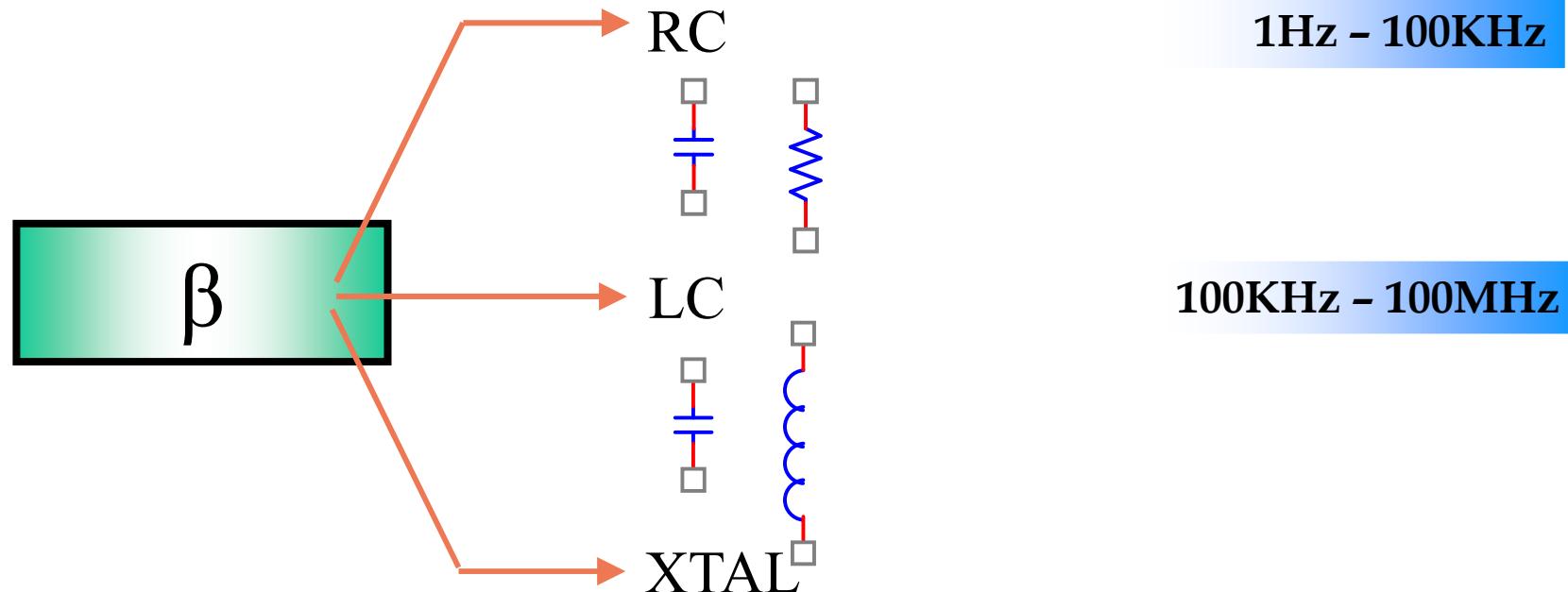
Stability ~ Pole location



Poles move as the loop gain changes

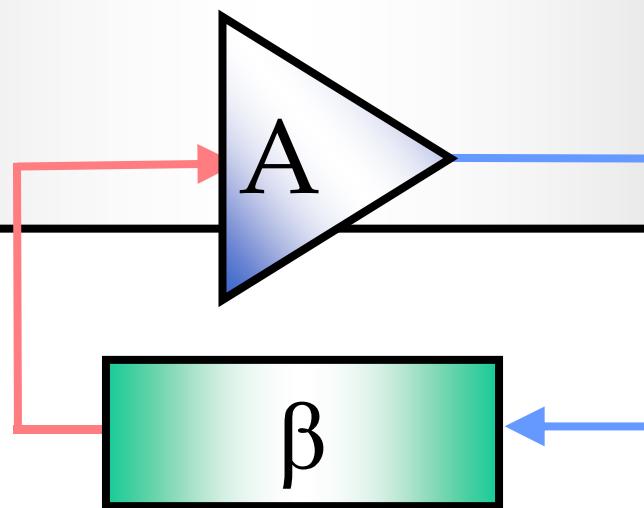
## Feedback network implementation

Allows to classify the oscillators,



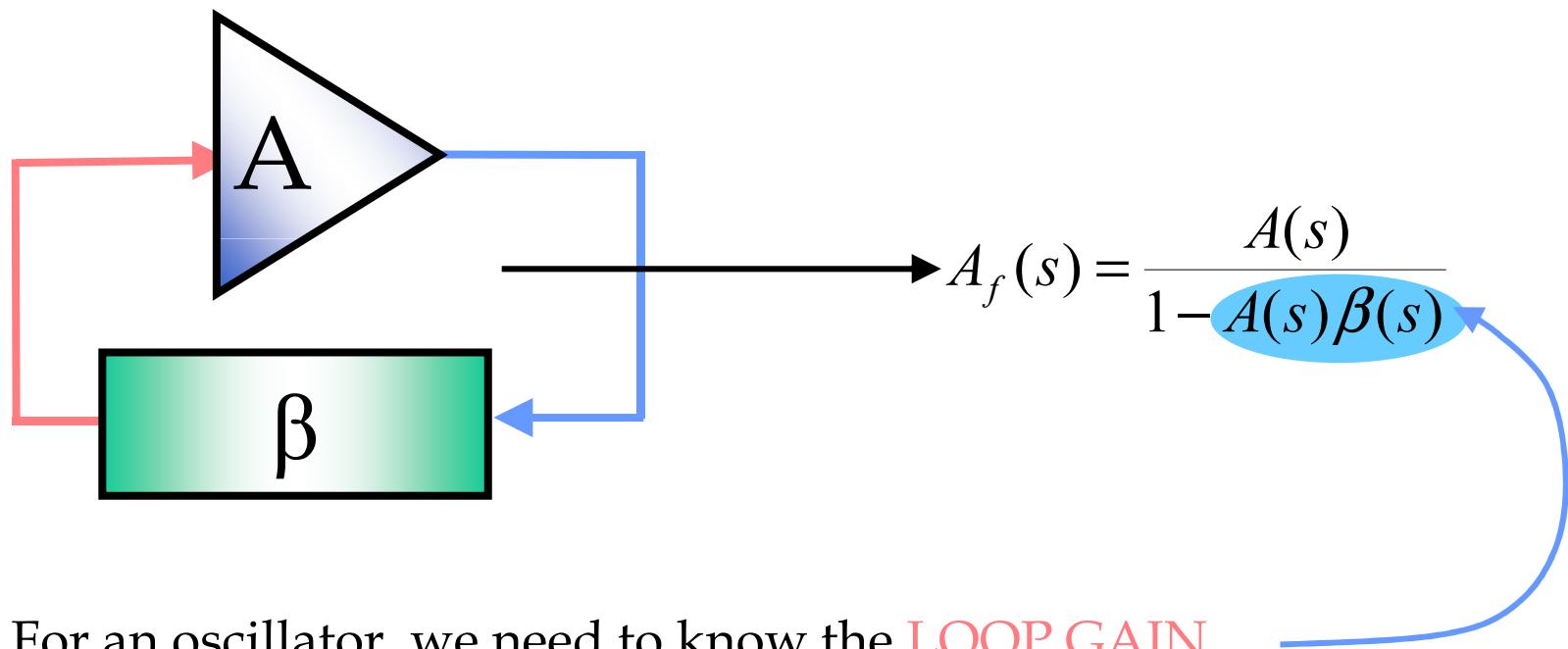
# OSCILADOR ANALYSIS

## Loop Gain Calculation



## Transfer Function

The behaviour of any circuit is known from its transfer function.

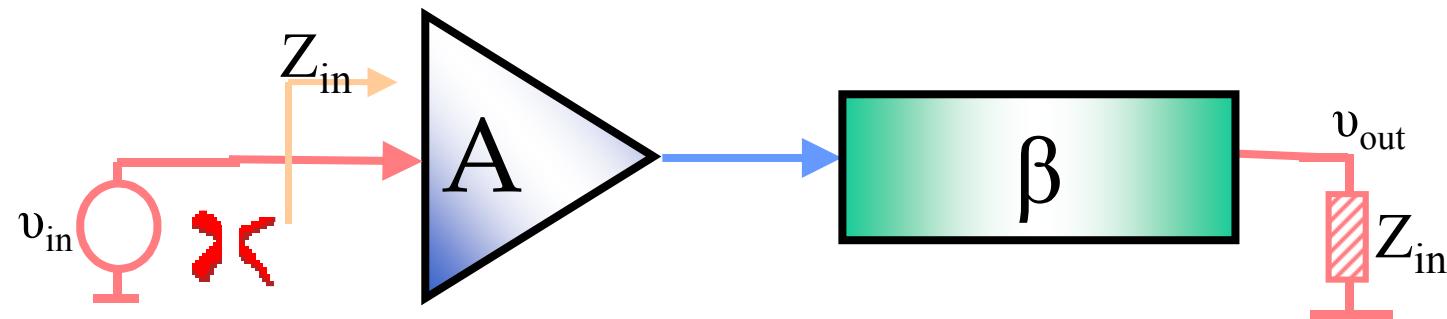


For an oscillator, we need to know the LOOP GAIN

From it, poles can be found solving the characteristic equation:

$$1 - A(s)\beta(s) = 0$$

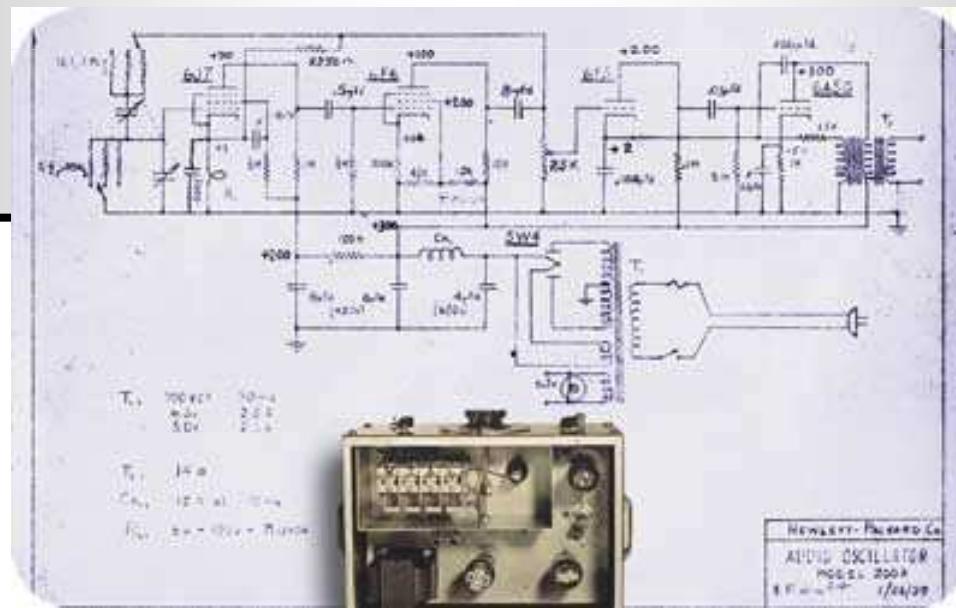
## Loop gain $[A\beta]$ calculation steps



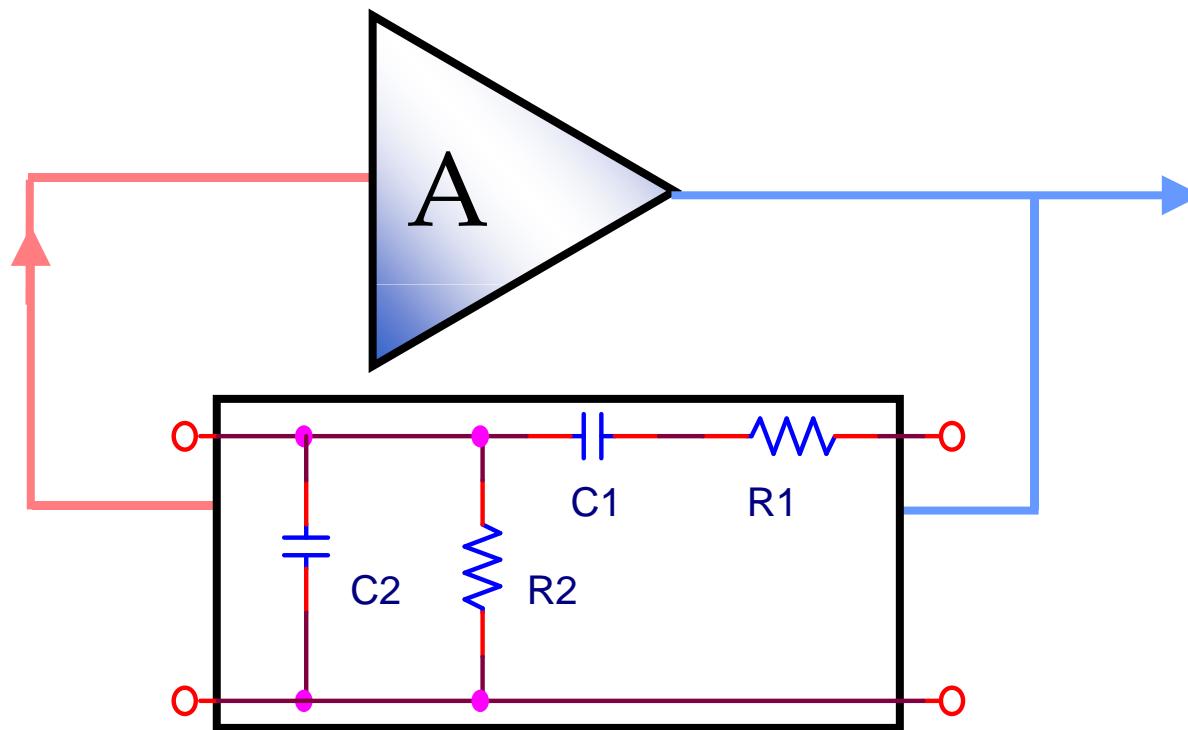
1. Open the feedback loop.
2. Load the output with input impedance,  $Z_{in}$ .
3. Apply an input signal source,  $v_{in}$ .
4. Calculate the transfer function ( $A\beta$ ) as  $v_{out} / v_{in}$ .
5. Apply the Barkhausen criterion by forcing  $v_{out} = v_{in}$ .

## OSCILLATOR EXAMPLE

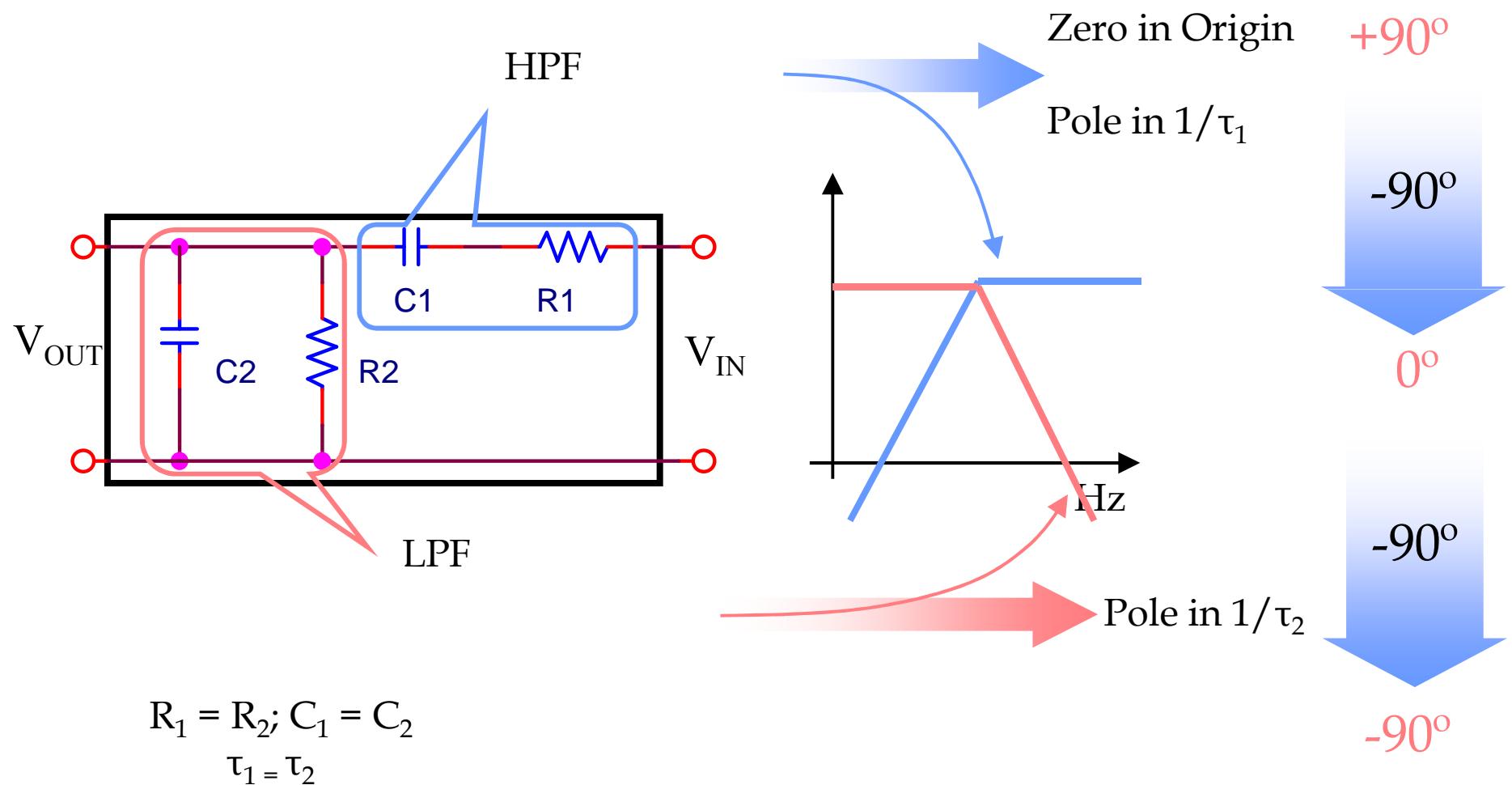
### The Wien bridge oscillator



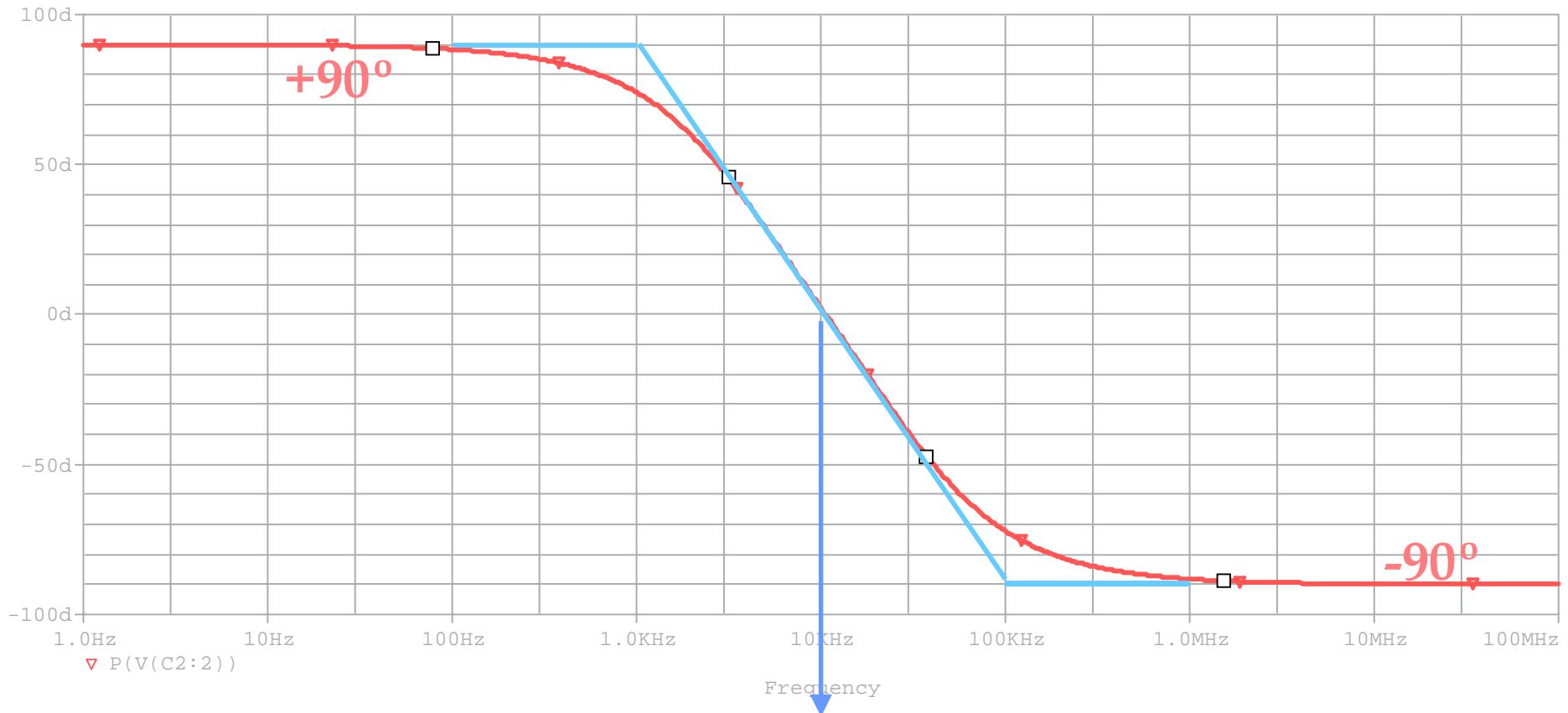
## Wien bridge feedback network



## Qualitative analysis

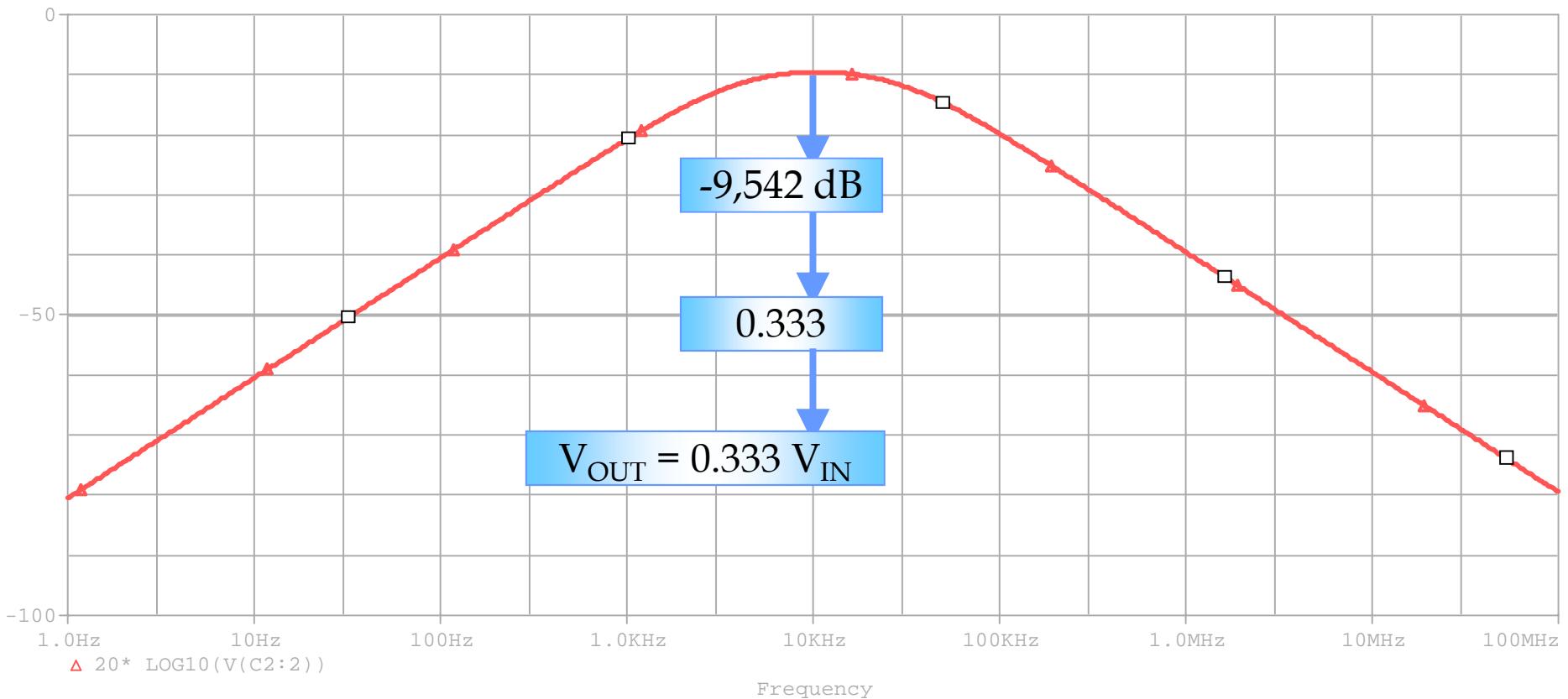


## Qualitative analysis (Phase)



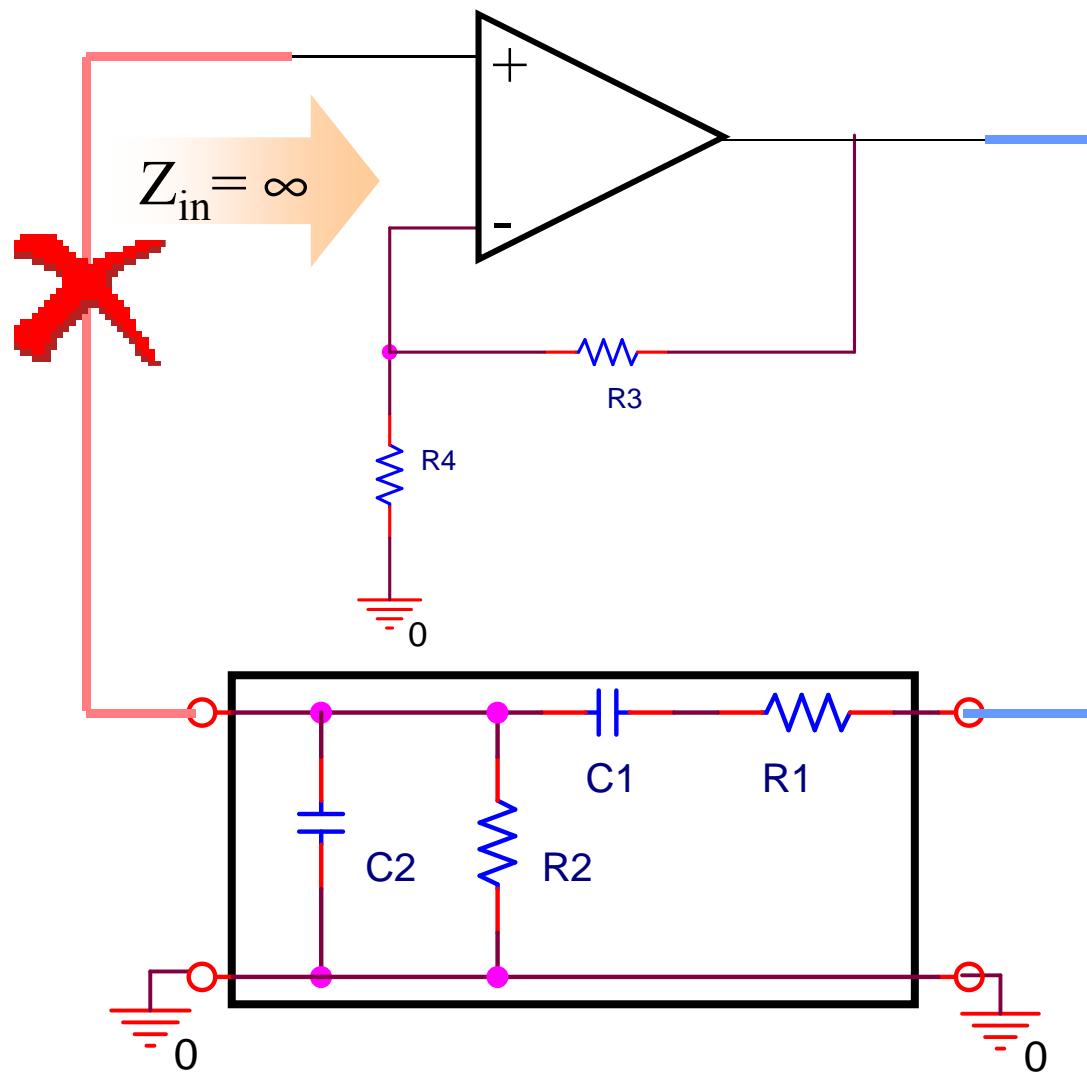
Requires NON-INVERTING AMP

## Qualitative analysis (Gain)

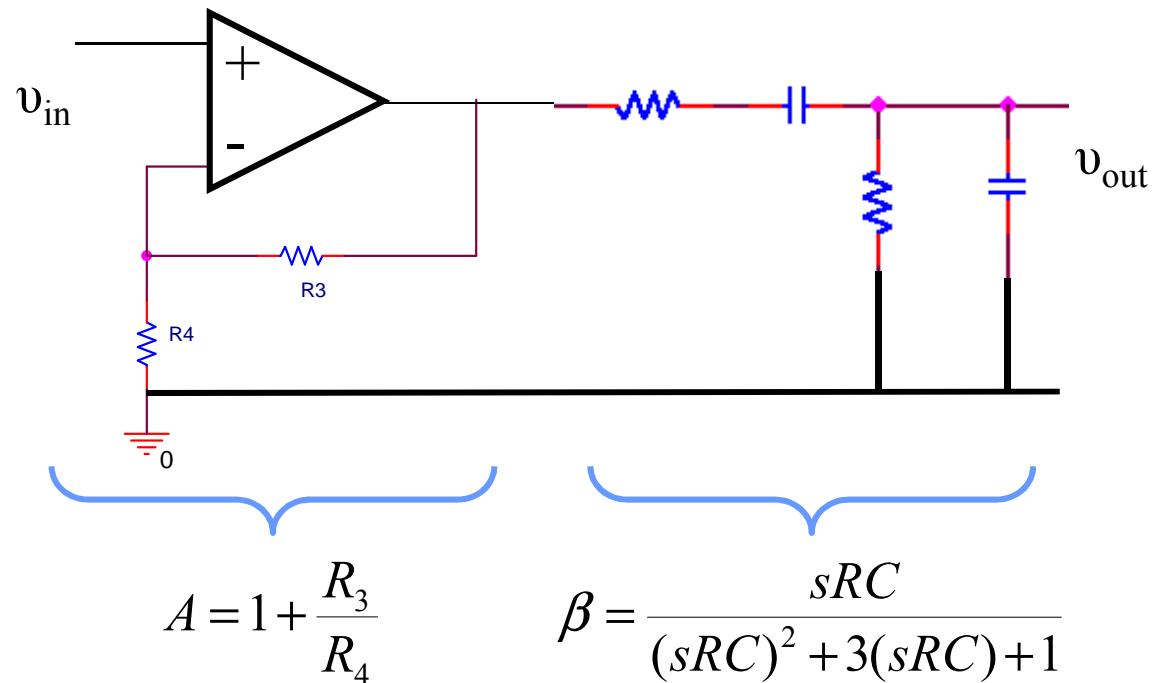


Feedback Network Attenuation level  $\beta = 3 !!$

# Oscillator Configuration



## Loop Gain Calculation



$$A\beta = \left(1 + \frac{R_3}{R_4}\right) \frac{sRC}{(sRC)^2 + 3(sRC) + 1} \Big|_{s=j\omega} = 1$$

## Conditions for Oscillation

$$j\omega RC \left( 1 + \frac{R_3}{R_4} \right) = -(\omega RC)^2 + j3(\omega RC) + 1$$

Phase

$$-(\omega RC)^2 + 1 = 0 \quad \xrightarrow{\hspace{1cm}} \quad \omega_0 = \frac{1}{RC}$$

Gain

$$\left( 1 + \frac{R_3}{R_4} \right) = 3 \quad \xrightarrow{\hspace{1cm}} \quad A = 3$$

## Root Locus

Solve the denominator of the TF,

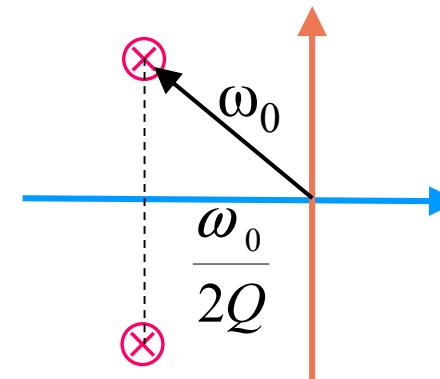
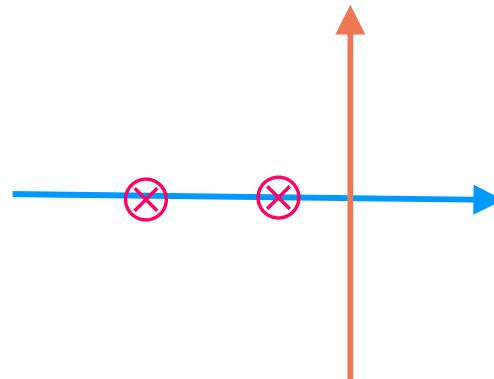
$$1 - A(s)\beta(s) = 0$$

Which results,

A second order system,

$$(sRC)^2 + (3-A)(sRC) + 1 = 0$$

$$s^2 + s \frac{\omega_0}{Q} + \omega_0^2 = 0$$
$$\omega_0 = \frac{1}{RC} \quad Q = \frac{1}{3-A}$$



## Root locus in terms of AMP GAIN

The poles of the second order system result . . .

. . . . two real poles

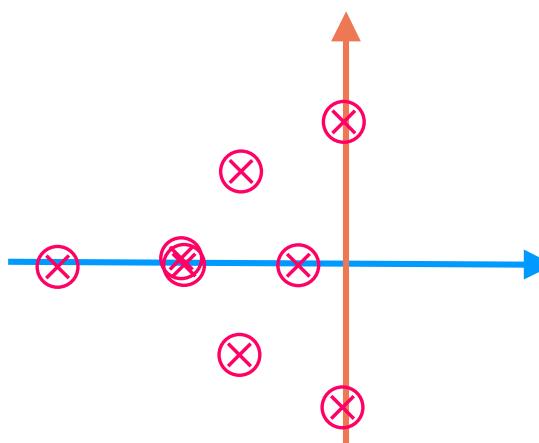
IF  $Q < 0.5 \rightarrow A < 1$

. . . . two complex conjugate

IF  $Q > 0.5 \rightarrow A > 1$

. . . . In the imaginary axis

IF  $Q = \infty \rightarrow A = 3$



# Some results

## **Wien Bridge Oscillator without Amplitude Control.**

With  $A = 3$

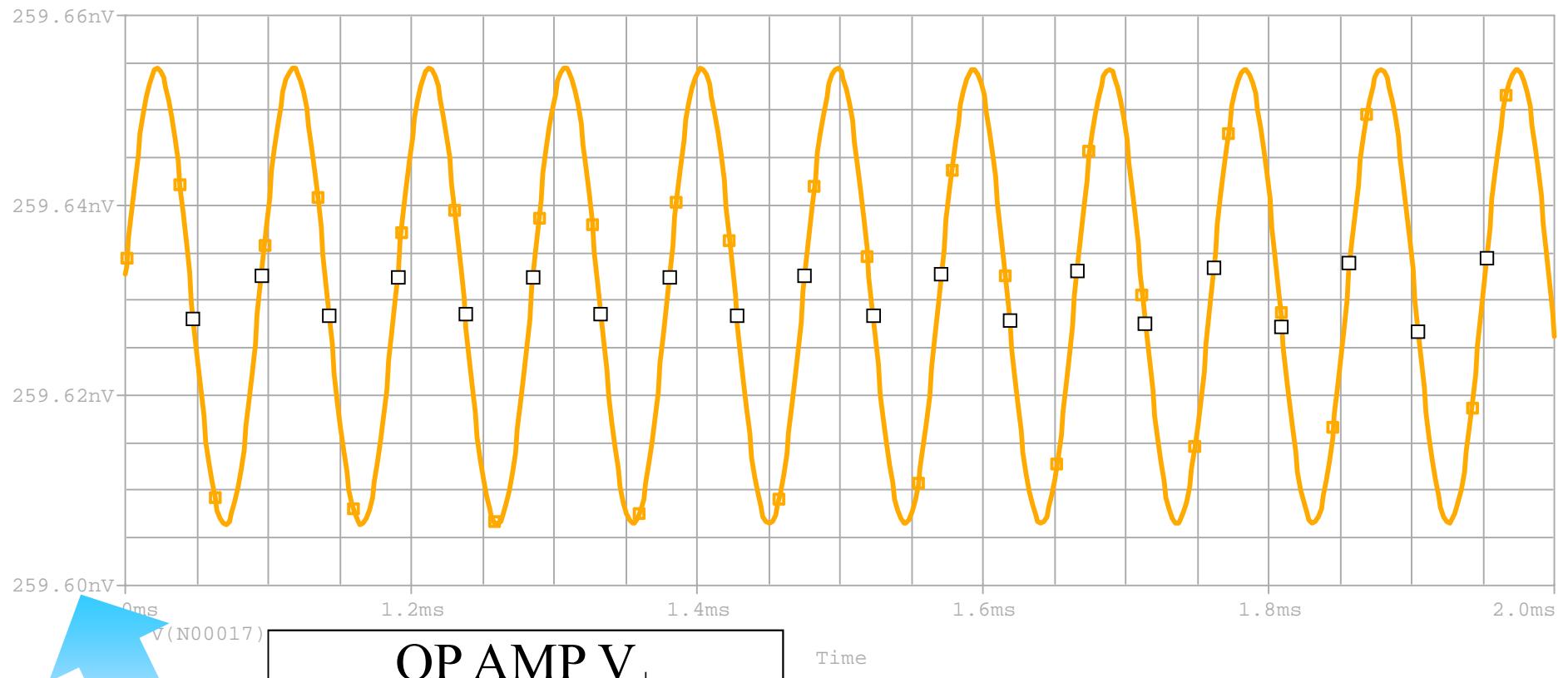
With  $A = 3.2$

## **Wien Bridge Oscillator with Amplitude Control**

with Light Bulb

Ohm region FET

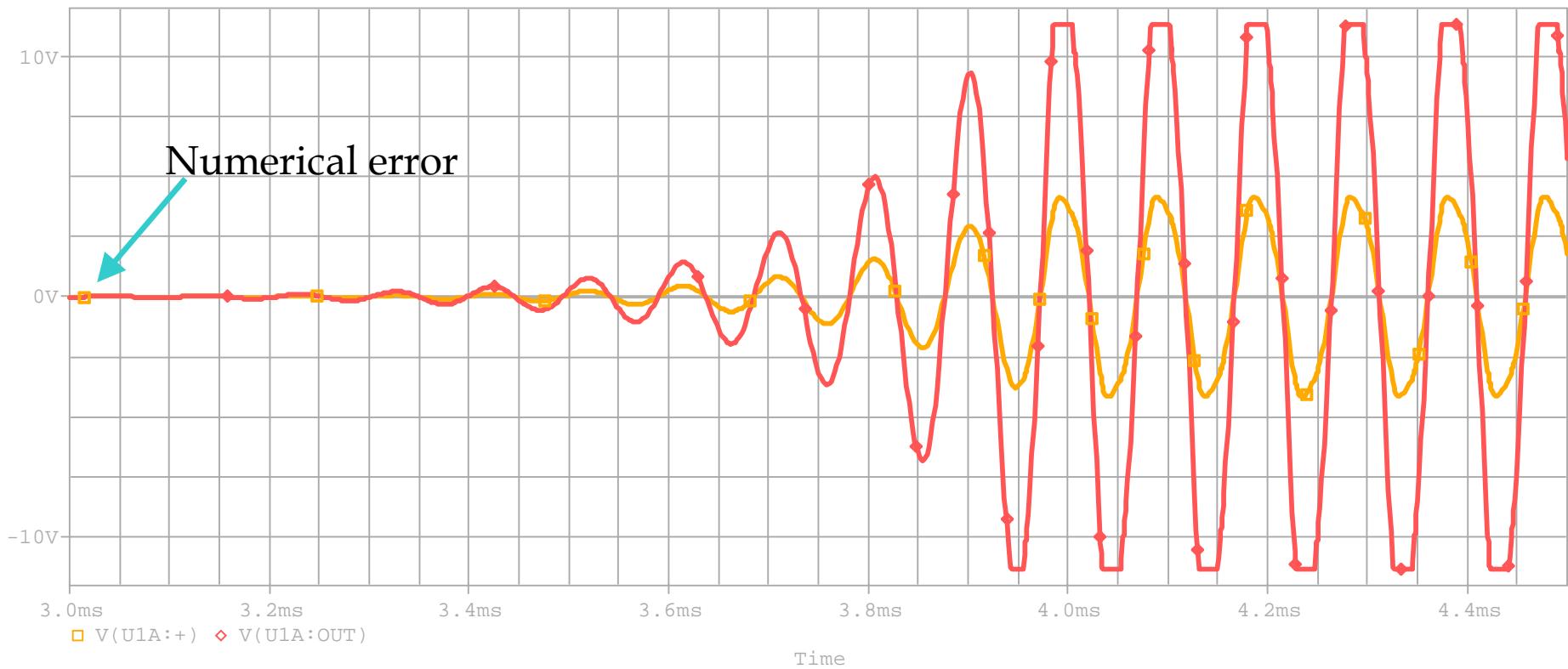
# Spice analysis with $A = 3$



No practical use!

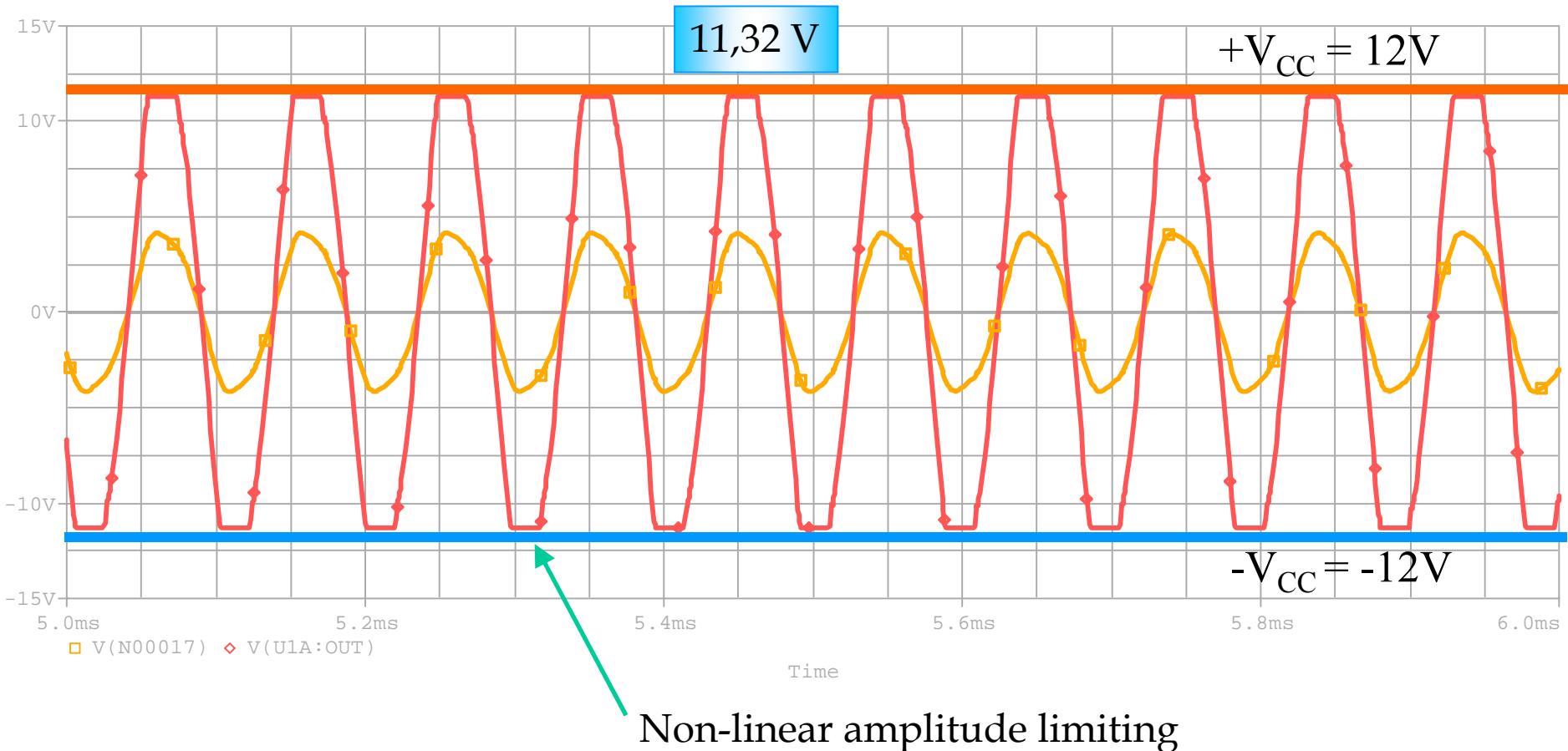
## Spice analysis with A = 3,2

Start up.



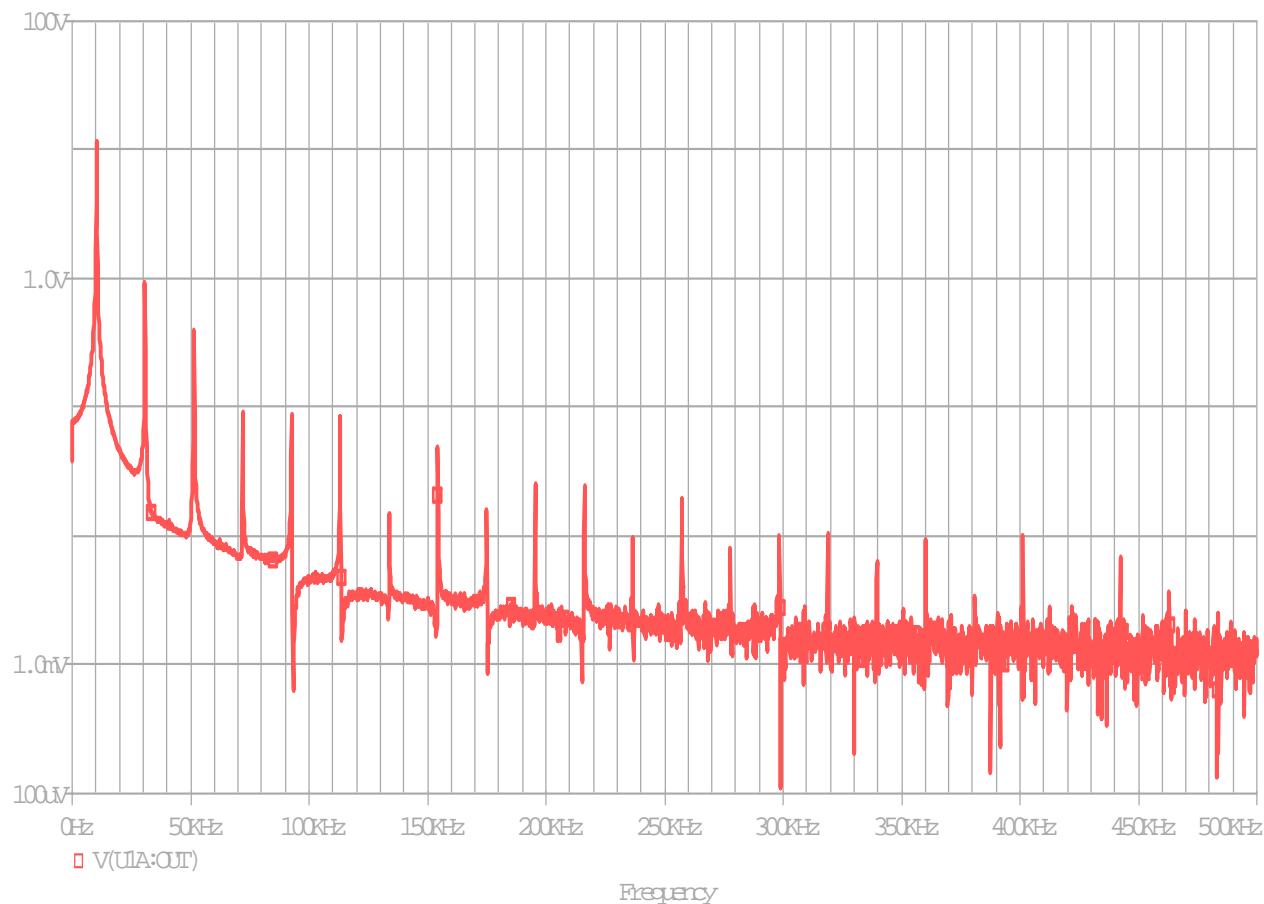
# Spice analysis with $A = 3,2$

CW oscillation



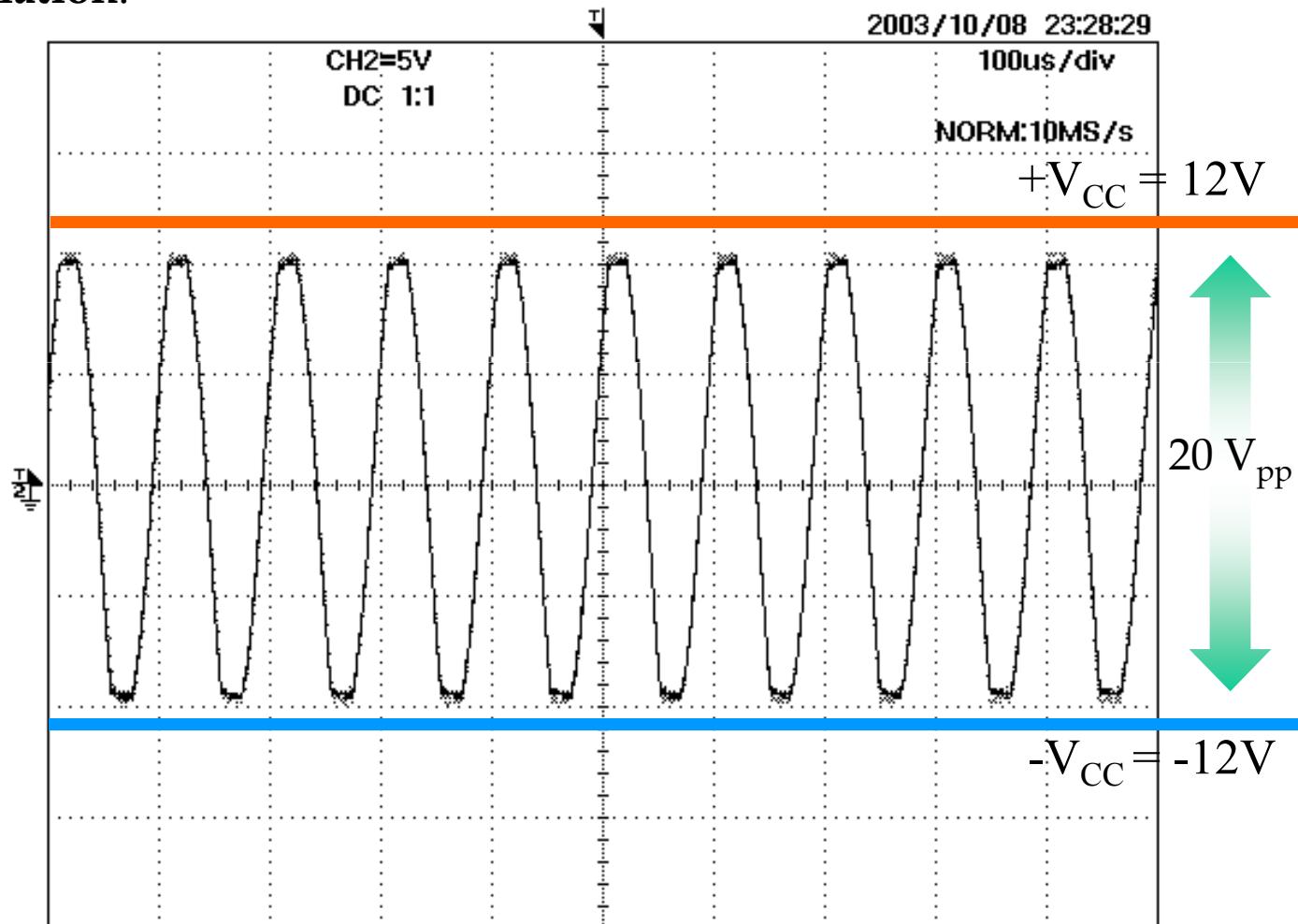
# Spice analysis with $A = 3,2$

Fourier picture of the oscillation.



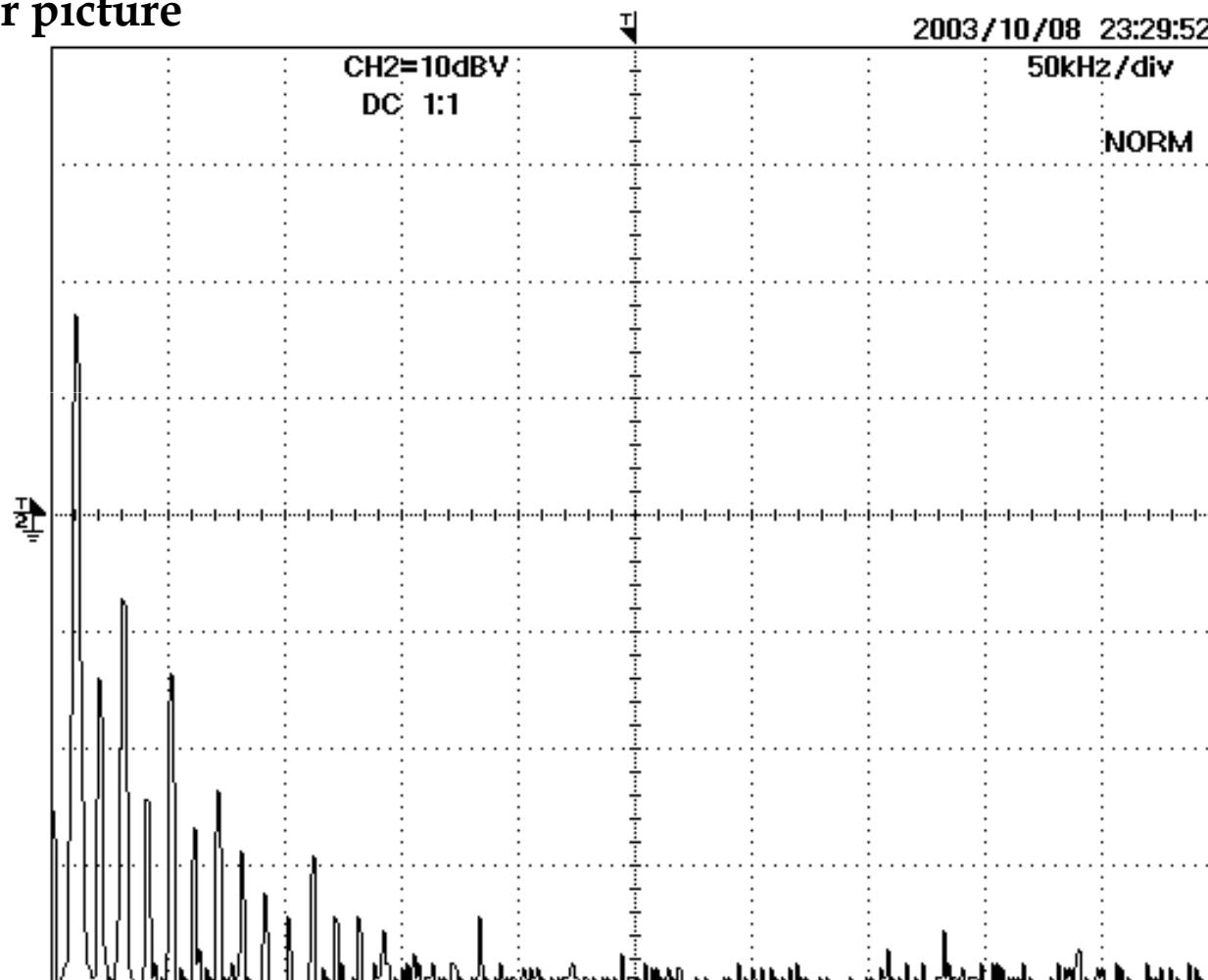
# The real thing with $A = 3,2$

CW oscillation.

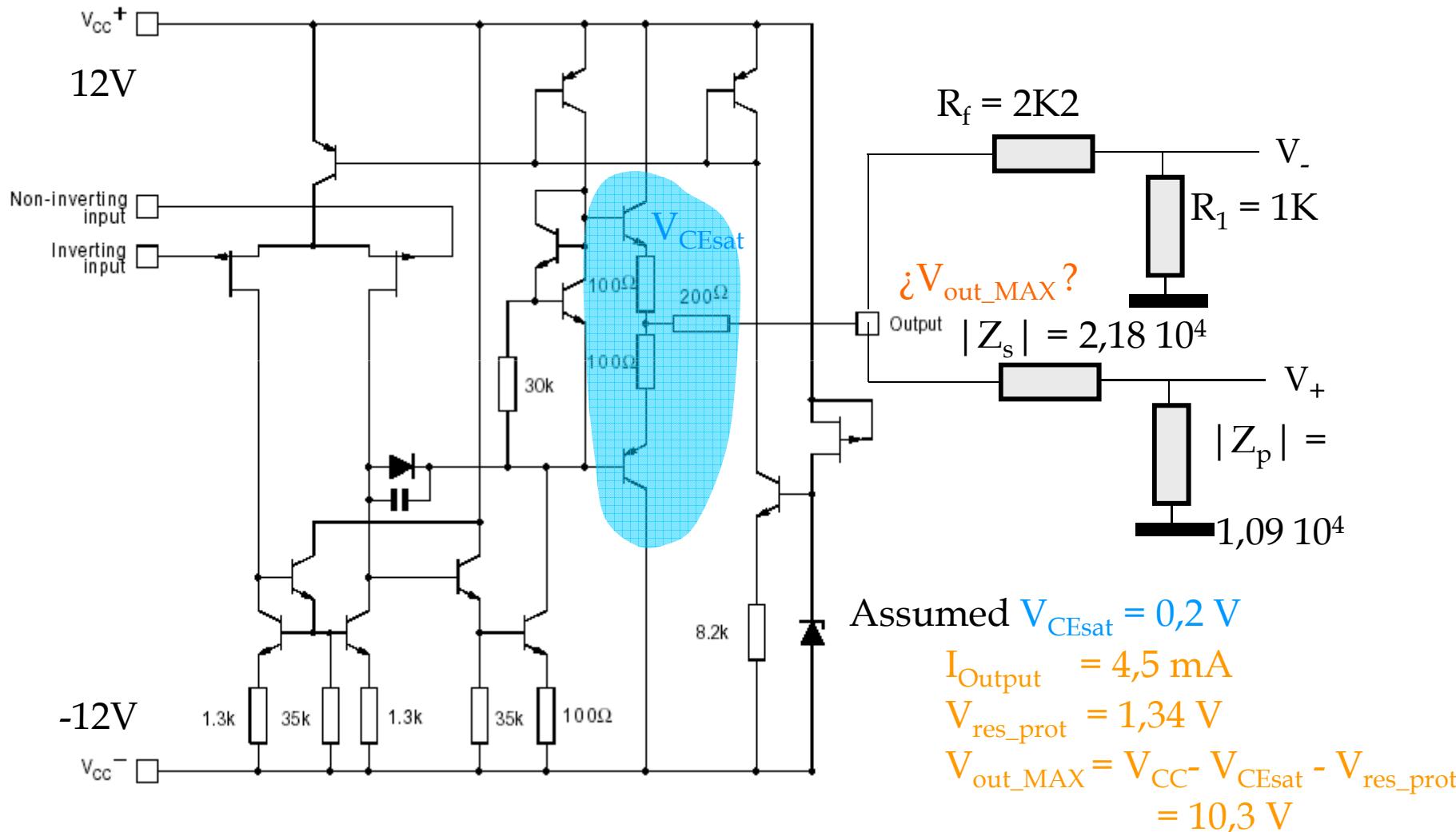


# The real thing with A = 3,2

Fourier picture

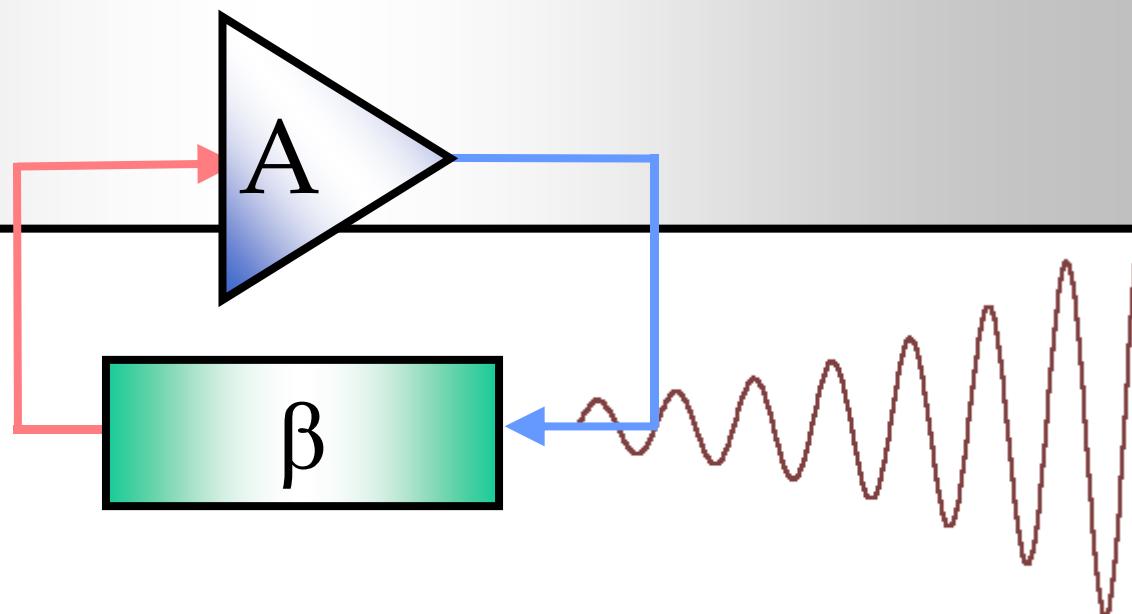


# Non-linear amplitude limitation



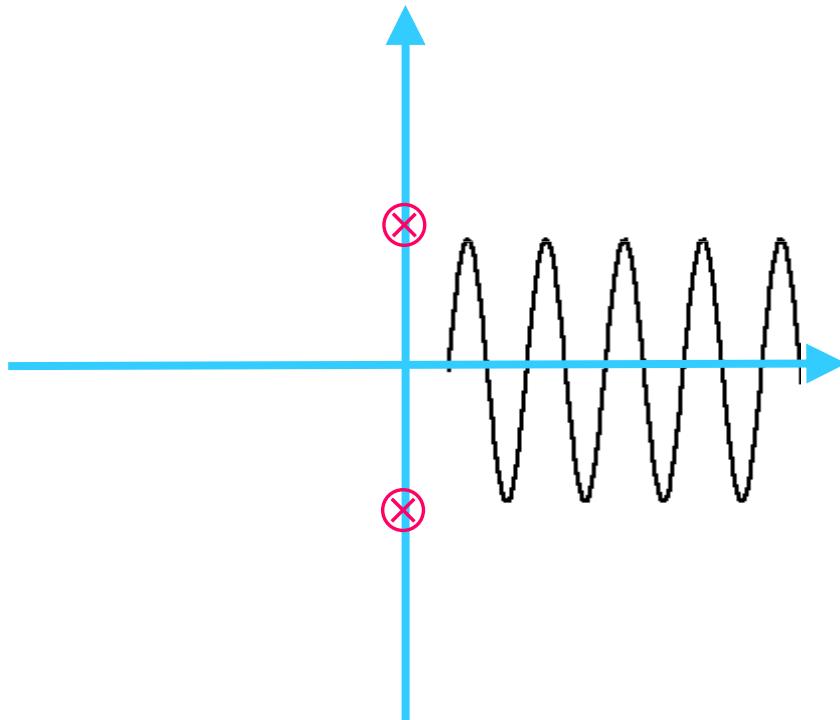
## OSCILLATOR AMPLITUDE CONTROL

### Wien Bridge Example



## What we do know

For an oscillator to operate properly, requires  $|A\beta|=1$  (PRECISE)

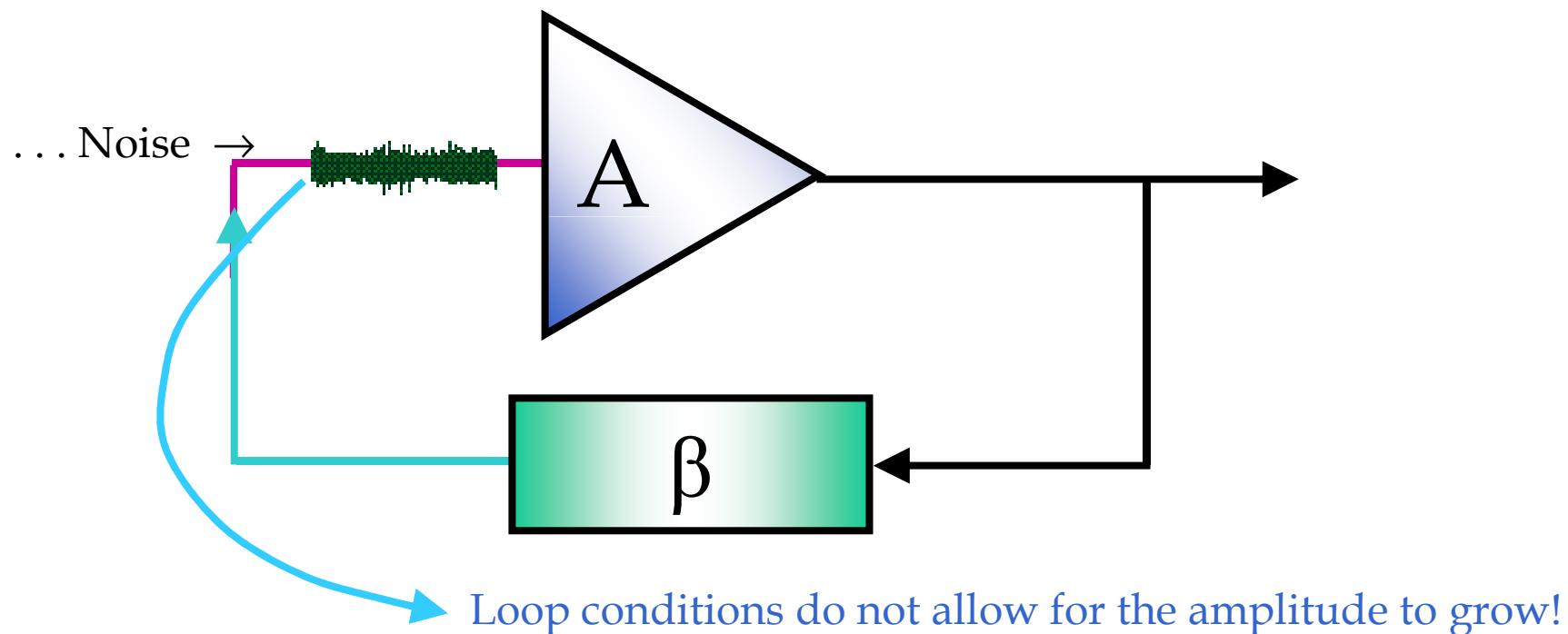


A precise adjustment of the Amplifier gain to exactly compensate for the feedback network losses in the loop.

Precise adjustment of amplifier gain → Use of feedback.

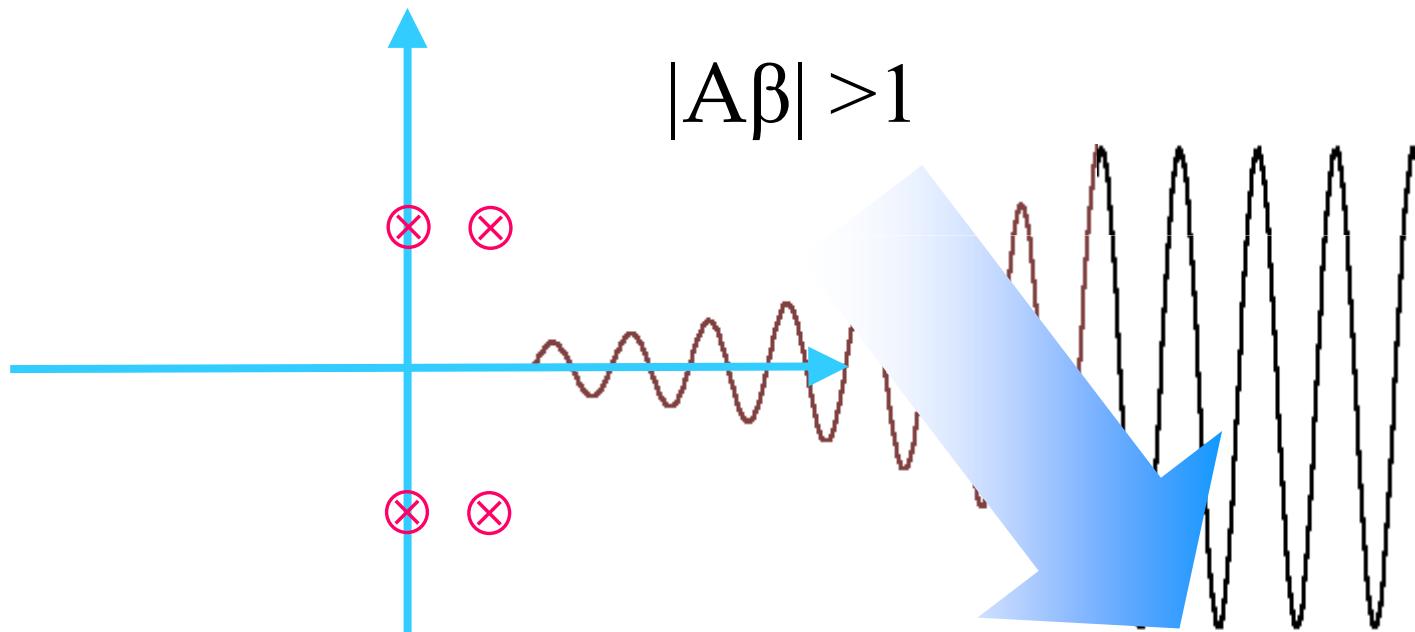
## Oscillation turn-on

Gain = Loss means poles are on the imaginary axis, which allows to sustain oscillation. However, at turn-on time, the oscillation amplitude is given by noise



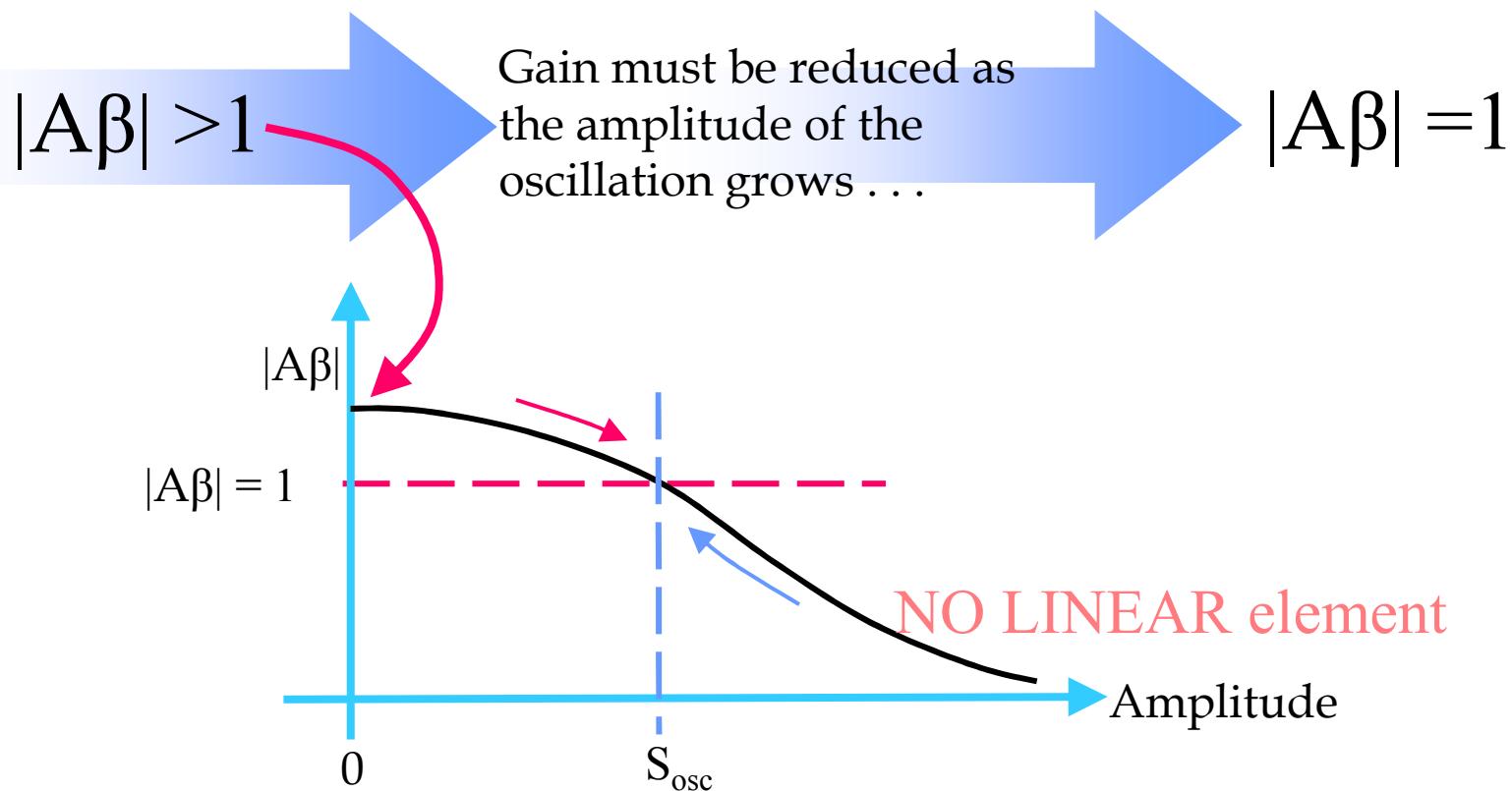
## Oscillation turn-on

We need to build in a system that when the oscillation amplitude is low, locates the system poles on the right hand side . . .



. . . And as the amplitude grows, the poles move  $|A\beta| = 1$  onto the imaginary axis, therefore, sustaining the oscillation at a desired amplitude level.

## Automatic Gain Control (AGC) system



## Elementos necesarios de un oscilador (y II)



**Amplificador Básico, ...**

que proporciona **GANANCIA** (con un desfase).



**Red de realimentación, ...**

**SELECTIVA EN FRECUENCIA** para determinar la frecuencia de oscilación, y que además introduce **PÉRDIDAS**.

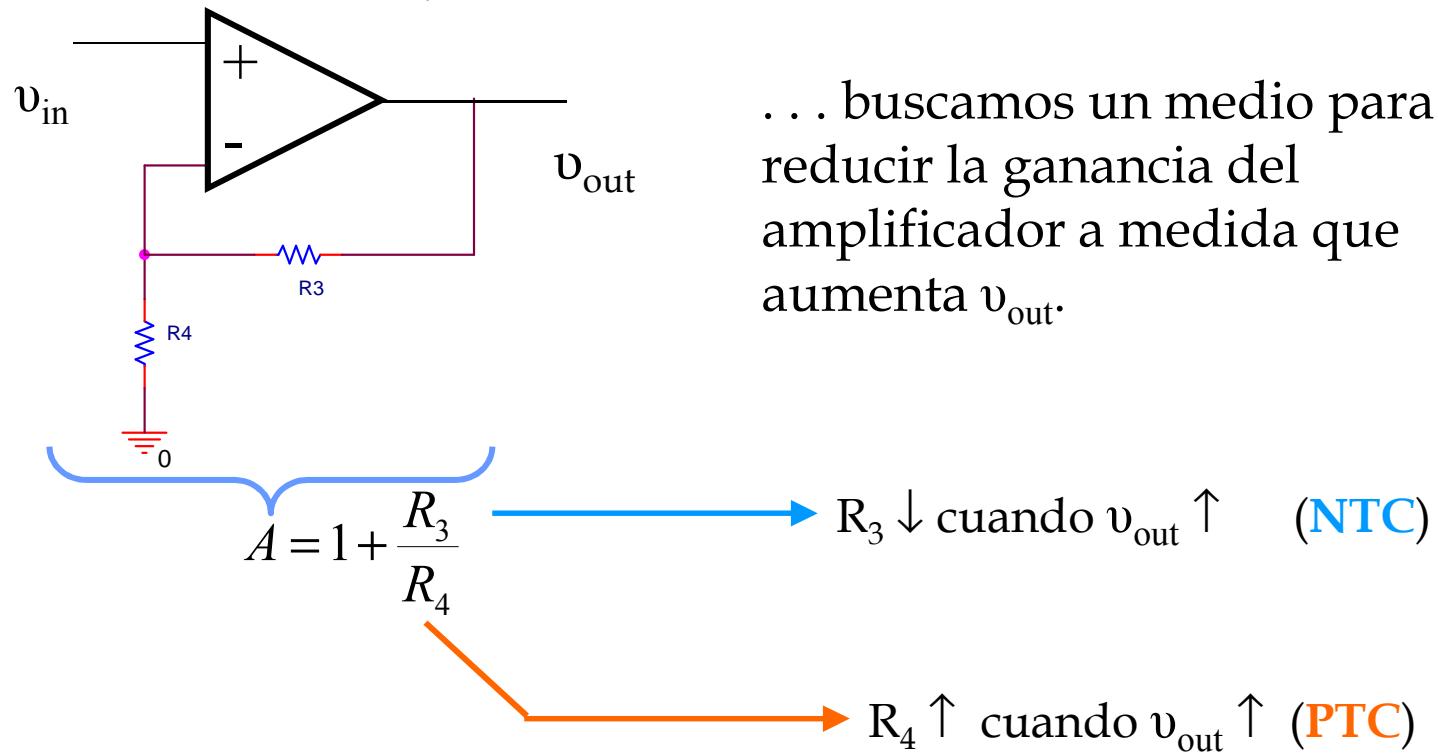


**Control no lineal de la ganancia, ...**

que permite **ARRANCAR** al oscilador a partir del ruido.

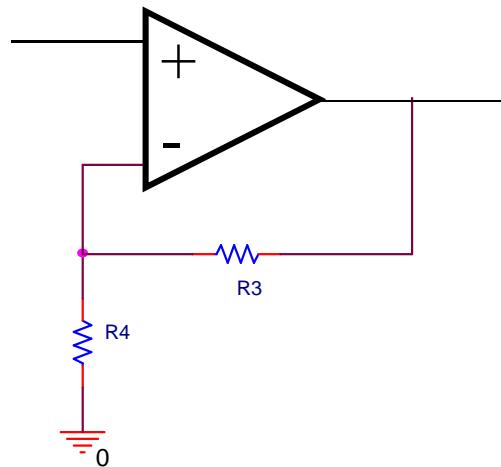
## Control de la amplitud. Bases

Fijada inicialmente (cuando  $v_{\text{out}} = 0$ )  $|A\beta| > 1, \dots$



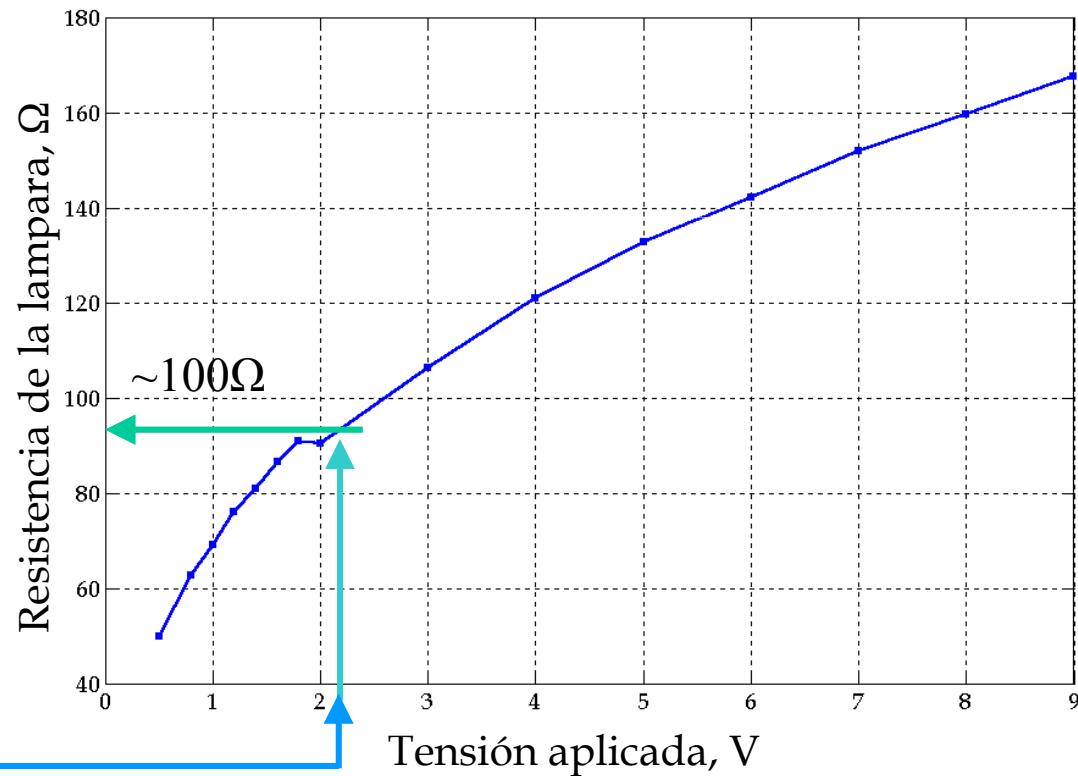
**IMPORTANTE:** La constante de tiempo de variación de la resistencia  $\tau \gg T_{\text{osc}}$

# Control de la amplitud con lampara incandescente (I)

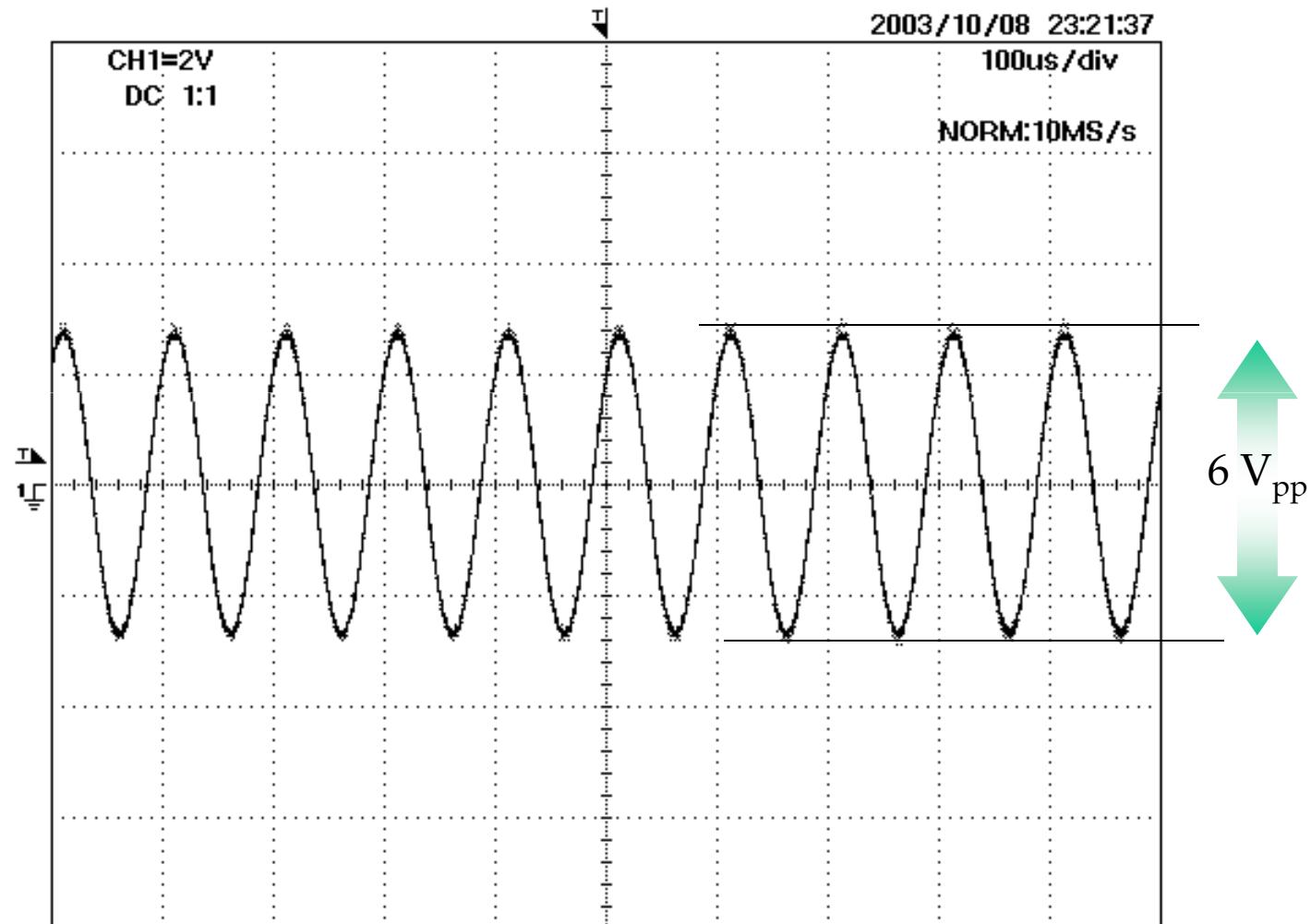


$$V_{\text{OUT}} = 3 \text{ V}$$

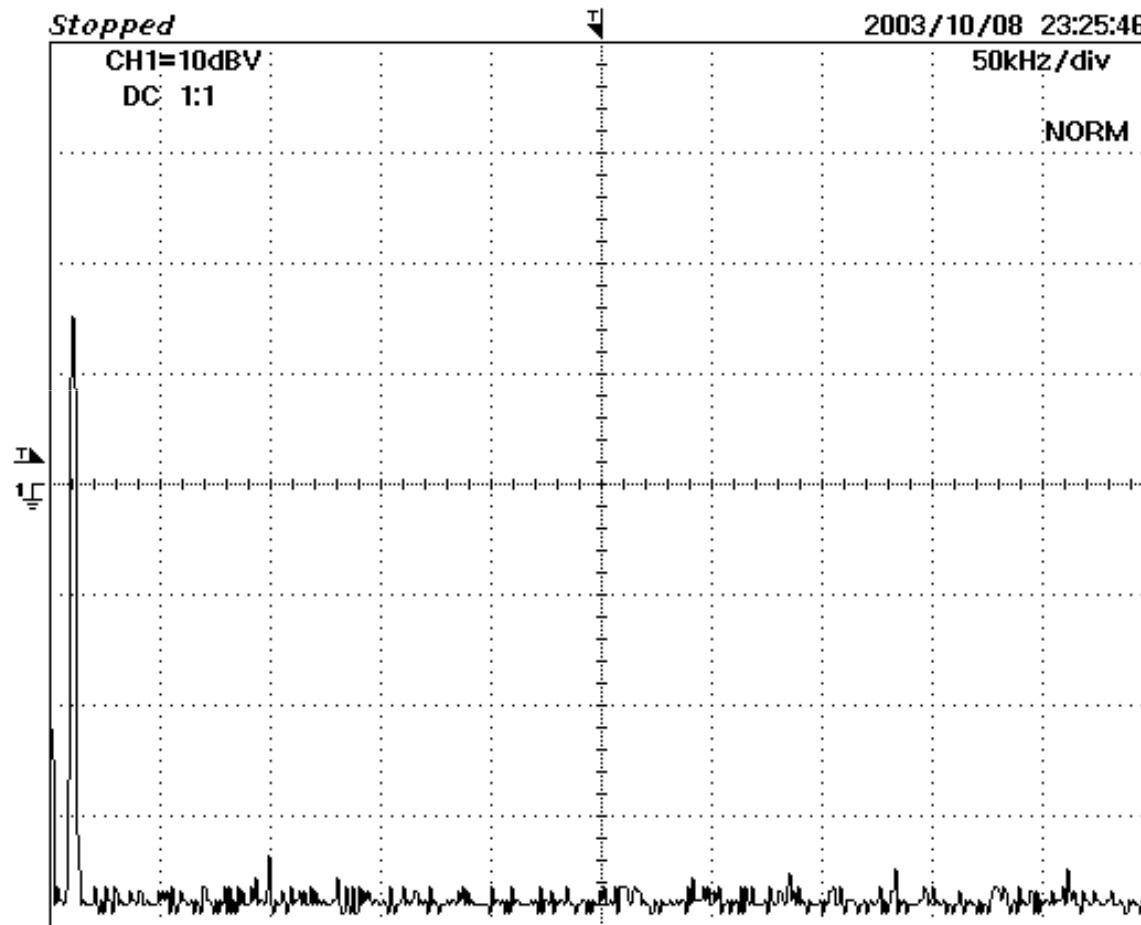
$$V_{\text{OUT\_rms}} = 2.12 \text{ V}$$



## Control de la amplitud con lampara incandescente (II)

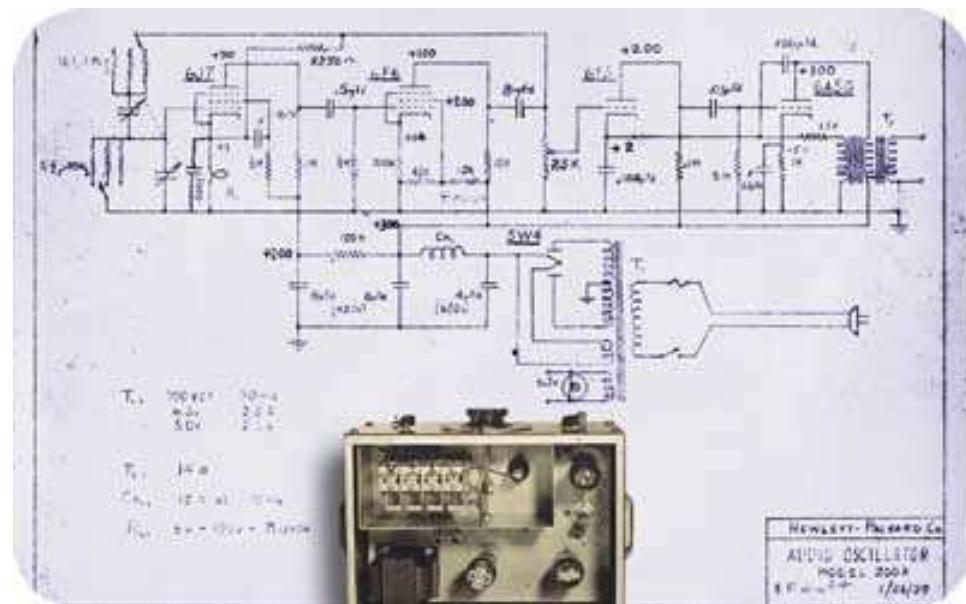


## Control de la amplitud con lampara incandescente (III)



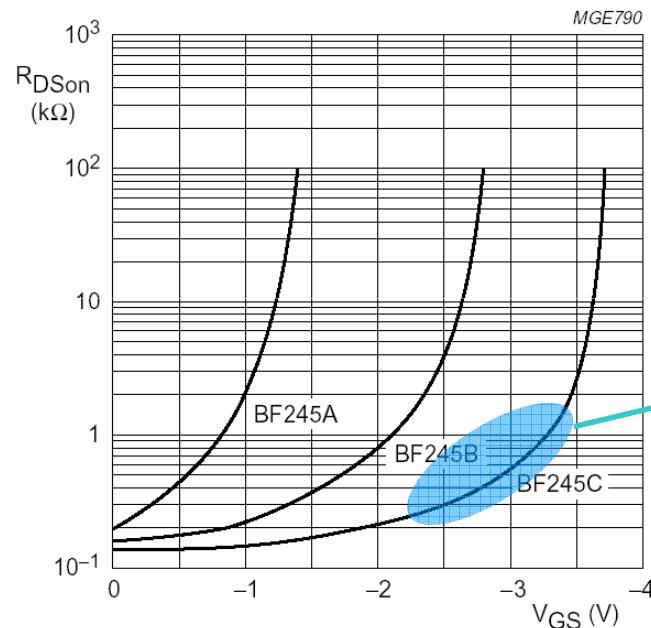
## Control de la amplitud, Bill Hewlett y HP

En Enero del 2002, HP celebró el 60<sup>th</sup> aniversario de la patente de Bill Hewlett sobre el oscilador de audio HP 200A.



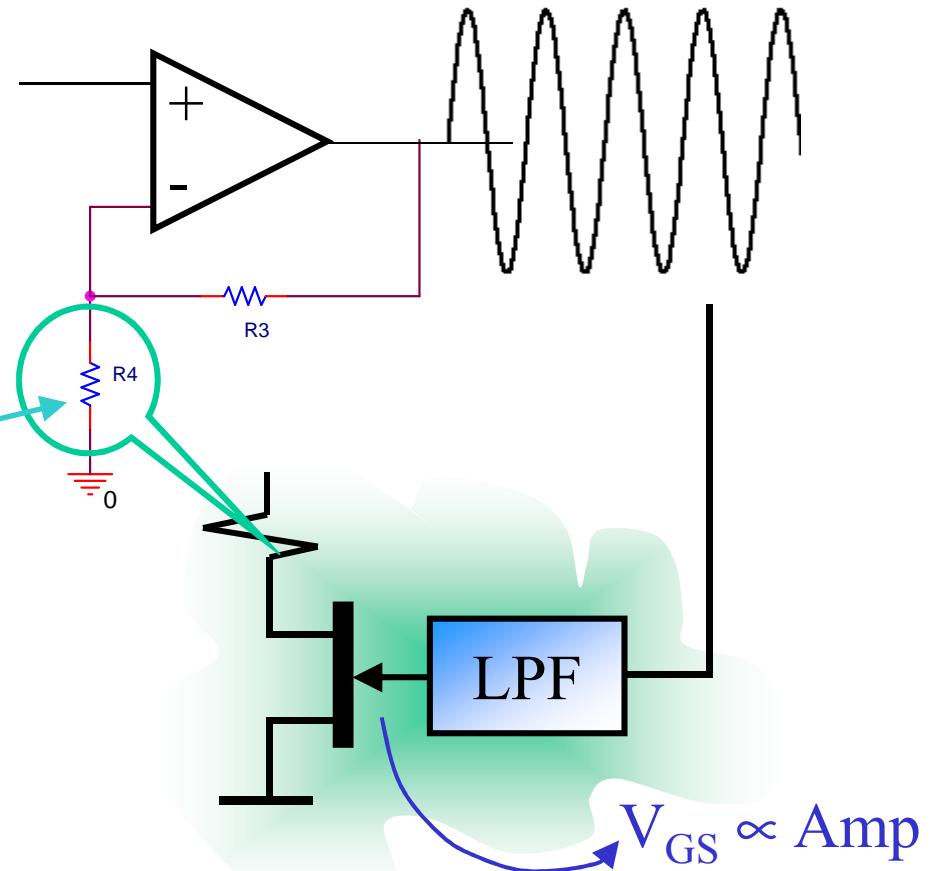
# Control de la amplitud con FET en zona Ohmica

Resistencia variable del FET ( $V_{ds} \ll$ )

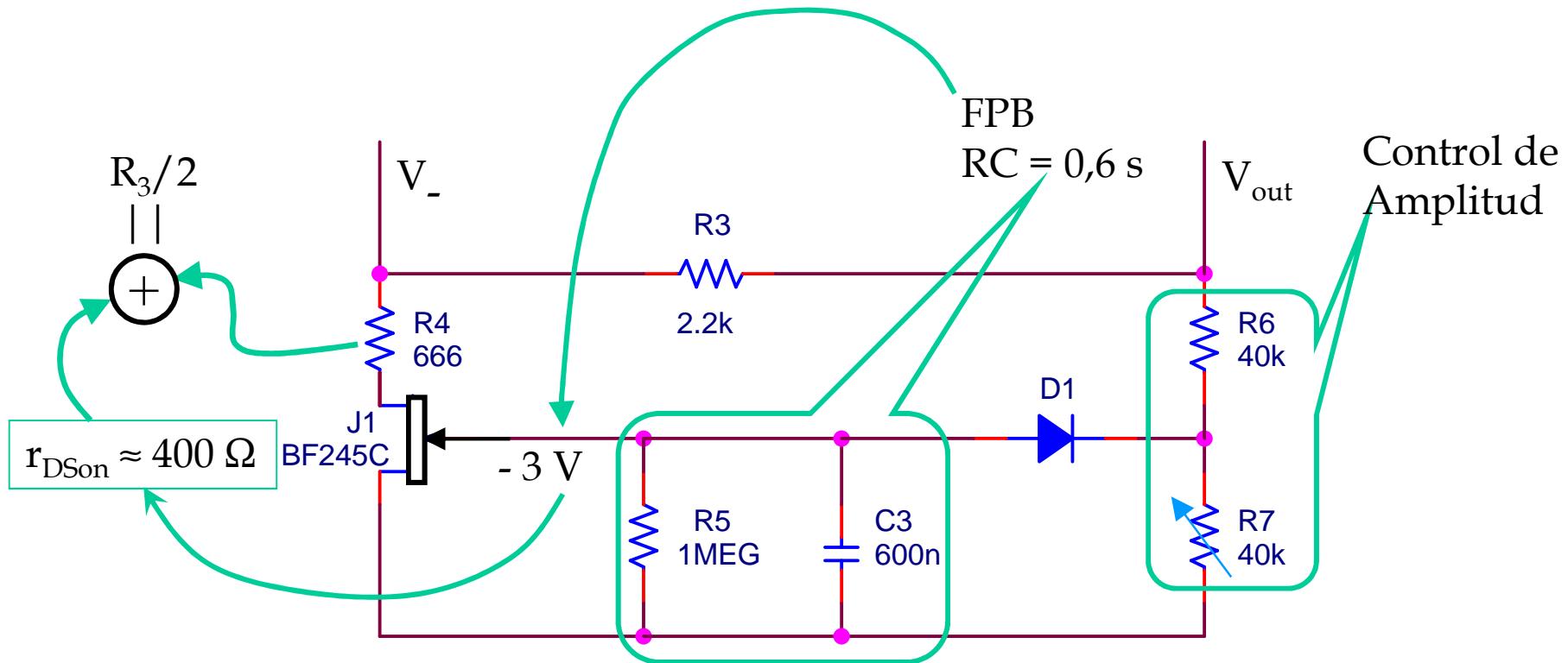


$V_{DS} = 0$ ;  $f = 1$  kHz;  $T_{amb} = 25$  °C.

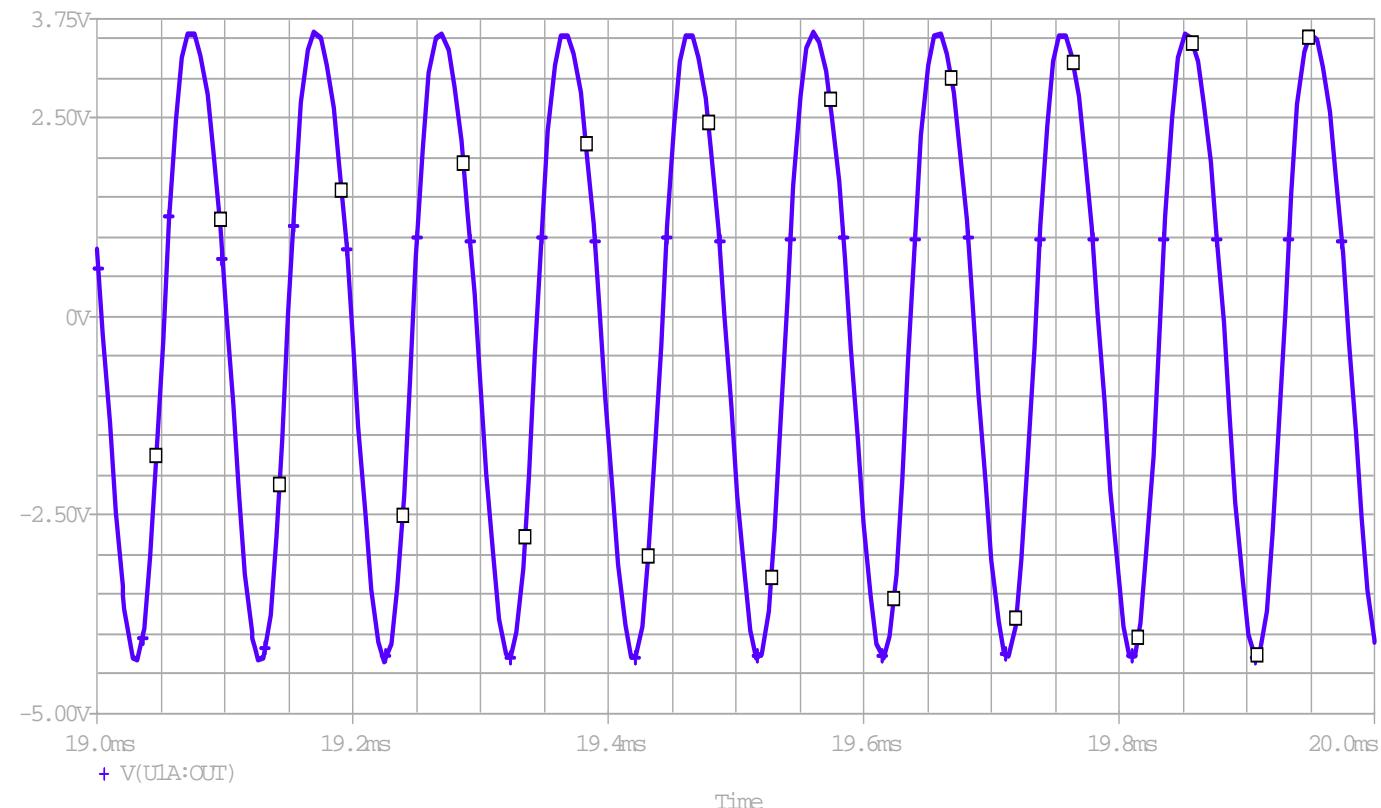
Fig.20 Drain-source on-state resistance as a function of gate-source voltage;  
typical values.



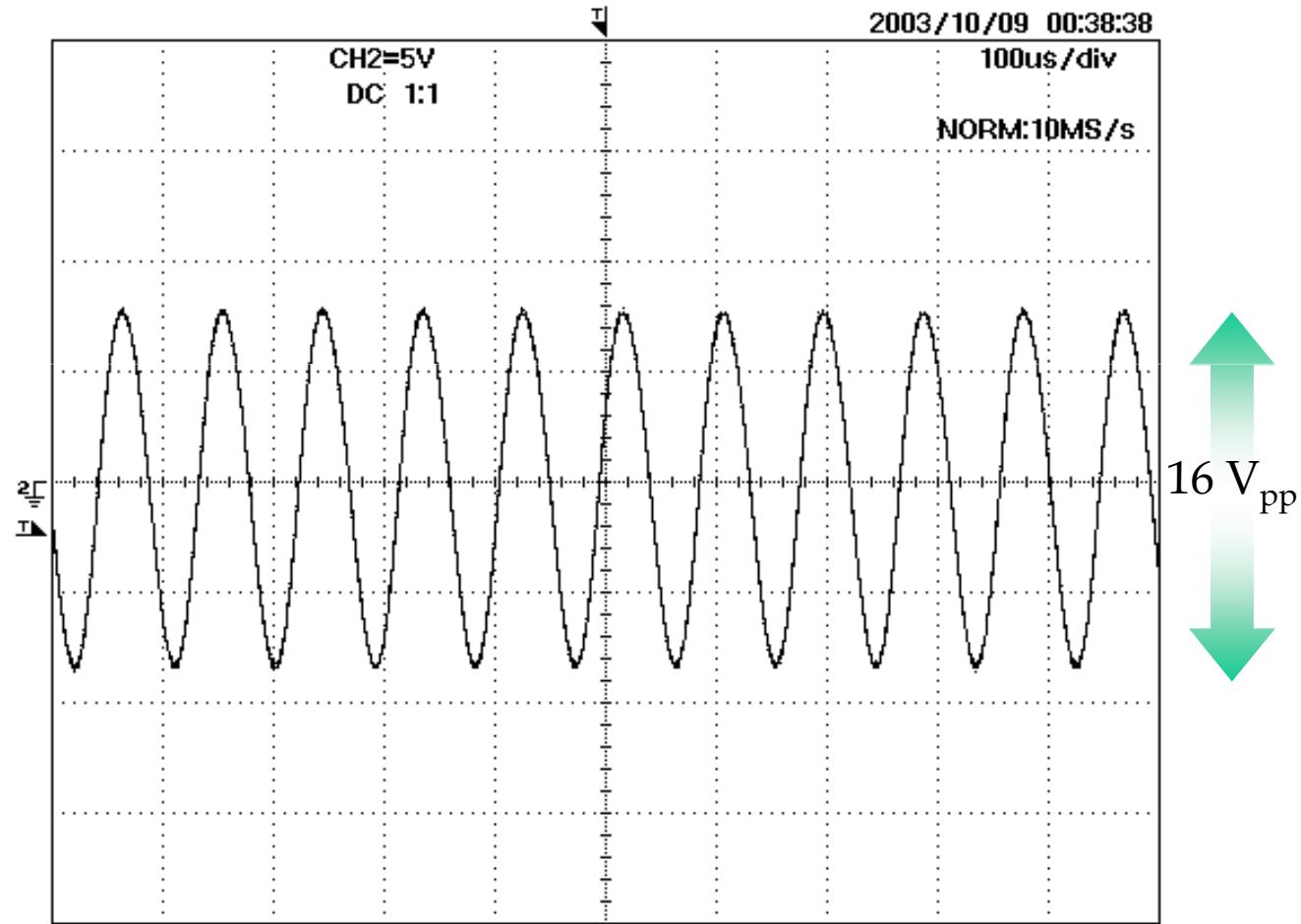
# Control de la amplitud con FET en zona Ohmica



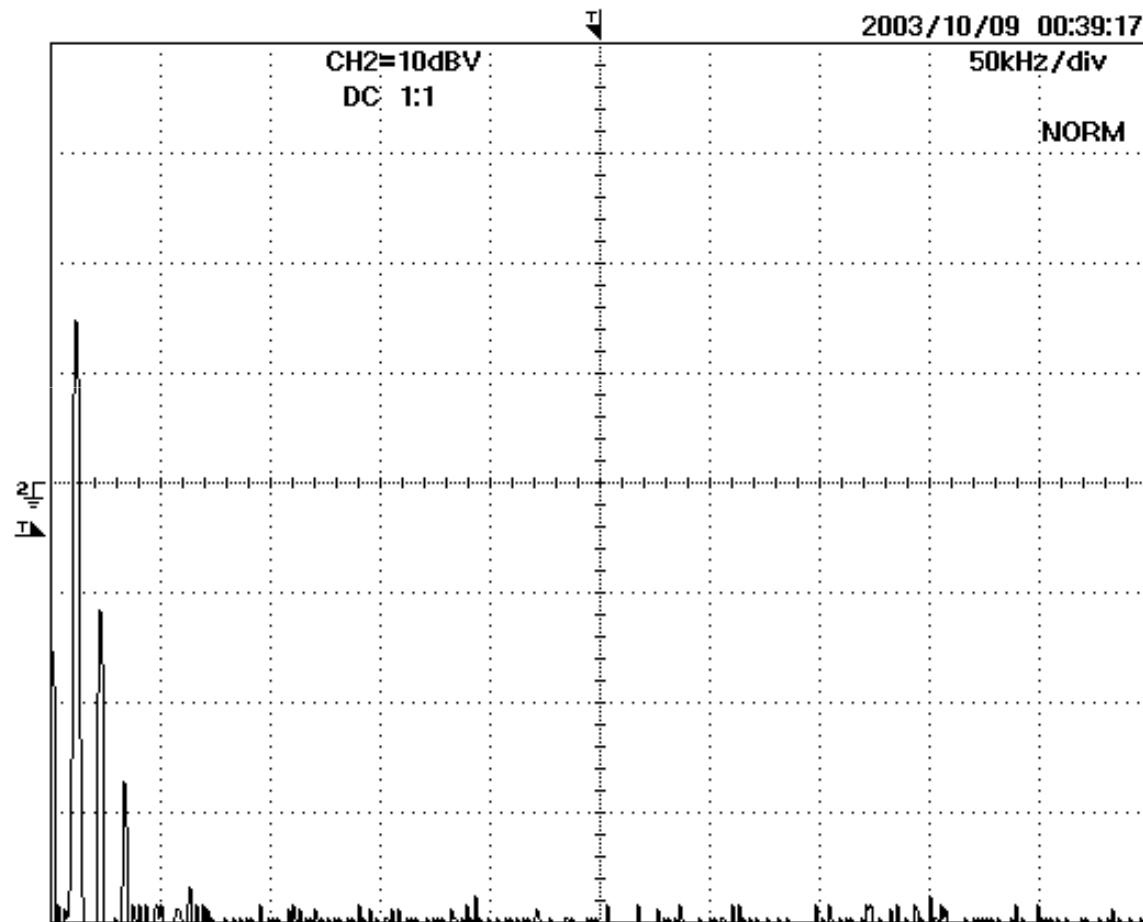
## Control de la amplitud con FET en zona Ohmica



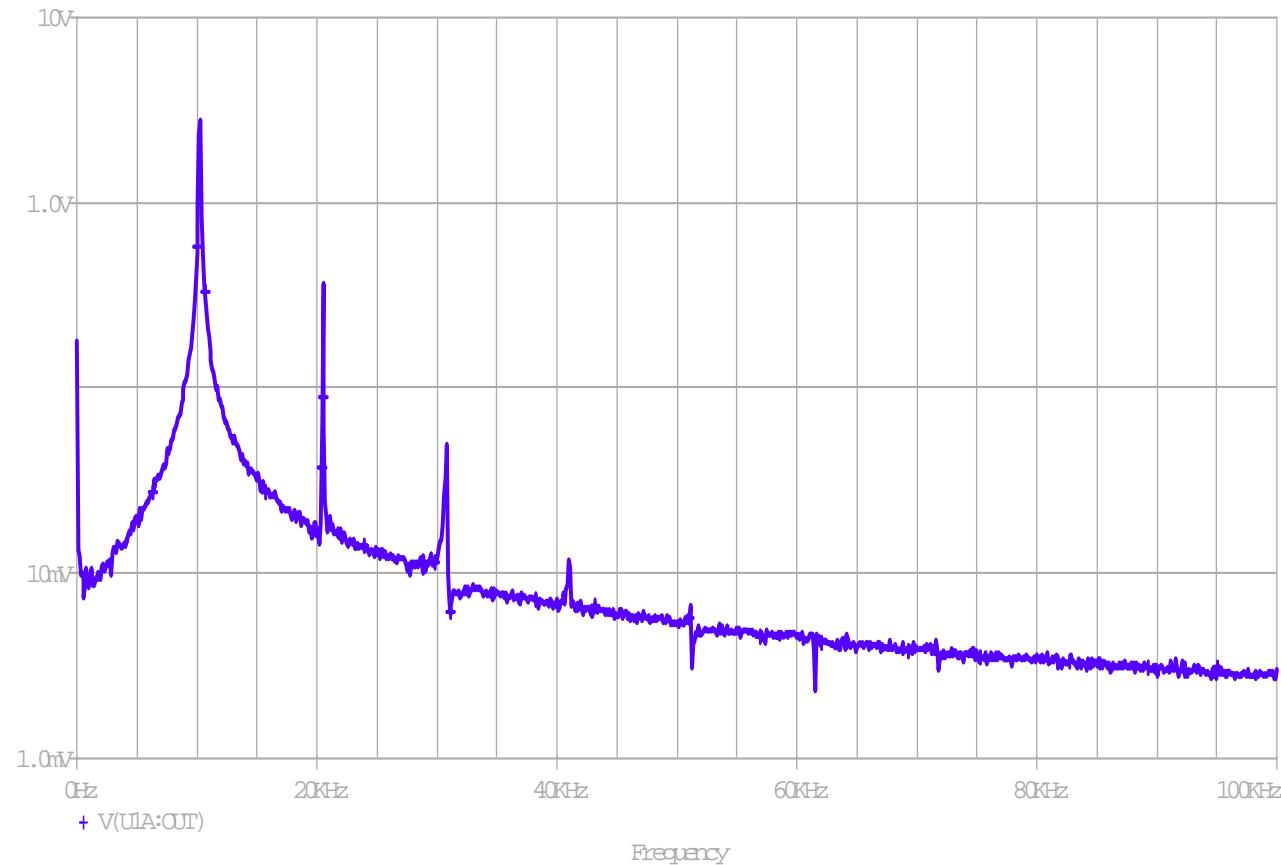
## Control de la amplitud con FET en zona Ohmica



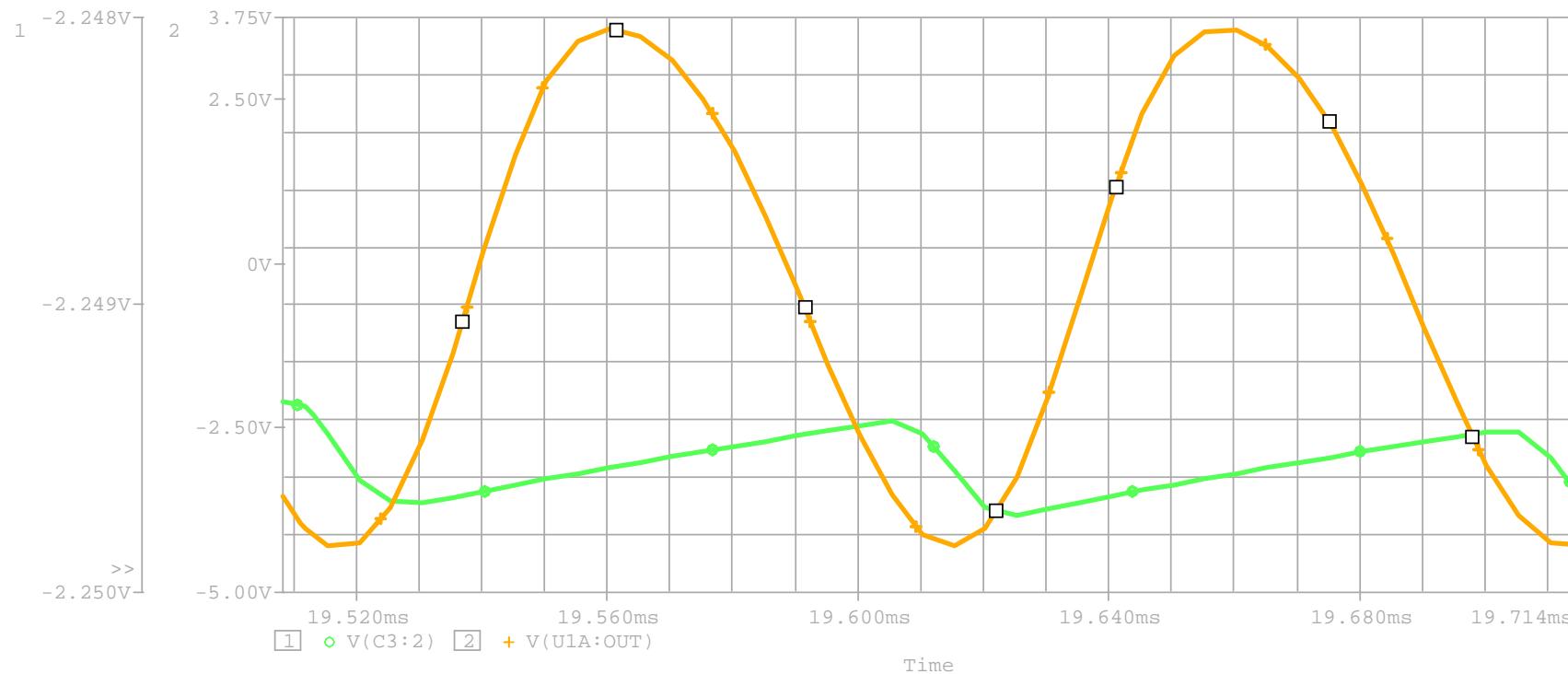
# Control de la amplitud con FET en zona Ohmica



# Control de la amplitud con FET en zona Ohmica

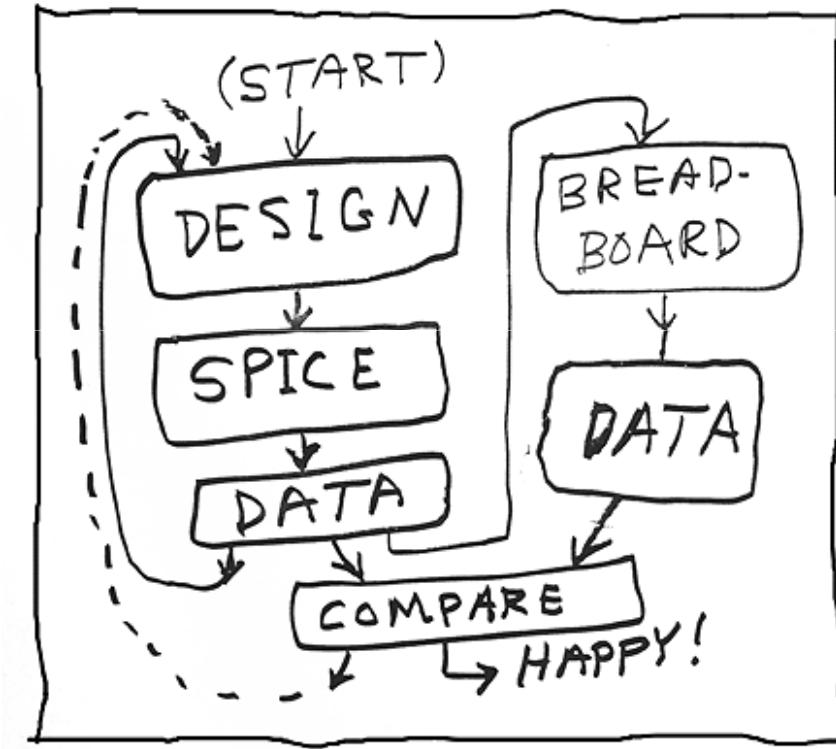


## Control de la amplitud con FET en zona Ohmica



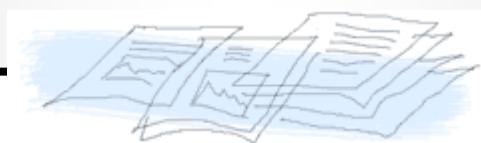
$C_3$  se carga sólo en periodos negativos, debido al diodo.  
Los procesos de carga y descarga son asimétricos en cada semiperíodo de la oscilación, y esta es por tanto, asimétrica.

# Pease y SPICE



"What's All This Spicey Stuff (Part I)," Electronic Design, November 22, 1990, p. 127  
"What's All This Spicey Stuff (Part II)," Electronic Design, December 13, 1990, p. 87

# CONCLUSIONES



## Conclusión

Importancia de la fase en el lazo de realimentación.

Importancia de la red de realimentación:

Determina la frecuencia de oscilación

Determina la ganancia necesaria del amplificador.

Importancia del control de amplitud

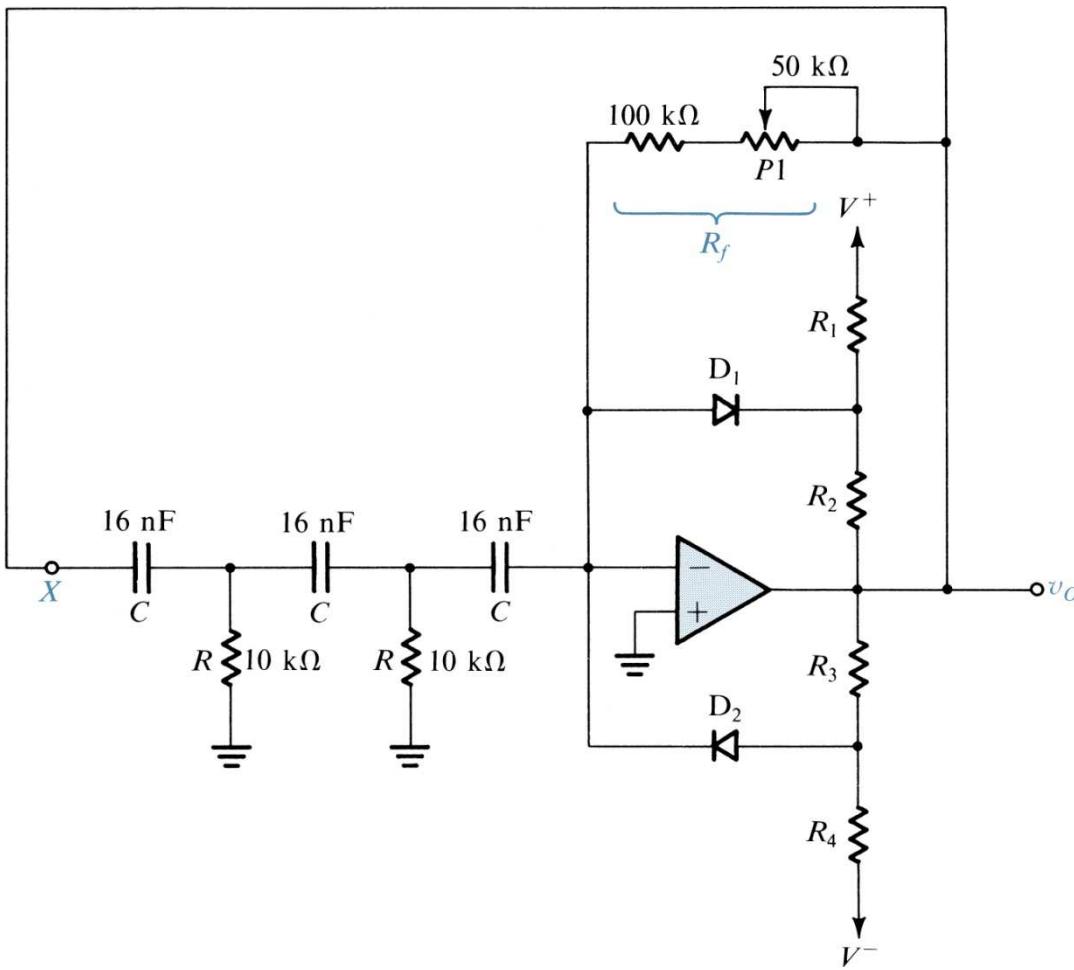
Pasos (iterativos):

1. Analítico
2. Simulación
3. Implementación.

Atención a los efectos del operacional: “Slew Rate” y GxBW

# **ANÁLISIS DE UN OSCILADOR**

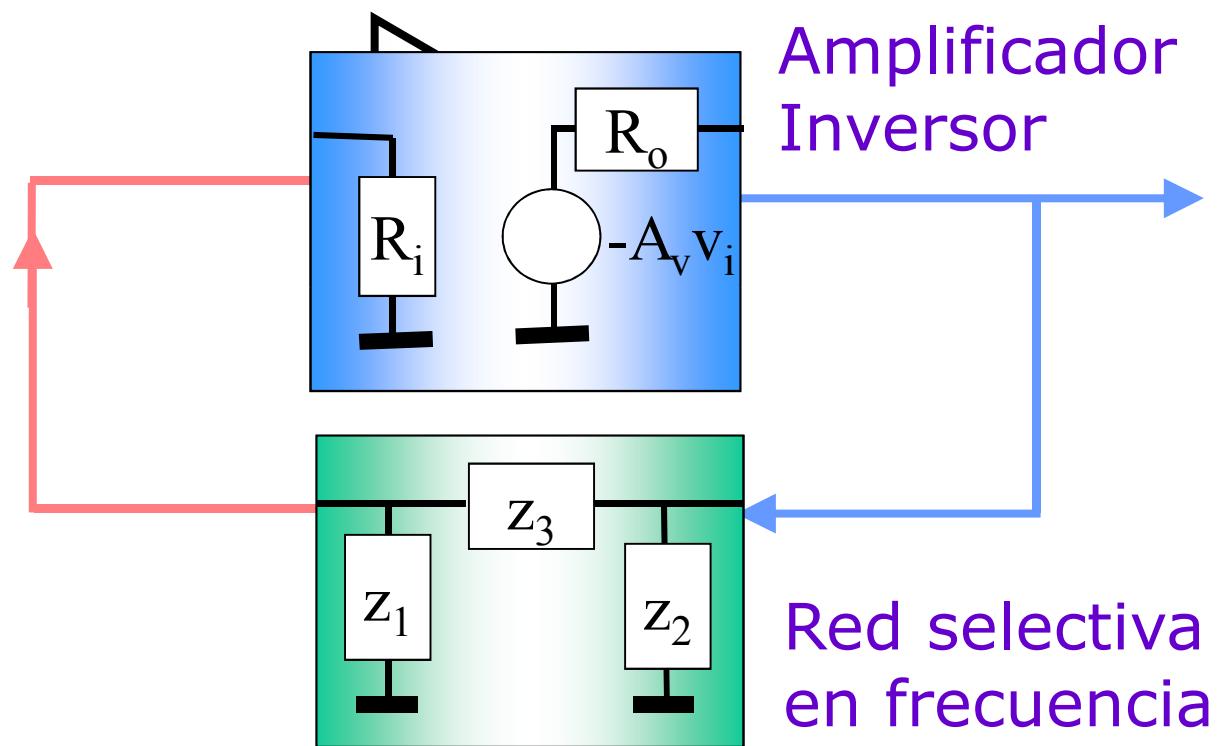
## **Oscilador RC por desplazamiento de fase**



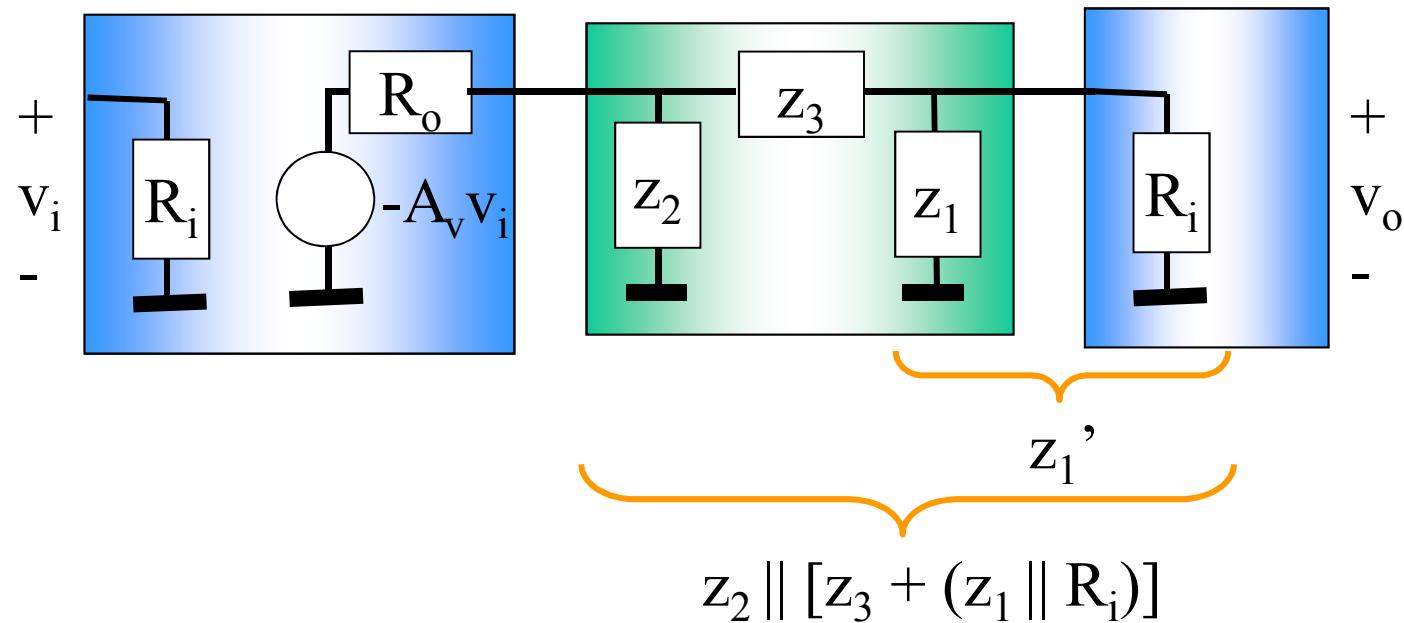
# **ANÁLISIS DE UN OSCILADOR**

## **Oscilador LC**

# Topología



## Análisis del Oscilador



$$A\beta = V_o/V_i = -A_v \frac{z_2 \cdot (z_1 \parallel R_i)}{R_o [(z_1 \parallel R_i) + z_2 + z_3] + z_2 [z_3 + (z_1 \parallel R_i)]}$$

## Condiciones de Oscilación

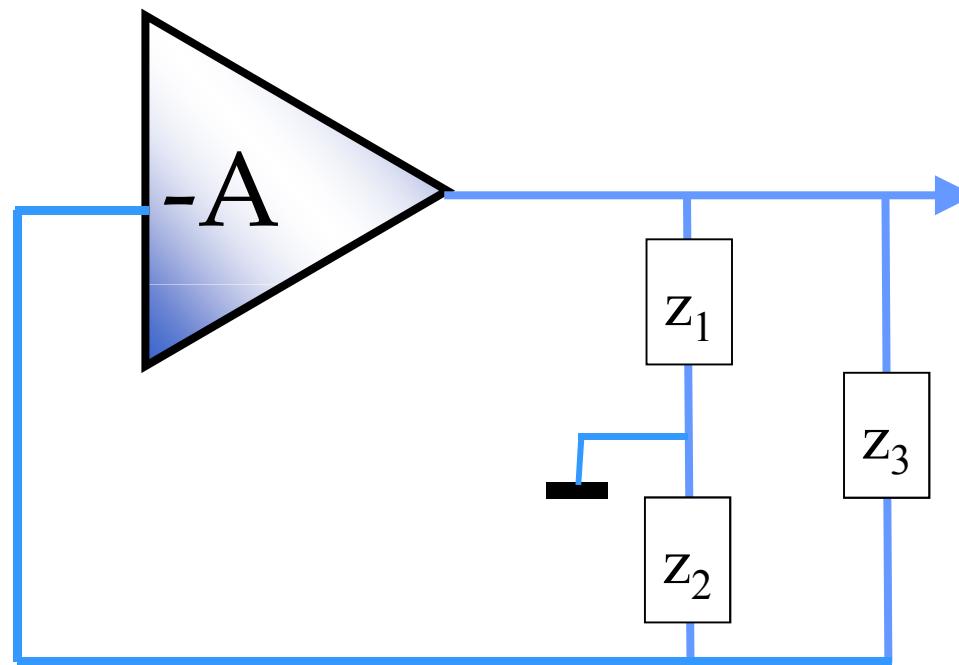
Una impedancia, z, proviene de un

Condensador                   $Z_C = 1/(j\omega C) = -j/(\omega C) = j [-1/(\omega C)] = jX_C$

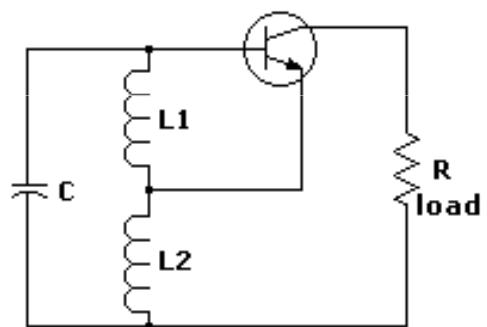
Bobina                   $Z_L = j\omega L = j [\omega L] = jX_L$

$$A\beta = v_o/v_i = -A_v \frac{-X_2 \cdot X_1}{j R_o [ X_1 + X_2 + X_3 ] - X_2 [ X_3 + X_1 ]}$$

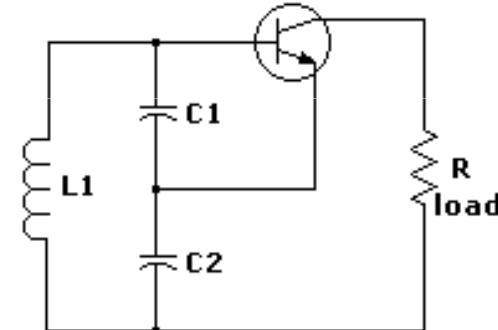
## Topología Plegada



Hartley



Colpitts



Atención!

Red de polarización del TRT  
NO representada, pero necesaria.

# **ANÁLISIS DE UN OSCILADOR**

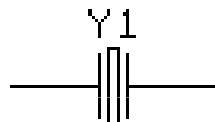
## **Oscilador de Cristal de Cuarzo**



Componente basado en efecto piezoeléctrico:

Ante una presión, el cristal genera una tensión en bornas de los conectores.

Ante una tensión aplicada, genera fuerzas mecánicas que alteran la forma del cristal. **Cuando la tensión aplicada varía con el tiempo, el cristal vibra**, y la amplitud de la vibración es máxima cuando la frecuencia de la señal aplicada tiene un determinado valor (**resonancia**)

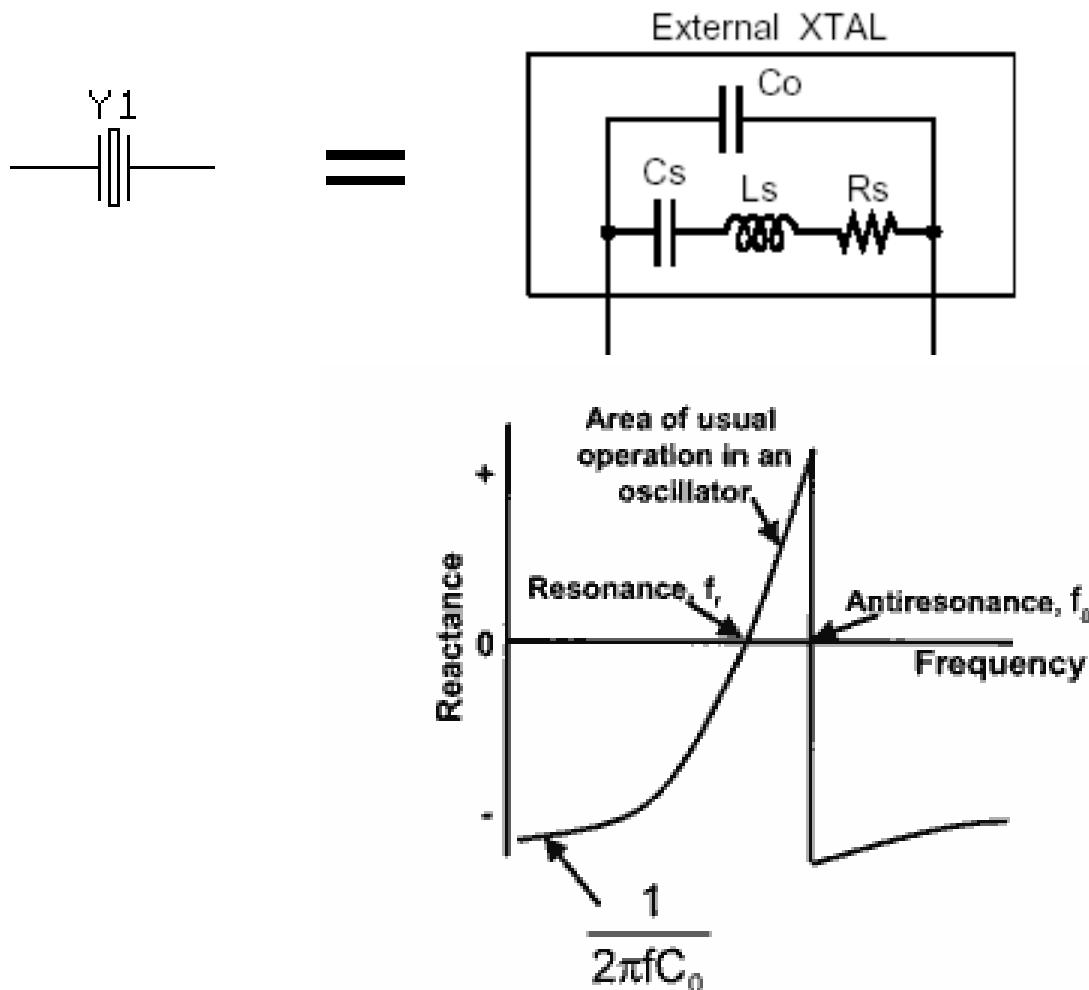


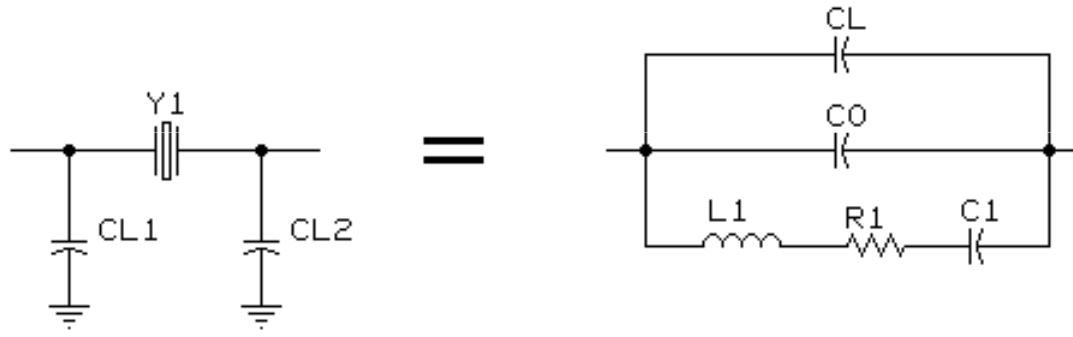
Los cristales permiten fijar una frecuencia de oscilación.

Esta frecuencia se especifica en partes por millón. Por ejemplo, un cristal de 32,768 Hz con tolerancia de  $\pm 20$  ppm a 25°C, la frecuencia de resonancia puede encontrarse entre:

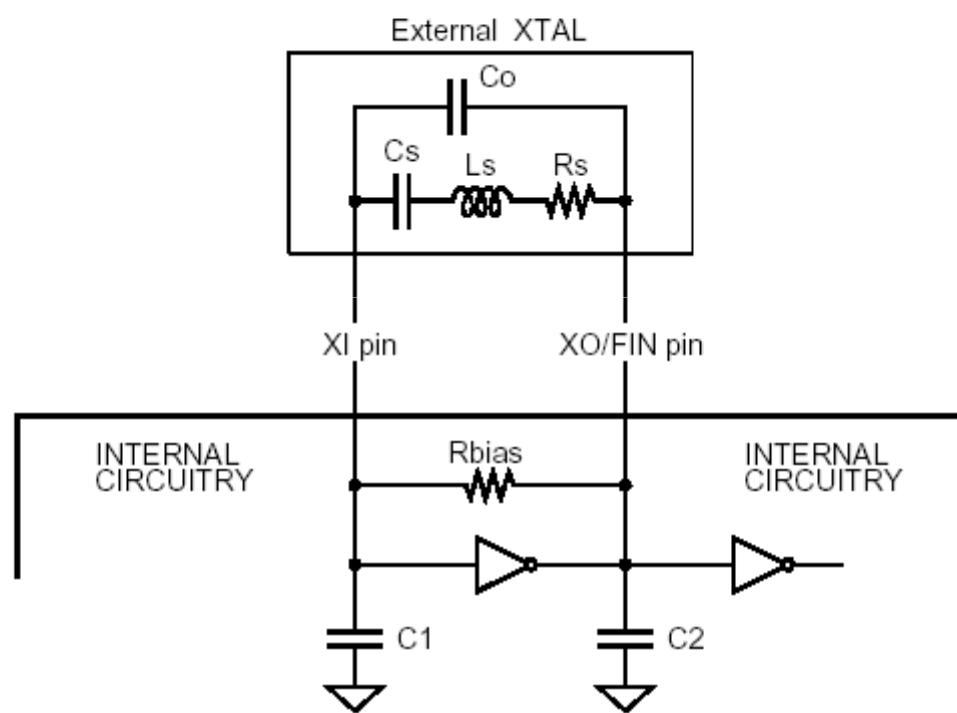
$$32.768 + 32.768 * (20/1000000) = 32.76865536 \text{ Hz}$$

$$32.768 - 32.768 * (20/1000000) = 32.76734464 \text{ Hz}$$





$$F_p = F_s \sqrt{1 + \frac{C_1}{C_O + CL}}$$



## Nota histórica



- 1911 - 1912      **Fritz Lowenstein**,  
Laboratorios en Nassau St. (N.Y.)  
Primer uso del audión de De Forest como amplificador  
Primer oscilador operativo.
- 1912      **Van Etten**  
Descubre el hecho de que al realimentar un audión se  
producen oscilaciones (**HOWLING, SINGING**)
- 1912-1913      **E.H. Armstrong (USA), A. Meissner (DE)**  
Uso de la realimentación positiva → Detector regenerativo.

## El fenómeno de 'regeneración'

### AMPLIFICADOR CON REALIMENTACIÓN POSITIVA

Cuando se **realimentaba suficiente señal**, el amplificador operaba como un oscilador estable, perfecto para los transmisores de radio.

**Reduciendo el nivel de señal**, el amplificador operaba como un receptor de señal con una sensibilidad que superaba a todos los dispositivos de la época.

