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Carlos III de Madrid  
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# Session 12

## Analysis of DC circuits with BJT (polarization)

Electronic Components and Circuits  
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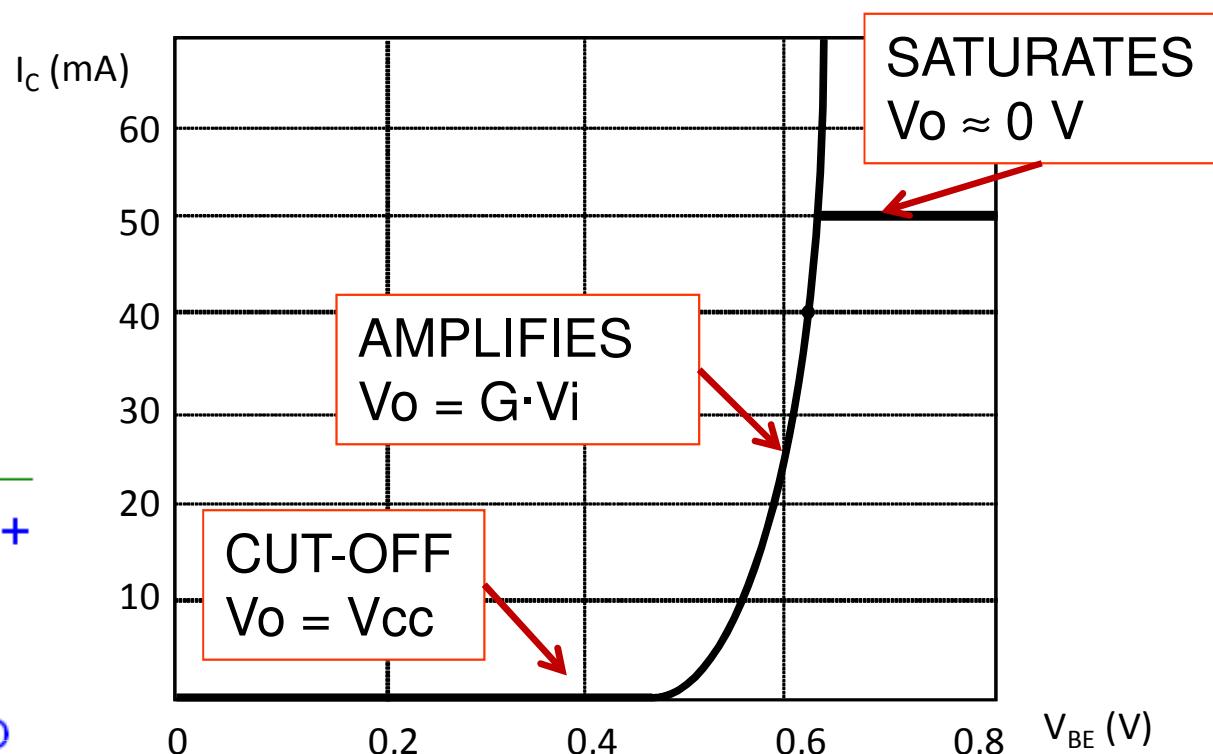
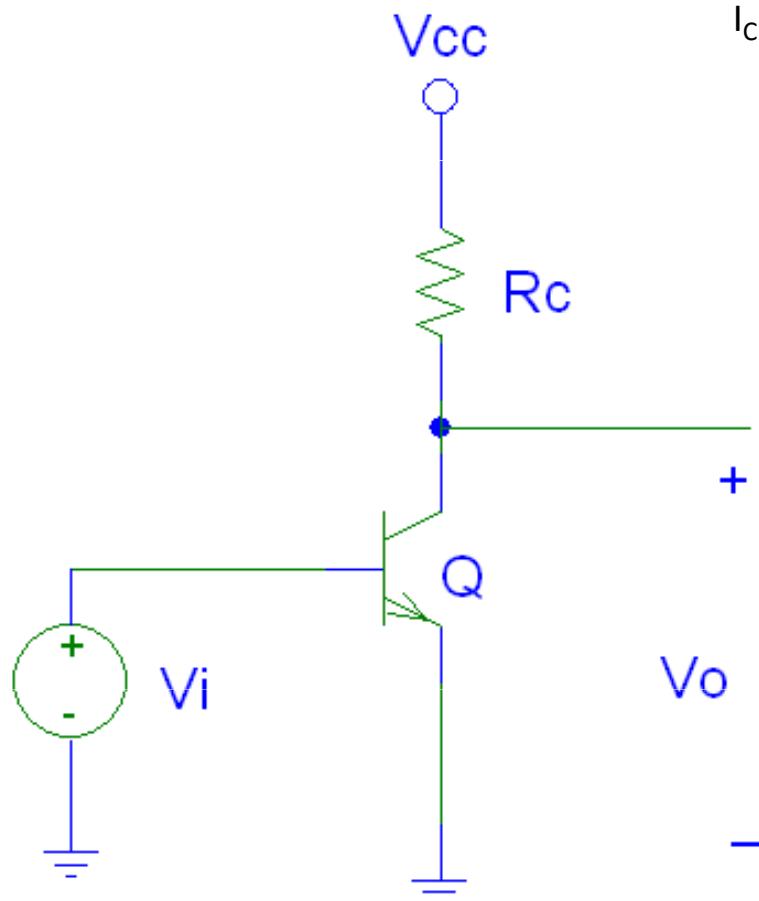
[www.uc3m.es/portal/page/portal/dpto\\_tecnologia\\_electronica/Personal/JoseAntonioGarcia](http://www.uc3m.es/portal/page/portal/dpto_tecnologia_electronica/Personal/JoseAntonioGarcia)

# DC circuits with BJT and polarization of transistors

## OBJETIVES

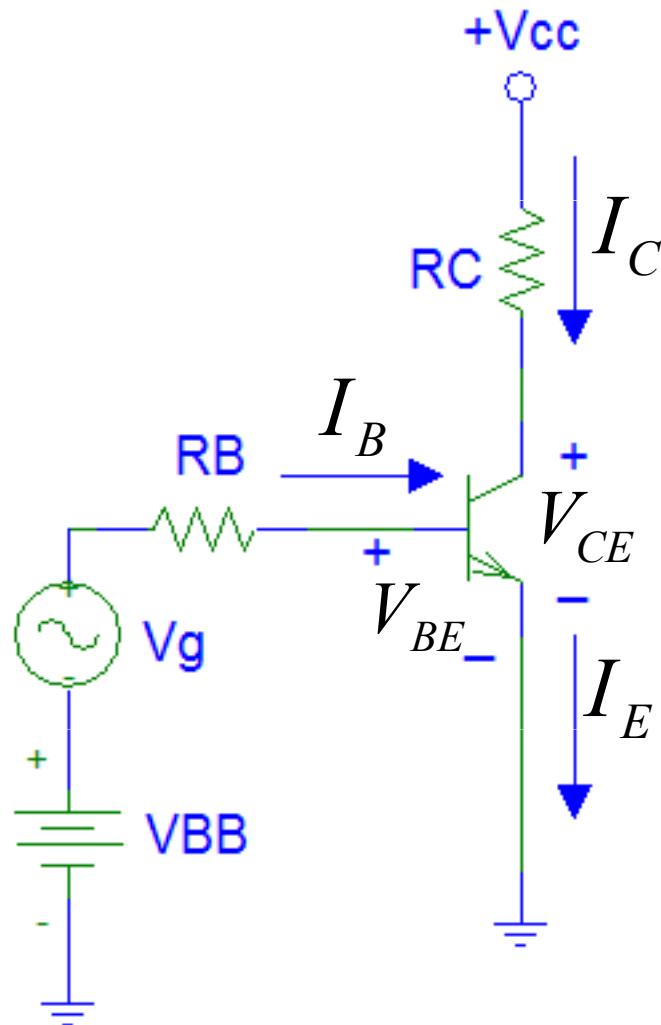
- Summarizing the operating regions and introducing the amplification (active)  
Active, Cut-off, Saturation
- Analyzing basic BJT circuits in DC. Static characteristics and Load line.
- Understanding the need of polarization circuits
- Knowing and analyzing typical polarization circuits of transistors. Bias (quiescent) point.

# Amplification concept with BJT

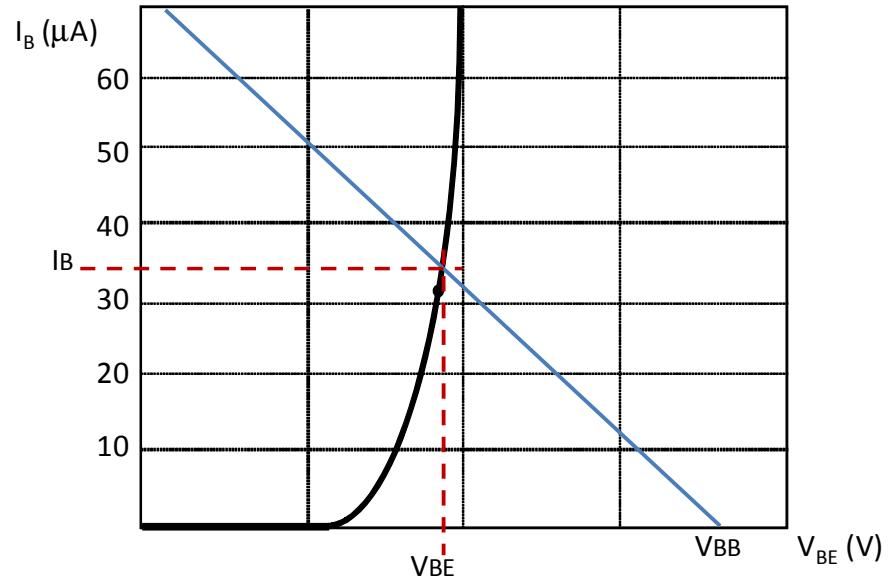


- Small changes of  $V_i$  result in greater variation of  $V_o$ , thus providing gain  $V_o/V_i$
- It should be around a bias point or quiescent point  $V_{BE-Q}$ ,  $V_{CE-Q}$

# Superposition of DC Bias and Signal



- $V_{BB}$  is a continuous source that provides along with  $R_B$  a bias point (polarization) :  $v_g = 0$



- A variable signal is introduced and it is added to  $V_{BB}$     $V_{BB} + v_g$

# Amplification focuses on Active region

- Datasheet  $V_{BE(on)}$   $V_{CE(sat)}$   $h_{FE}$   $V_{BE(sat)}$   
Search BC547 in <http://www.fairchildsemi.com/>

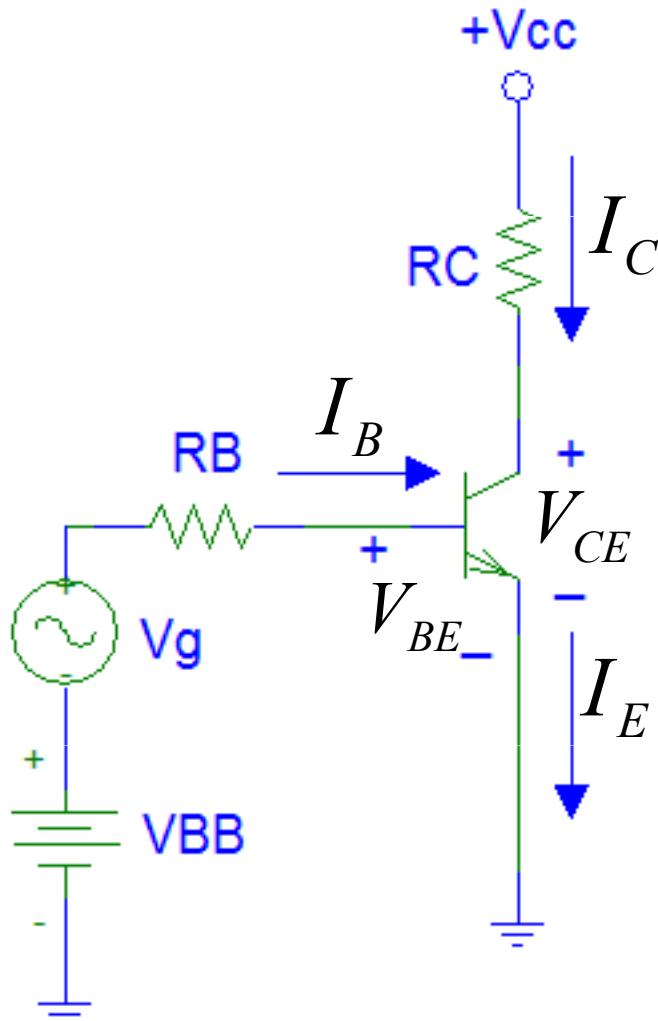
Region	Base-Emitter Junction	Base-Collector Junction
Cut-off	Reverse(OFF)	Reverse
<b>Active</b>	<b>Forward (ON)</b>	<b>Reverse (Transistor Effect)</b>
Saturation	Forward (ON)	Forward (Saturated)

Region	Conditions NPN	Operation NPN	
Cut-off	$V_{BE} < V_{BE-ON}$ o $I_B = 0$	$I_B=0$ , $I_C=I_E=0$	
<b>Active</b>	<b><math>V_{BE-ON} \leq V_{BE} \leq V_{CE-SAT}</math></b>	$I_C \approx h_{FE} \cdot I_B$	<b><math>[V_{BE}=V_{BE-ON}]</math></b>
Saturation	$V_{BE-ON} \leq V_{BE} \leq V_{CE-SAT}$	$V_{CE} = V_{CE-SAT}$	<b><math>[V_{BE}=V_{BE-SAT}]</math></b>

# Graphical DC Analysis

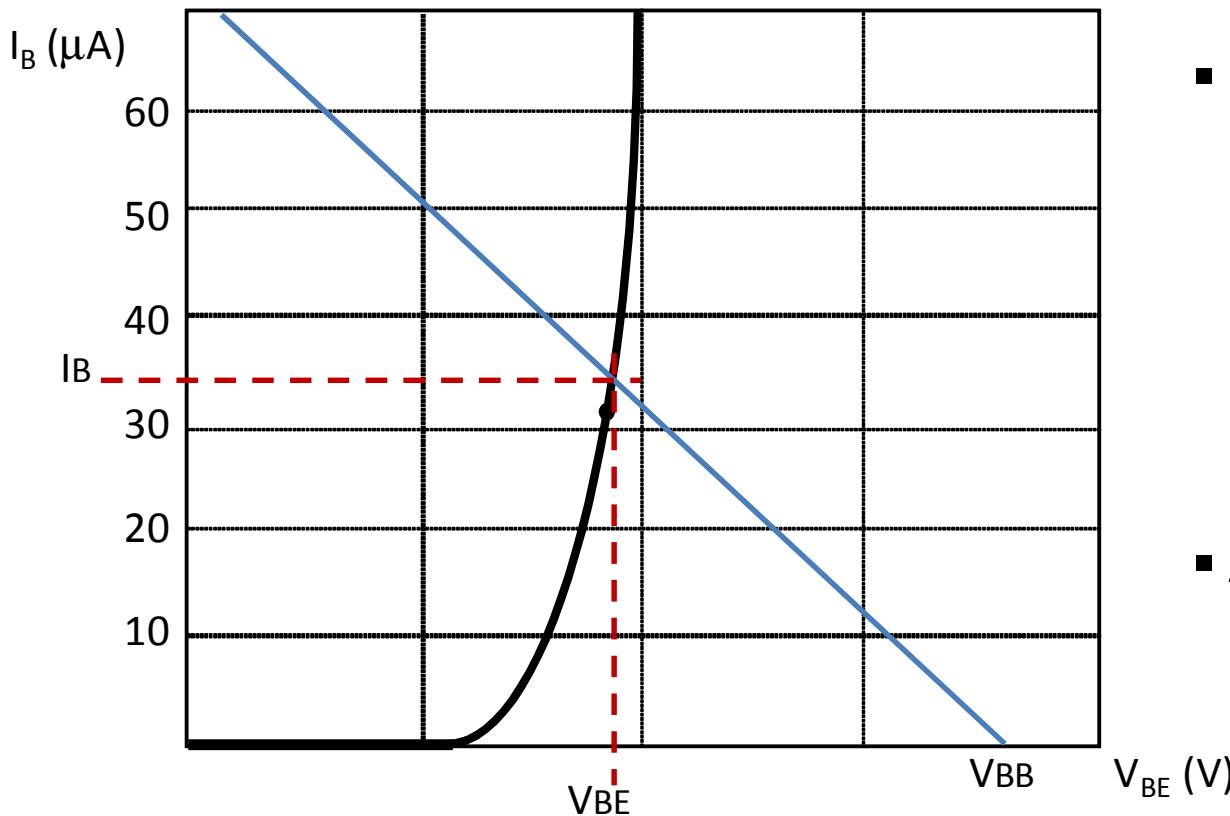
## EXAMPLE

- $RC = 100 \Omega$
- $RB = 10 \text{ k}\Omega$
- $V_{CC} = 10 \text{ V}$
- $V_{BB} = 10 \text{ V}$
- $V_{BE(\text{on})} = 0,7 \text{ V}$
- $V_{CE(\text{sat})} = 0,2 \text{ V}$
- $hFE = 100$



- Cancel the signal (superposition)  
 $v_g = 0$
- Analyze the input
  - Device Equation  
(Input Characteristic)
  - Circuit Equation  
(Load line)
- Analyze the output
  - Device Equation  
(Output Characteristic)
  - Circuit Equation  
(Load line)

# Input Characteristic and Load Line (I)



$$V_{BE} \approx V_{BE(on)} \quad I_B = \frac{V_{BB} - V_{BE(on)}}{R_B}$$

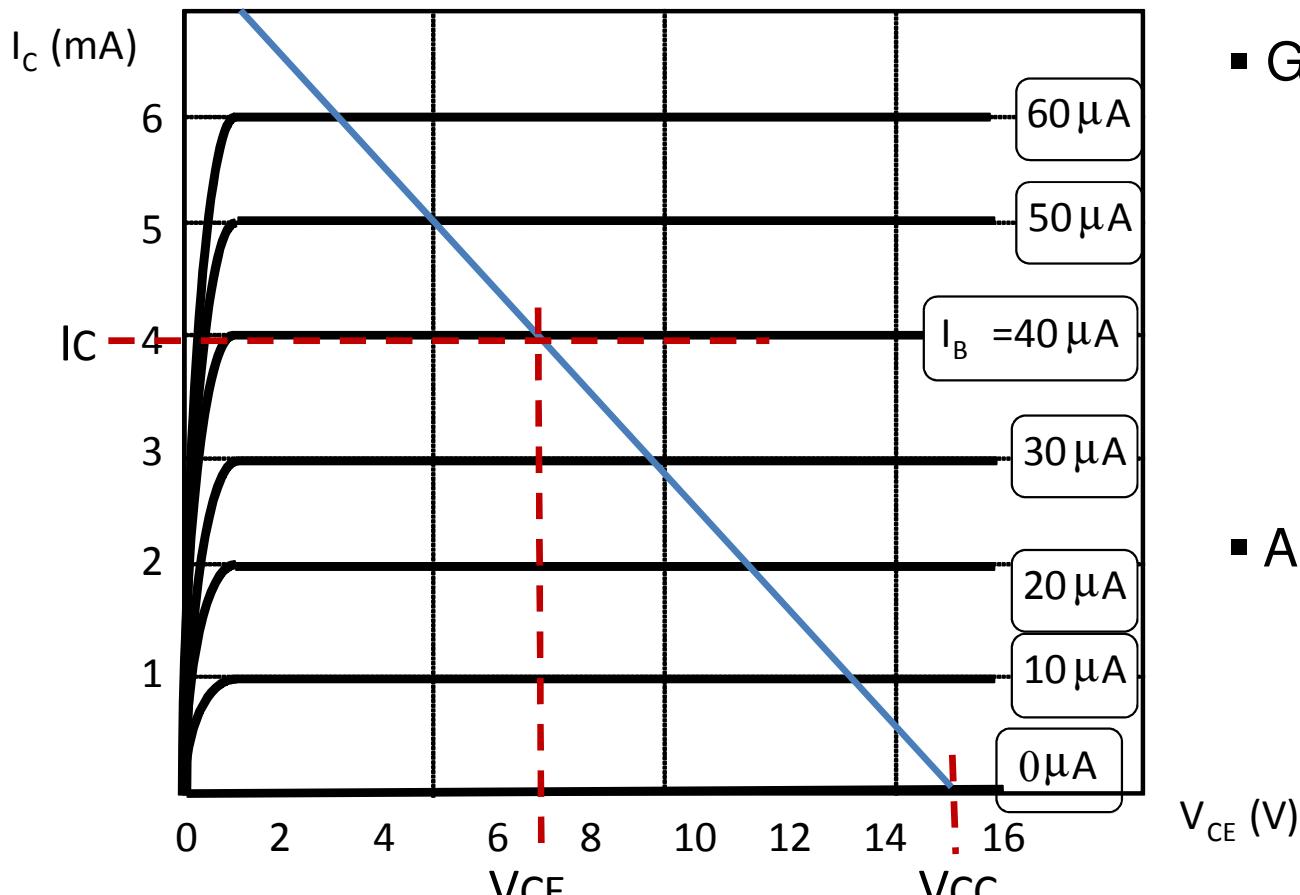
- Graphically
  - Characteristic:  $i_B = i_B(v_{BE}, v_{CE})$
  - Load line:

$$i_B = \frac{V_{BB} - v_{BE}}{R_B}$$

- Analytically
  - $V_{BB} > V_{BE(\text{on})}$
  - $v_{BE} = V_{BE(\text{on})}$

$$V_{BB} = v_{BE} + i_B \cdot R_B$$

# Output Characteristic and Load Line (II)



- Graphically
  - Characteristic:  $i_C = i_C(v_{CE}, i_B)$
  - Load line :  $i_C = \frac{V_{CC} - v_{CE}}{R_C}$
- Analytically
  - $V_{CE} > V_{CE(\text{sat})}$
  - $i_C = h_{FE} \cdot i_B$
  - $V_{CC} = v_{CE} + i_C \cdot R_C$

$$I_C = h_{FE} \cdot I_B$$

$$V_{CE} = V_{CC} - I_C \cdot R_C$$

# DC equivalent circuit: Analytically

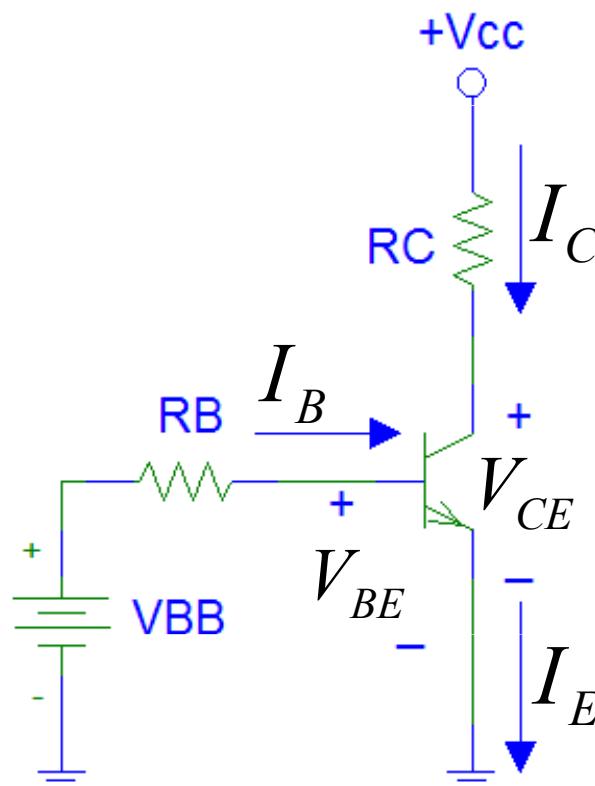
## EXAMPLE

- $RC = 100 \Omega$
- $RB = \dots$
- $VCC = 10 \text{ V}$
- $VBB = \dots$
- $VBE(\text{on}) = 0,7 \text{ V}$
- $VCE(\text{sat}) = 0,2 \text{ V}$
- $hFE = 100$

### Case 3

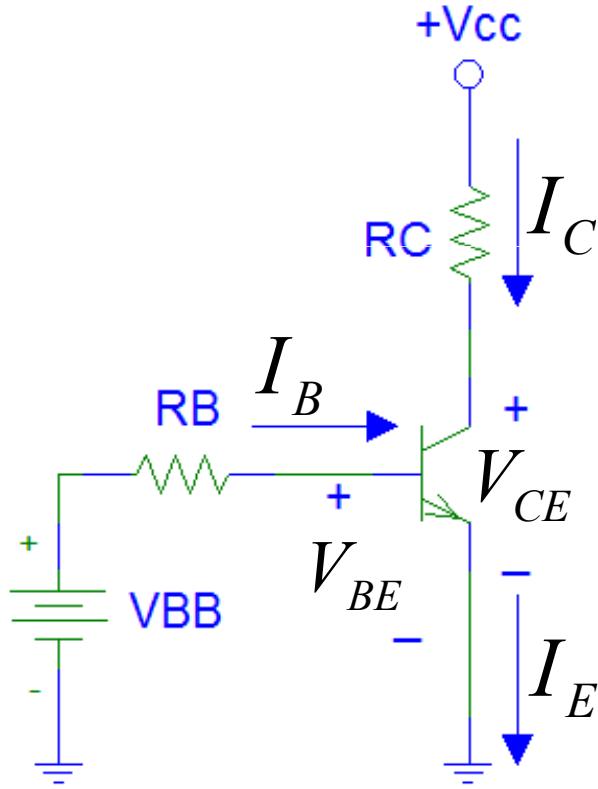
$VBB = 10 \text{ V}$

$RB = 10 \text{ k}\Omega$



- Analyze the input
  - Device Equation
  - Circuit Equation
- Analyze the output
  - Device Equation
  - Circuit Equation

# Solution: DC Analysis



- Analyze the input

- $V_{BB} > V_{BE(on)}$

- Device Equation

$$v_{BE} = V_{BE(on)}$$

- Circuit Equation

$$V_{BB} = v_{BE} + i_B \cdot R_B$$

- Analyze the output

- $V_{CE} > V_{CE(sat)}$

- Device Equation

$$i_C = h_{FE} \cdot i_B$$

- Circuit Equation

$$V_{CC} = v_{CE} + i_C \cdot R_C$$

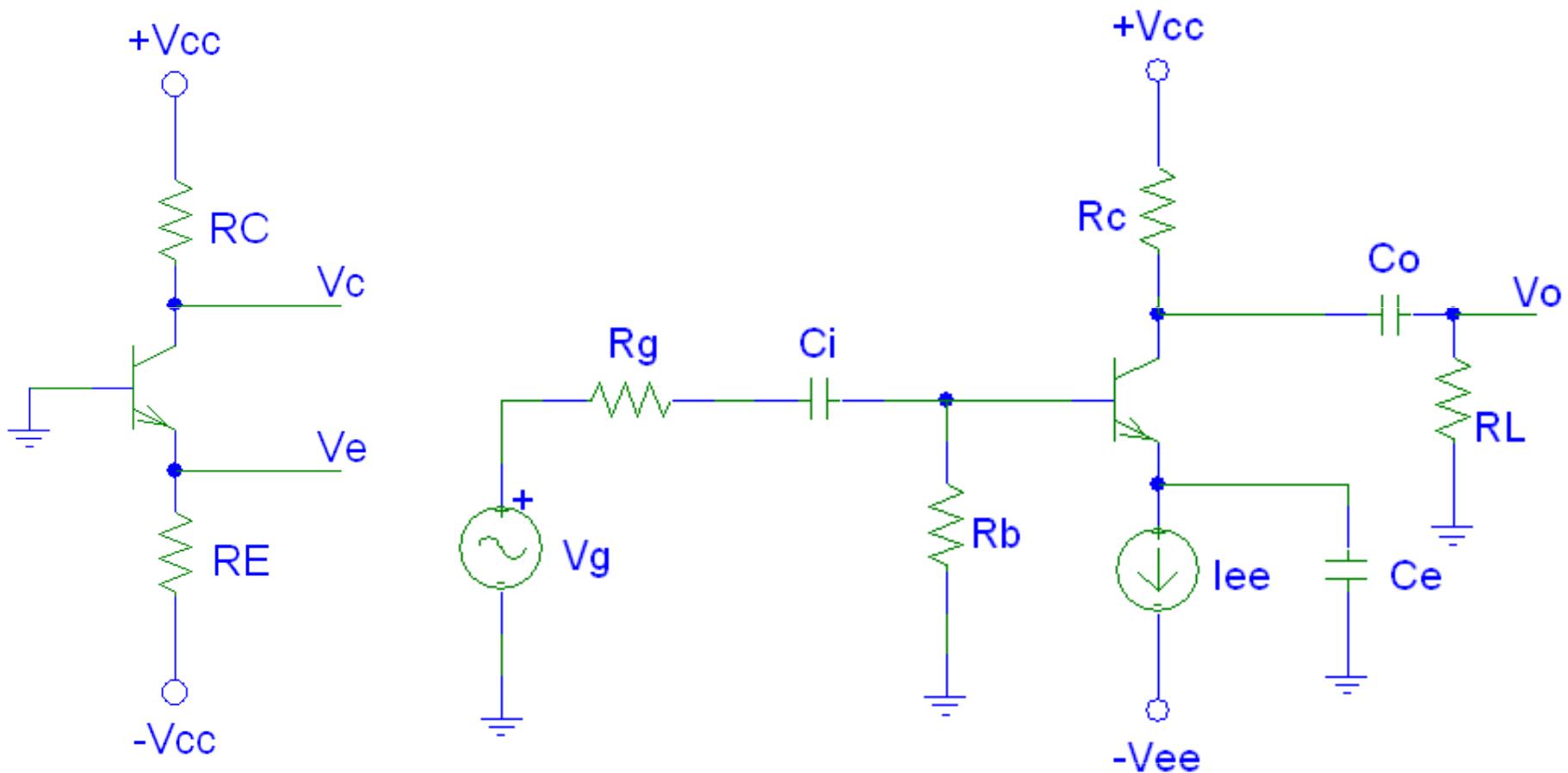
$$V_{BE} \approx V_{BE(on)}$$

$$I_B = \frac{V_{BB} - V_{BE(on)}}{R_B}$$

$$I_C = h_{FE} \cdot I_B$$

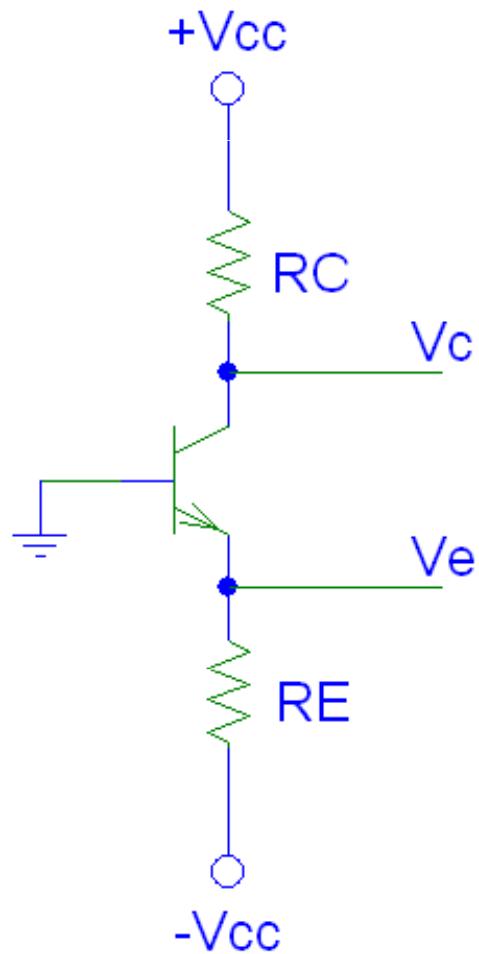
$$V_{CE} = V_{CC} - I_C \cdot R_C$$

# Bias circuits



- Set a stable operating point desensitized against the transistor parameters.
- Optimize the signal amplifier circuit.
- Separate bias circuit if necessary (signal AC coupling).

# Example



- Reasoning operating region
- Calculate the voltage  $V_E$
- Calculate the current  $I_E$
- Derive the relationship between  $I_E$ ,  $I_B$  and  $I_C$
- Calculate the currents  $I_C$  and  $I_B$
- Calculate the voltage  $V_C$

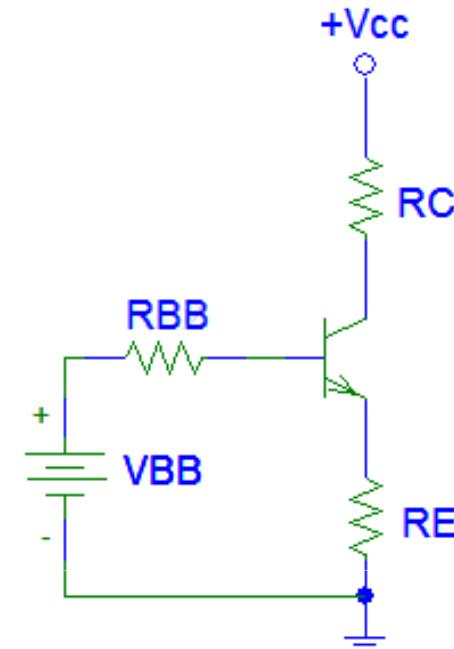
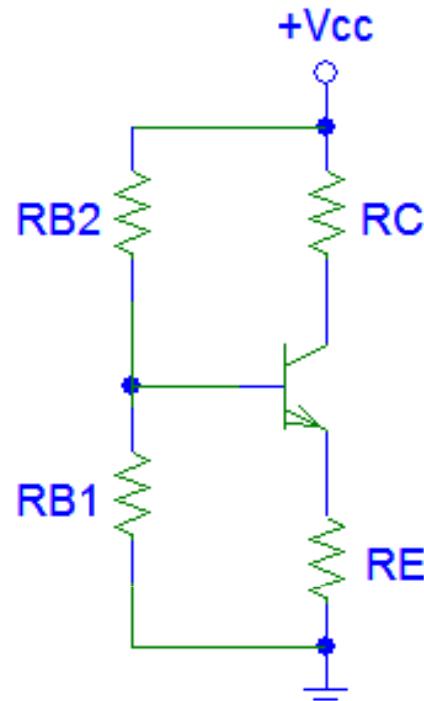
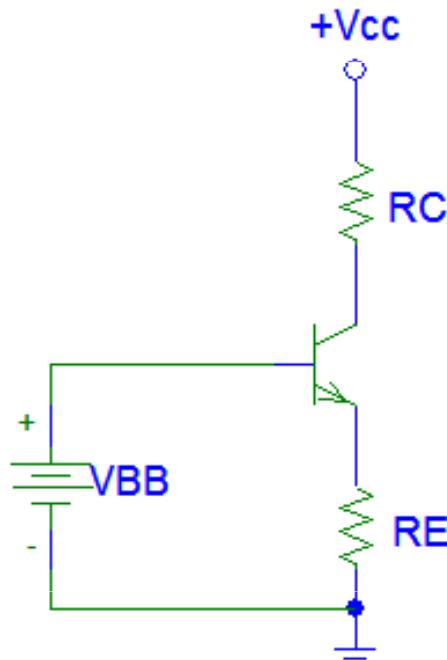
## DATA

- $V_{CC} = 12 \text{ V}$
- $R_C = R_E = 10 \text{ k}\Omega$
- $V_{BE(on)} = 0,7 \text{ V}$
- $V_{CE(sat)} = 0,2 \text{ V}$
- $h_{FE} = 100$

# Types of polarization circuits

## Biasing with RE

Practical circuit



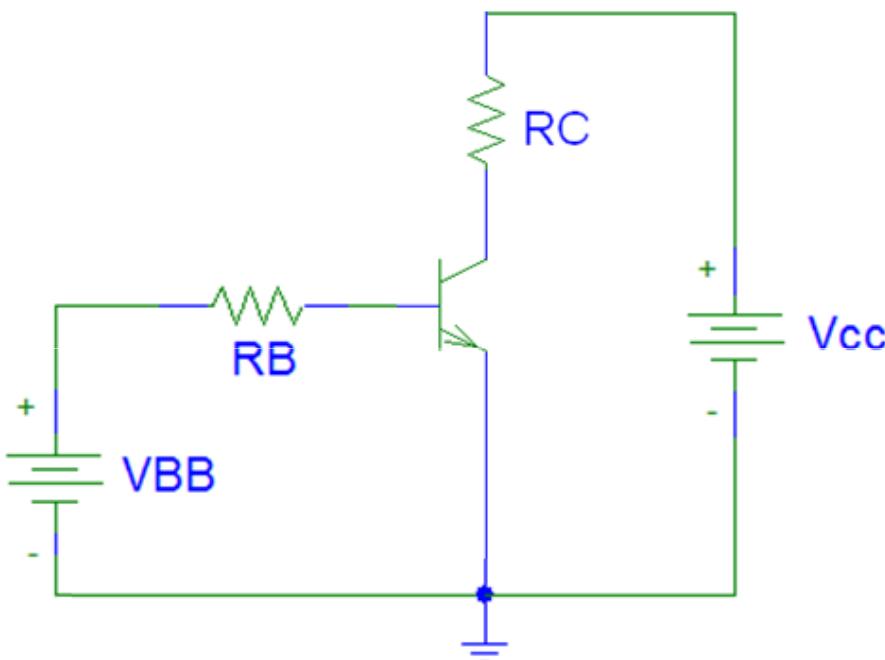
- Lower sensitivity to the transistor current gain
- Stabilizes the bias point (quiescent point) against  $V_{BE}$ ,  $h_{FE}$ , etc.

# Case 1: Biasing with RB

DATA:

- $V_{BB} = 5 \text{ V}$
- $V_{CC} = 10 \text{ V}$
- $R_B = 50 \text{ k}\Omega$
- $R_C = 3 \text{ k}\Omega$
- $R_E = 2 \text{ k}\Omega$
- $V_{BE(\text{on})} = 0,7 \text{ V}$
- $V_{CE(\text{sat})} = 0,2 \text{ V}$
- $hFE = 100$

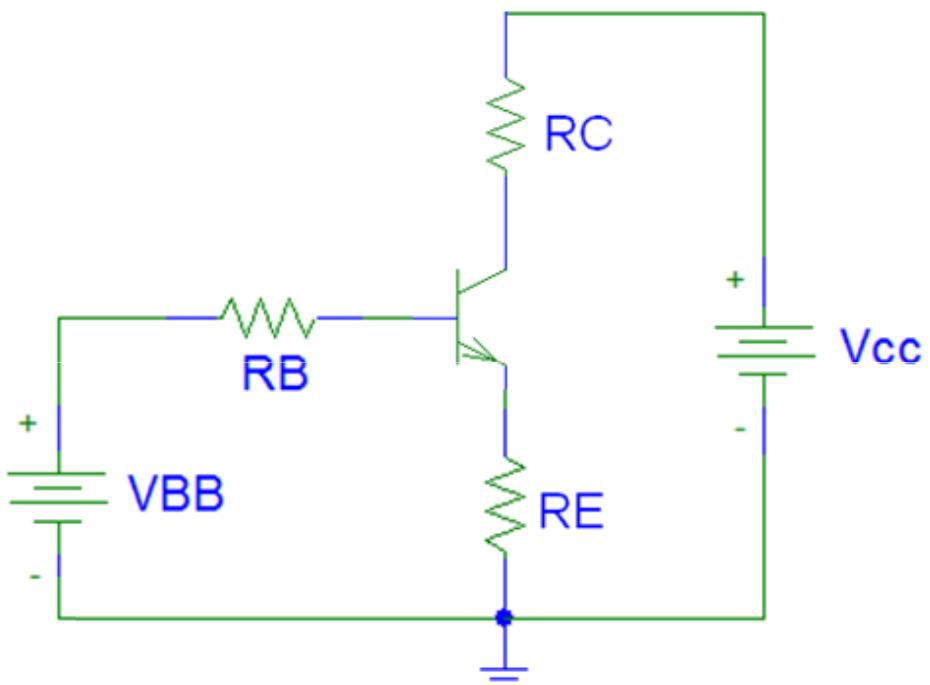
- Reasoning the operating region
- Indicate the value of  $V_{BE}$
- Calculate the currents  $I_B$ ,  $I_C$  e  $I_E$
- Calculate the voltage  $V_{CE}$
- Check that is in active
- Recalculate if you change  $hFE = 200$



# Case 2: Biasing with RE

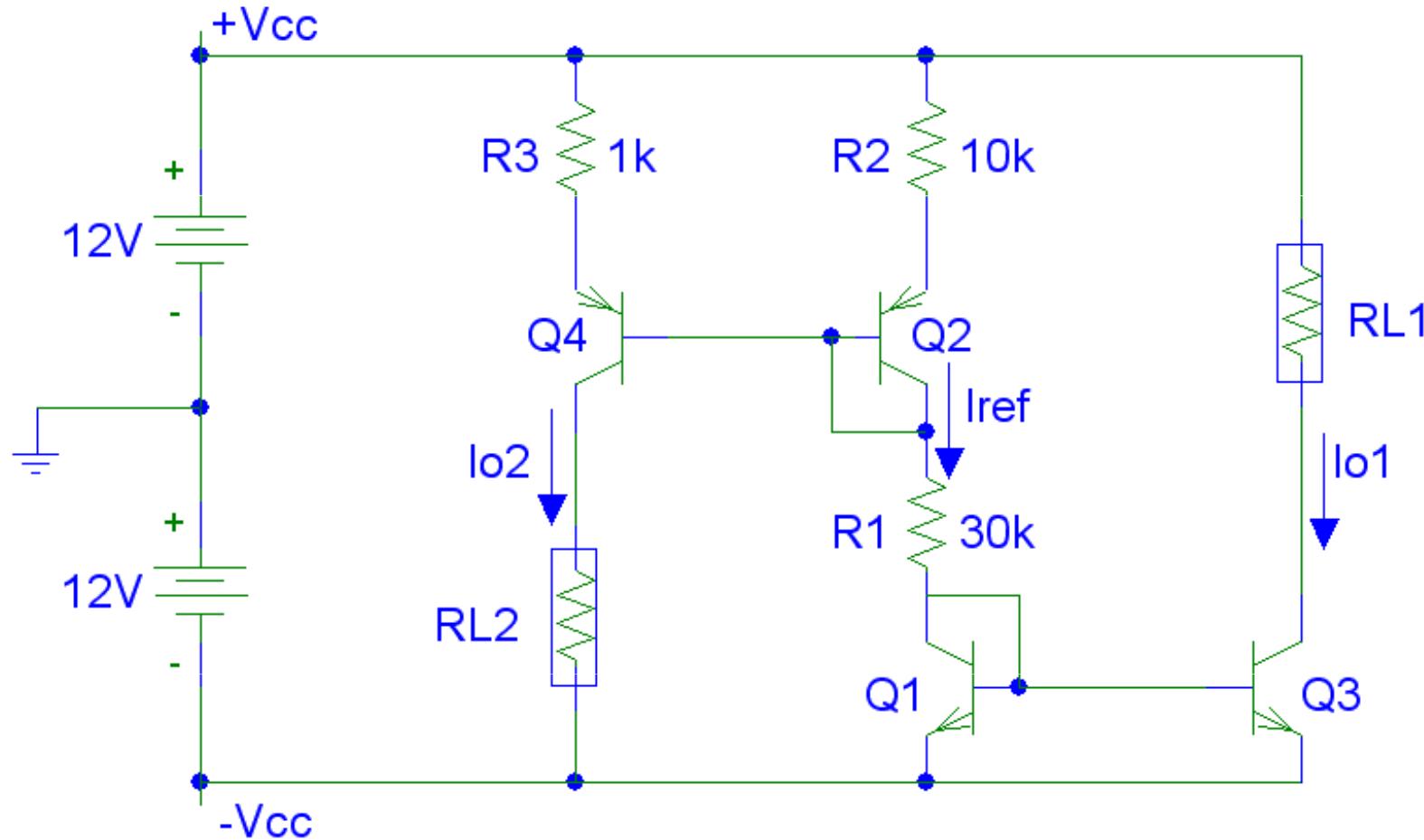
DATA:

- $V_{BB} = 5 \text{ V}$
- $V_{CC} = 10 \text{ V}$
- $R_B = 10 \text{ k}\Omega$
- $R_C = 3 \text{ k}\Omega$
- $R_E = 2 \text{ k}\Omega$
- $V_{BE(\text{on})} = 0,7 \text{ V}$
- $V_{CE(\text{sat})} = 0,2 \text{ V}$
- $hFE = 100$



- Reasoning the operating region
- Indicate the value of  $V_{BE}$
- Calculate the current  $I_E$  (you can neglect the base current  $I_B$ )
- Calculate the currents  $I_C$ ,  $I_B$
- Check that  $I_B$  is negligible
- Calculate the voltage  $V_{CE}$
- Check that the BJT is in active
- Recalculate if you change  $hFE = 200$
- Generalize if not negligible  $I_B$  (eg if  $R_B = 50 \text{ k}\Omega$ )

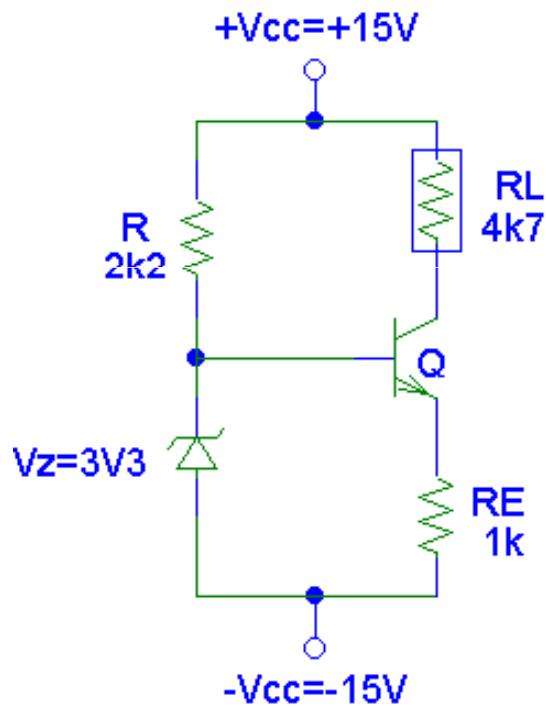
# Biasing with current mirrors



$$I_{O2} = I_{ref} \frac{R_2}{R_3} = 10 \cdot I_{ref}$$

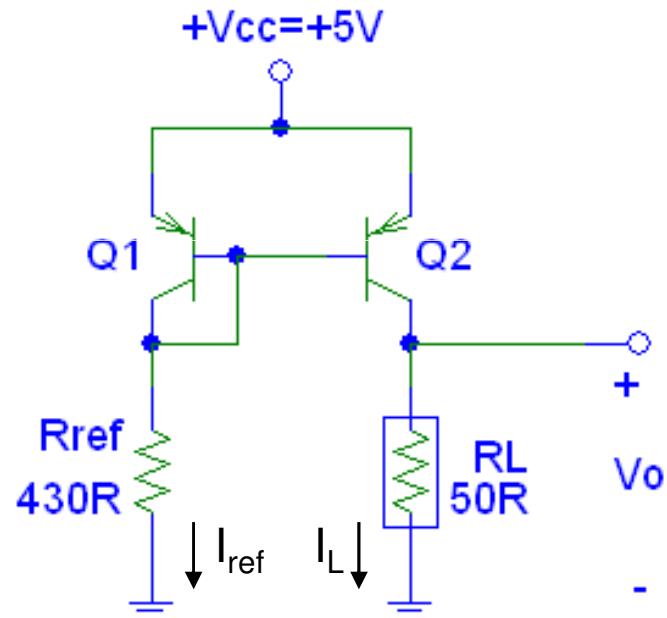
$$I_{O1} \approx I_{ref}$$

# Proposed exercise: Current sources



Zener ideal:  
 $V_Z = 3,3 \text{ V}$   
 $I_{Z\min} = 10 \text{ mA}$

Transistor:  
 $V_{CEsat} = 0,2 \text{ V}$   
 $V_{BEon} = 0,7 \text{ V}$   
 $\beta = 270$



- Calculate  $I_E$ ,  $I_C$ ,  $I_B$  and  $V_B$ ,  $V_C$ ,  $V_E$ ,  $V_{CE}$ ,  $I_Z$ .
- For  $R_L = 1 \text{ k}\Omega$ , calculate  $I_C$  y  $V_C$
- For  $R_L = 22 \text{ k}\Omega$ , calculate  $I_C$  y  $V_C$
- Plot the load lines (three cases).
- Maximum  $R_L$  as a current source?.
- In the case  $R_L = 22 \text{ k}\Omega$ , calculate  $I_B$ ,  $I_Z$

- Obtain the ratio  $I_L/I_{ref}$
- Reason if  $I_B$  is negligible
- Obtain  $I_{ref}$
- There is the scale factor  $I_{C2} = 2 \cdot I_{C1}$  between both transistor. Calculate  $V_o$ .