

It is required:

1. Define the G grammar that would generate valid sentences of this programming language.
2. Can the grammar G of the first exercise be used to perform an LL(1) analysis? If not, modify it so that it can. Generate the Table LL(1).
3. Construct the Table LR(1) that recognizes sentences of the language generated by the modified grammar of section 2, showing the states and the transitions between them.

Solution

A grammar that generates the given language can be defined as follows:

$$G = \{S, A, B, D, E, V, X\}, \{S\}, \{ ;, \text{type, var, do, endo, =, o, p, " ;" }\}$$

- (1) $S ::= A ; S$
- (2) $S ::= A ;$
- (3) $A ::= D$
- (4) $A ::= B$
- (5) $A ::= E$
- (6) $D ::= \text{type } V$
- (7) $V ::= \text{var}$
- (8) $V ::= \text{var } , V$
- (9) $B ::= \text{do } S \text{ endo } X$
- (10) $E ::= \text{var } = X$
- (11) $X ::= o$
- (12) $X ::= o p X$

The token "type" represents the strings "num" and "log", the token "var" to the set of characters that identifies a variable, "o" is an operand (variable or number) and "p" is an operator, either of arithmetic or logical type.

After left-factoring, the modified G' is:

$$G' = \{S, S', A, B, D, E, V, V', X, X'\}, \{S\}, \{ ;, \text{type, var, do, endo, =, o, p, " ;" }\}$$

- (1) $S ::= A ; S'$
- (2) $S' ::= S$
- (3) $S' ::= \lambda$
- (4) $A ::= D$
- (5) $A ::= B$
- (6) $A ::= E$
- (7) $D ::= \text{type } V$
- (8) $V ::= \text{var } V'$
- (9) $V' ::= , V$
- (10) $V' ::= \lambda$
- (11) $B ::= \text{do } S \text{ endo } X$
- (12) $E ::= \text{var } = X$
- (13) $X ::= o X'$
- (14) $X' ::= p X$
- (15) $X' ::= \lambda$

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Σ_N	First				Follow	
S	type	do	var		\$	endo
S'	type	do	var	λ	\$	endo
A	type	do	var			
B	do					
D	type					
E	var					
V	var					
V'	λ	,				
X	o					
X'	λ	p				

Table LL(1)		Σ_T									
		\$;	type	var	do	endo	=	o	P	,
Σ_N	S			1	1	1					
	S'	3		2	2	2	3				
	A			4	6	5					
	B					11					
	D			7							
	E					12					
	V					8					
	V'		10								9
	X								13		
	X'		15								14

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State 0	Action	Go To
S' ::= · S		[0,S]=1
S ::= · A ; S'		[0,A]=2
A ::= · D		[0,D]=3
A ::= · B		[0,B]=4
A ::= · E		[0,E]=5
D ::= · type V	[0,type]=D6	
B ::= · do S endo X	[0,do]=D7	
E ::= · var = X	[0,var]=D8	
State 1	Action	Go To
S' ::= S ·	[1,\$]=ACP	
State 2	Action	Go To
S ::= A · ; S'	[2,","]=D9	
State 3	Action	Go To
A ::= D ·	[3,","]=R4	
State 4	Action	Go To
A ::= B ·	[4,","]=R5	
State 5	Action	Go To
A ::= E ·	[5,","]=R6	
State 6	Action	Go To
D ::= type · V		[6,V]=10
V ::= · var V'	[6,var]=D11	
State 7	Action	Go To
B ::= do · S endo X		[7,S]=D12
S ::= · A ; S'		[7,A]=2
A ::= · D		[7,D]=3
A ::= · B		[7,B]=4
A ::= · E		[7,E]=5
D ::= · type V	[7,type]=D6	
B ::= · do S endo X	[7,do]=D7	
E ::= · var = X	[7,var]=D8	
State 8	Action	Go To
E ::= var · = X	[8,"="]=D13	
State 9	Action	Go To
S ::= A ; · S'		[9,S']=14
S' ::= · S		[9,S']=15
S' ::= λ	[9,\$]=R3	
	[9,endo]=R3	
S ::= · A ; S'		[9,A]=2
A ::= · D		[9,D]=3
A ::= · B		[9,B]=4
A ::= · E		[9,E]=5
D ::= · type V	[9,type]=D6	
B ::= · do S endo X	[9,do]=D7	
E ::= · var = X	[9,var]=D8	
State 10	Action	Go To
D ::= type V ·	[10,","]=R7	
State 11	Action	Go To
V ::= var · V'		[11,V']=16
V' ::= · , V	[11,","]=D17	
V' ::= λ	[11,","]=R10	
State 12	Action	Go To
B ::= do S · endo X	[12,endo]=D1	

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tate 13	Action	Go To