## uc3m

## UNIT 5: TOP-DOWN PARSING TECHNIQUES

Build a compiler for the following programming language. There are three types of statements: declaration, arithmetic / logical expression and loop and two types of data: numeric and logical. The sentences are described as follows:

- Declaration
- type name_variable [, name_variable]* ;
- where type can be num or log and name_variable is a char string with a máximum number of 8 characters
- Arithmetic/Logic expressions
- name_variable = expression_arithmetic ;
- name_variable $=$ expression_logic;
- Arithmetic expressions can contain variables of type num and numbers with the operators: $+,-, *, /$
- The logical expression relates variables of type num with numbers through logical operators: <,>, =, \#. The possible results of the evaluation of the logical expression is V or F . The variable to which it is assigned must be type log.
- Loop
- do [sentence]+ endo [expression_logic | variable_logic] ;
- where sentences can be declaration, expression or loop.

The sentences of the loop are executed at least once, and the loop is repeated while the logical expression in endo takes the value V . The variables are local to the loop where they are declared, if variables are used in the logical expression of the endo then there must be been declared inside the loop. The variables declared in the main body of the program are considered local to it.

Example of a program without errors:


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It is required:

1. Define the G grammar that would generate valid sentences of this programming language
2. Can the grammar $G$ of the first exercise be used to perform an LL(1) analysis? If not, modify it so that it can. Generate the Table LL(1).
3. Represent the derivation tree obtained when performing the LL (1) analysis with the Table of section 2, for the following sentence:
```
num i;
i = i * 5;
do
    num k, m;
    log b;
    k = m *2 + k;
    b = k < 10;
endo b;
```


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## Solution

A grammar that generates the given language can be defined as follows:
$\mathbf{G}=\{\mathbf{S}, \mathbf{A}, \mathbf{B}, \mathbf{D}, \mathbf{E}, \mathbf{V}, \mathbf{X}\},\{\mathbf{S}\},\{;$, type, var, do, endo, $=, \mathrm{o}, \mathrm{p}, ", "\}$
(1) $\mathbf{S}::=\mathbf{A} ; \mathbf{S}$
(2) $\mathbf{S}::=\mathbf{A}$;
(3) $\mathbf{A}::=\mathbf{D}$
(4) $\mathbf{A}::=\mathbf{B}$
(5) $\mathbf{A}::=\mathbf{E}$
(6) $\mathbf{D}::=$ type $\mathbf{V}$
(7) $\mathrm{V}::=\mathrm{var}$
(8) $\mathbf{V}::=$ var, $\mathbf{V}$
(9) $\mathbf{B}::=$ do $\mathbf{S}$ endo $\mathbf{X}$
(10) $\mathbf{E}::=\mathrm{var}=\mathbf{X}$
(11) $\mathbf{X}::=0$
(12) $\mathbf{X}::=$ o p X

The token "type" represents the strings "num" and "log", the token "var" to the set of characters that identifies a variable, " o " is an operand (variable or number) and " p " is an operator, either of arithmetic or logical type.

After left-factoring, the modified $G^{\prime}$ is:
$G^{\prime}=\left\{\mathbf{S}, \mathbf{S}^{\prime}, \mathbf{A}, \mathbf{B}, \mathbf{D}, \mathbf{E}, \mathbf{V}, \mathbf{V}^{\prime}, \mathbf{X}, \mathbf{X}^{\prime}\right\},\{\mathbf{S}\},\{;$, type, var, do, endo, =, o, p, """\}
(1) $\mathbf{S}::=\mathbf{A} ; \mathbf{S}$,
(2) $\mathbf{S}^{\prime}::=\mathbf{S}$
(3) $\mathbf{S}^{\prime}::=\lambda$
(4) $\mathbf{A}::=\mathbf{D}$
(5) $\mathbf{A}::=\mathbf{B}$
(6) $\mathbf{A}::=\mathbf{E}$
(7) $\mathbf{D}::=$ type $\mathbf{V}$
(8) $\mathbf{V}::=\operatorname{var} \mathbf{V}$,
(9) $\mathbf{V}^{\prime}::=, \mathbf{V}$
(10) $\mathbf{V}^{\prime}::=\lambda$
(11) $\mathbf{B}::=\operatorname{do} \mathbf{S}$ endo $\mathbf{X}$
(12) $\mathbf{E}::=$ var $=\mathbf{X}$
(13) $\mathbf{X}::=$ o $\mathbf{X}$ '
(14) $X^{\prime}::=p \mathbf{X}$
(15) $X^{\prime}::=\lambda$

| $\Sigma_{\mathbf{N}}$ | First |  |  | Follow |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{S}$ | type | do | var |  | $\$$ | endo |
| $\mathbf{S}^{\prime}$ | type | do | var | $\lambda$ | $\$$ | endo |
| $\mathbf{A}$ | type | do | var |  | $;$ |  |
| $\mathbf{B}$ | do |  |  |  | $;$ |  |
| $\mathbf{D}$ | type |  |  |  | $;$ |  |
| $\mathbf{E}$ | var |  |  |  | $;$ |  |
| $\mathbf{V}$ | var |  |  |  | $;$ |  |
| $\mathbf{V}$ | $\lambda$ | , |  |  | $;$ |  |
| $\mathbf{X}$ | o |  |  |  | $;$ |  |
| $\mathbf{X}^{\prime}$ | $\lambda$ | p |  |  | $;$ |  |


| Table LL(1) |  | $\Sigma_{\text {T }}$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | \$ | ; | type | var | do | endo | $=$ | 0 | P | , |
| $\Sigma_{\text {N }}$ | S |  |  | 1 | 1 | 1 |  |  |  |  |  |
|  | $\mathbf{S}^{\prime}$ | 3 |  | 2 | 2 | 2 | 3 |  |  |  |  |
|  | A |  |  | 4 | 6 | 5 |  |  |  |  |  |
|  | B |  |  |  |  | 11 |  |  |  |  |  |
|  | D |  |  | 7 |  |  |  |  |  |  |  |
|  | E |  |  |  | 12 |  |  |  |  |  |  |
|  | V |  |  |  | 8 |  |  |  |  |  |  |
|  | V, |  | 10 |  |  |  |  |  |  |  | 9 |
|  | X |  |  |  |  |  |  |  | 13 |  |  |
|  | X |  | 15 |  |  |  |  |  |  | 14 |  |

## 3

```
num i;
i = i * 5;
do
    num k, m;
    log b;
    k = m *2 + k;
    b = k < 10;
endo b;
```

The lexical analysis will convert into a previous fragment in the following sequence of tokens (the indentation has been maintained to favor its reading):

```
type var;
var = o p o;
do
    type var, var;
    type var;
    var = o p o p o;
    var = o p o;
endo o;
```

The LL(1) analysis produces the next syntactic tree generated from the axiom to the leaves.

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