

EXERCISES

3.1. A plate 10 mm thick is subjected to bending moments M_x equal to 5 Nm/mm and M_y equal to 2 Nm/mm. Calculate the maximum normal stresses in the plate.

Ans. $\sigma_{\max} = 300$ MPa

3.2. A thin, elastic square plate of side a , and thickness h , is simply supported on all four sides and is subjected to a uniformly distributed load q_0 . The Young modulus, E , and the Poisson's ratio, ν , are known. Using the first three terms of the displacements series expansion, calculate the maximum deflection of the plate.

Ans. $w_{\max} = 0.04866 \cdot (1 - \nu^2) \cdot q_0 \cdot a^4 / (E \cdot t^3)$

3.3. Consider a circular plate of radius a , and thickness h , with clamped edge, and loaded by a distributed uniform compressive load p_0

Calculate:

1. The bending moments distributions
2. The maximum transversal displacement of the plate

Data

Plate radius, $a = 3.5$ m; plate thickness, $h = 0.12$ m; Young Modulus, $E = 210$ GPa, Poisson ratio, $\nu = 0.3$; distributed load, $p_0 = 0.1$ MPa

Ans. $w_{\max} = -7.06$ mm

3.4. Repeat the exercise 3.3 considering the plate has a simply supported edge.

Ans. $w_{\max} = -28.77$ mm

3.5. Consider a circular plate of radius a , and thickness h , simply supported on an annular interior ring of radius R , and loaded by a uniform load p_0 , as shown in the figure.

Calculate:

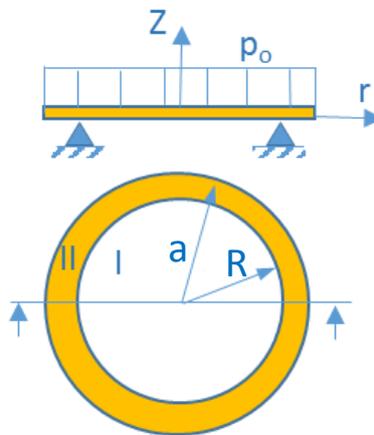
1. The bending moments distributions
2. The transversal displacement at the centre of the plate

Data

Plate radius, $a = 4.5 \text{ m}$; plate thickness, $h = 2 \text{ cm}$; supporting ring radius, $R = 3.5 \text{ m}$

Young Modulus, $E = 210000 \text{ MPa}$, Poisson ratio, $\nu = 0.3$.

Distributed load, $p_0 = 1000 \text{ N/m}^2$



Ans. $w(r = 0) = -19.7 \text{ mm}$

3.6. Consider a spherical tank of radius a , and the wall thickness h , supported by an annular ring as showed in the figure. The tank is filled with kerosene.

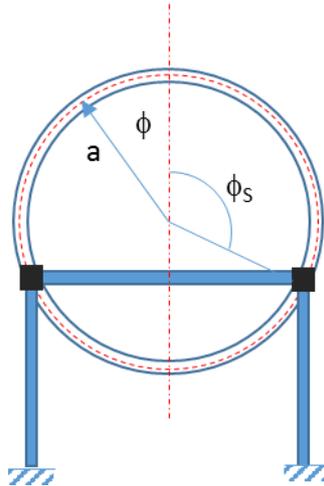
Calculate:

1. Internal forces in the shell at the section given by $\phi = \pi/3$,
2. The horizontal displacement, δ at the section given by $\phi = \pi/3$
3. The meridian rotation, γ at the supported section ($\phi = \phi_s$)

Data

$a = 20 \text{ m}$; $t = 10 \text{ mm}$; annular ring radius, $R = 16 \text{ m}$; Young Modulus, $E = 210 \text{ GPa}$;

Poisson ratio, $\nu = 0.3$; Density of kerosene: 800 kg/m^3



Ans.

$$N_{\phi}(\pi/3) = 280.4 \text{ kN/m}$$

$$N_{\theta}(\pi/3) = 981.3 \text{ kN/m}$$

$$\delta(\pi/3) = 7.9 \text{ mm}$$

$$\gamma(\phi_s) = -1.20 \cdot 10^{-3} \text{ rad}$$

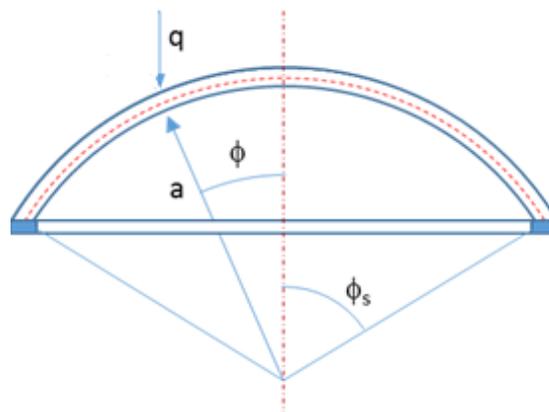
3.7. The roof of an airport terminal building can be modelled as a semi-spherical shell supported by an annular ring as showed in the figure. The total load on the roof shell is taken as $q = 3.5 \text{ kPa}$ constant over its surface area.

At the supported section, ($\phi = \phi_s$), calculate:

1. Internal forces in the shell
2. The horizontal displacement, δ
3. The meridian rotation, γ

Data

$a = 40 \text{ m}$; $t = 20 \text{ mm}$; $\phi_s = 60^\circ$; Young Modulus, $E = 27 \text{ GPa}$, Poisson ratio, $\nu = 0.20$



$$N_{\phi}(\pi/3) = -93.3 \text{ kN/m}$$

$$N_{\theta}(\pi/3) = 23.3 \text{ kN/m}$$

$$\delta(\pi/3) = 2.7 \text{ mm}$$

$$\gamma(\pi/3) = -4.94 \cdot 10^{-4} \text{ rad}$$