

Electrical Power Engineering Fundamentals

Departamento de Ingeniería Eléctrica. Universidad Carlos III de Madrid

Module 3. Analysis of AC Circuits. Week 6

Exercise 1. In the circuit below, find current $i(t)$ using Thevenin's Theorem:

$$U_{g1}(t) = 2\sqrt{2}\cos(2t) \text{ V}$$

$$I_{g2}(t) = 2\sin(2t + 45^\circ) \text{ A}$$

$$U_{g3}(t) = 3\sqrt{2}\sin(2t) \text{ V}$$

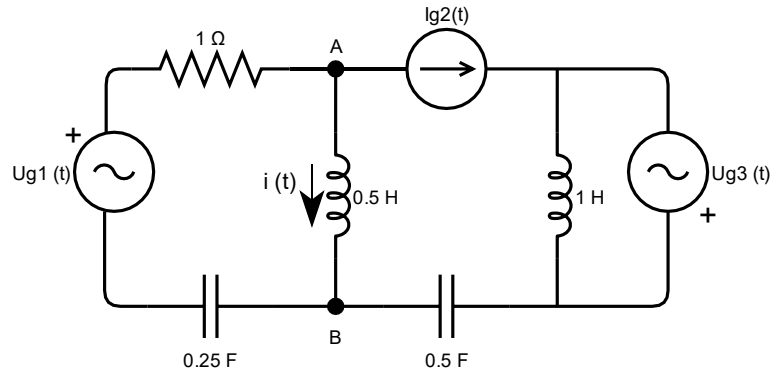


Figure 1 AC circuit 1

Solution: $i(t) = 3\sqrt{2}\sin(2t + 180^\circ) \text{ A}$; $U_{TH}(t) = 6\sin(2t + 135^\circ) \text{ V}$; $Z_{TH} = 1 - 2j \Omega$

Exercise 2. In the circuit below, find the power generated by sources and check the power balance:

$$U_g(t) = 5\sqrt{2}\sin(2t) \text{ V}$$

$$I_{g1}(t) = 20\sin(2t - 45^\circ) \text{ A}$$

$$I_{g2}(t) = 2\sqrt{2}\cos(2t) \text{ A}$$

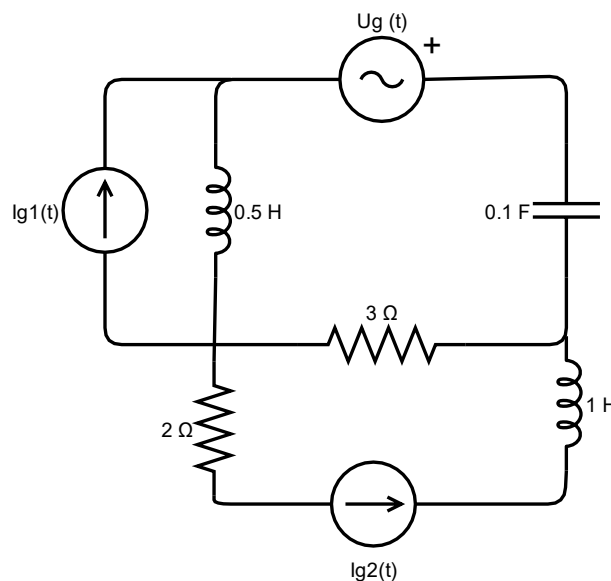


Figure 2 AC circuit 2

Solution: $S_{Ug} = 5.8 - 14.4j \text{ VA}$; $S_{I_{g1}} = 40.4 + 217.2j \text{ VA}$; $S_{I_{g2}} = 37.28 + 1.04j \text{ VA}$; $S_{consumed_by_loads} = S_{generated_by_sources} = 83.48 + 203.84j \text{ VA}$

Exercise 3. In the following circuit, find $i(t)$ and check the power balance:

$$U_{g1}(t) = 5\sqrt{2}\sin(0.5t) \text{ V}$$

$$U_{g2}(t) = 2\sqrt{2}\cos(0.5t) \text{ V}$$

$$U_{g3}(t) = \sqrt{2}\sin(0.5t - 90^\circ) \text{ V}$$

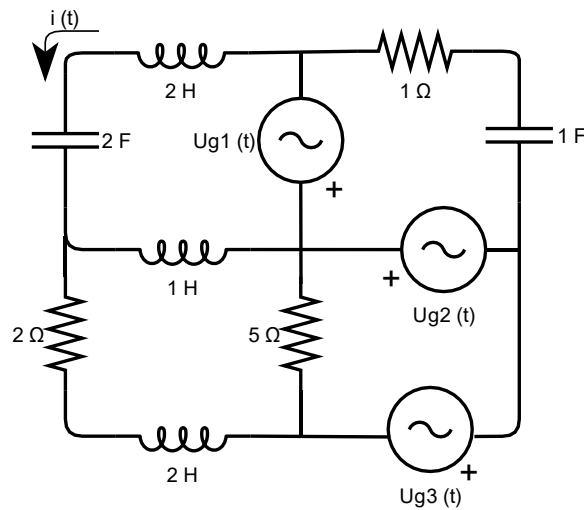


Figure 3. AC circuit 3

Solution: $i(t) = 16.32\cos(0.5t + 8.97^\circ) \text{ A}$; $S_{\text{consumed by loads}} = S_{\text{generated by sources}} = 16.4 + 43.6j \text{ VA}$

Exercise 4. Find the Thévenin equivalent between nodes A and B for the following circuit.

$$U_g(t) = \sqrt{2}\sin(2t + 180^\circ) \text{ V}$$

$$I_g(t) = \sqrt{2}\cos(2t) \text{ A}$$

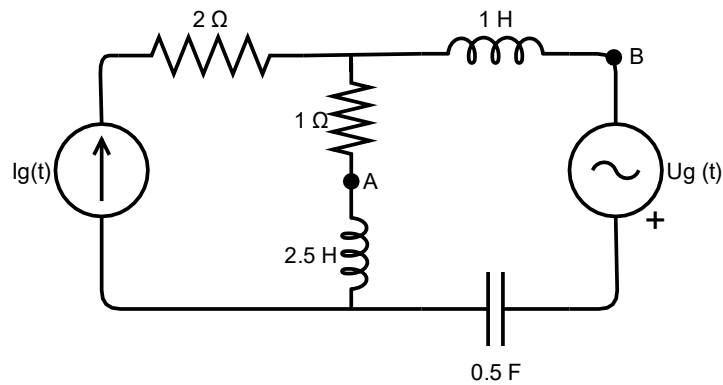


Figure 4. AC circuit 4

Solution: $U_{TH}(t) = 2\sqrt{2}\sin(2t + 180^\circ) \text{ V}$; $Z_{TH} = 16/37 + 52/37j \ \Omega$; $I_{SC}(t) = 1.36\sqrt{2}\sin(2t + 107^\circ) \text{ A}$;