

# Message Authentication Codes

## CRYPTOGRAPHY AND COMPUTER SECURITY

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# ÍNDICE

- 10. Message Authentication Codes (MAC)
  - Overview
  - Security requirements
  - MAC based on hash functions
  - MAC based on block ciphers
  - Authenticated encryption

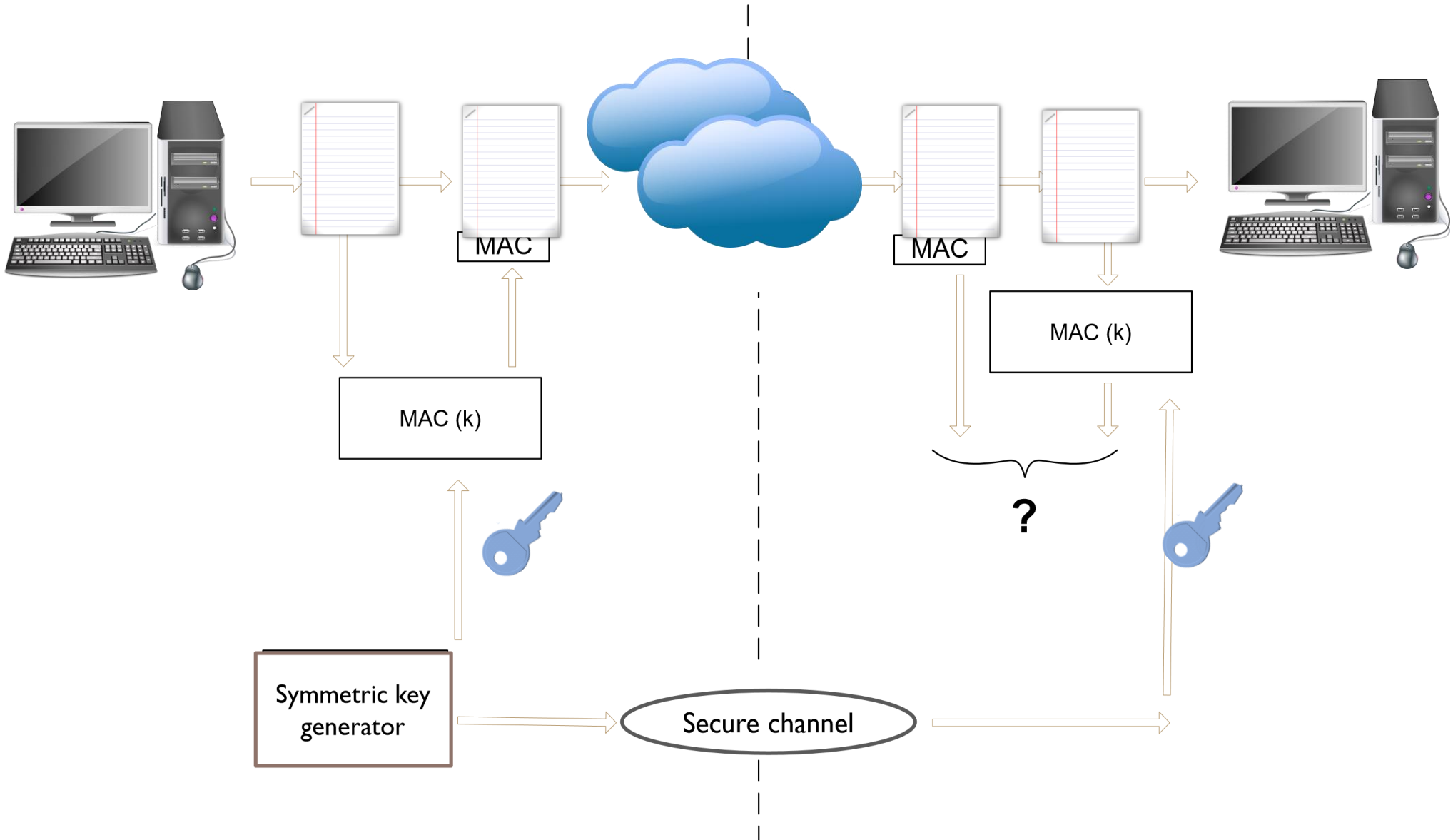
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# OVERVIEW

- A message Authentication Code (MAC) is a secret key algorithm that computes a fixed length value (authentication code) from a variable length message
- Any entity having the secret key is able to **verify the message integrity**
- A receiver sharing the secret key can **authenticate the message origin**
- Replay attacks can be avoided by including sequence numbers into the messages

# OVERVIEW



# OVERVIEW

- A MAC function needs not to be reversible
- Similarly as hash functions, collisions can be produced

$$|k| = 2^k$$

$$|MAC| = 2^n$$

$$|M| = \text{any}$$

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# SECURITY REQUIREMENTS

- Given  $M$  and its  $\text{MAC}(K, M)$  value, it is computationally unfeasible to find a message  $M'$  with the same MAC

$$\text{MAC}(K, M') = \text{MAC}(K, M)$$

- $\text{MAC}(K, M)$  must be uniformly distributed; thus the probability of finding 2 messages  $M$  and  $M'$  with the same MAC value is:
- Let  $M'$  be the output message of a transformation to  $M$  [ $M' = f(M)$ ]. In this case, it must be satisfied the following:

$$\Pr[\text{MAC}(K, M) = \text{MAC}(K, M')] = \frac{1}{2^n}$$



# SECURITY REQUIREMENTS

- MAC functions attacks

- Given a set  $M_i$ ,  $MAC(K, M_i)$ , the attacker wishes to generate  $M'$ ,  $MAC(K, M')$ , with  $M' \neq M_i \forall i=0 \dots n$

- Brute force

Key space attack  $(\frac{1}{2^k})$  versus MAC value attack  $(\frac{1}{2^n})$

Computational complexity is  $Min(\frac{1}{2^k}, \frac{1}{2^n})$

- Cryptanalysis

Requires the existence of vulnerabilities in the algorithm design or implementation (it will depend on internal structure)

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# MAC BASED ON HASH FUNCTIONS

- HMAC (Hash-MAC)
- Use known hash functions
- Hash function upon a message with some bits appended (obtained from the key)

$$\text{HMAC}(K, M) = H[(K' \oplus \text{opad}) || H[(K' \oplus \text{ipad}) || M]]$$

$K'$ :  $K$  padded with 0's on the left until reaching a length  $b$

$b$ : Processed block length in bits

ipad: 00110110 (0x36) repeated  $b/8$  times

opad: 01011100 (0x5C) repeated  $b/8$  times

$||$ : concatenation operator

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# MAC BASED ON BLOCK CIPHERS

- Symmetric block encryption of the message, using CBC mode
- The MAC value is the result of the last encrypted block
- The MAC value depends on every bit of the message

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# AUTHENTICATED ENCRYPTION

- Provide confidentiality, integrity and authenticity of communications
- In other words: privacy and authenticity is provided
- Symmetric encryption and MAC are used
  - MAC provides integrity and authentication
  - Encryption provides confidentiality

# AUTHENTICATED ENCRYPTION

- TYPES

- Encrypt-then-MAC
- Encrypt-and-MAC
- MAC-then-Encrypt

- For simplicity, in the following a single key is used from encryption and MAC but...

- The use of different keys (for encryption and MAC) is a solid way to construct an authenticated encryption scheme

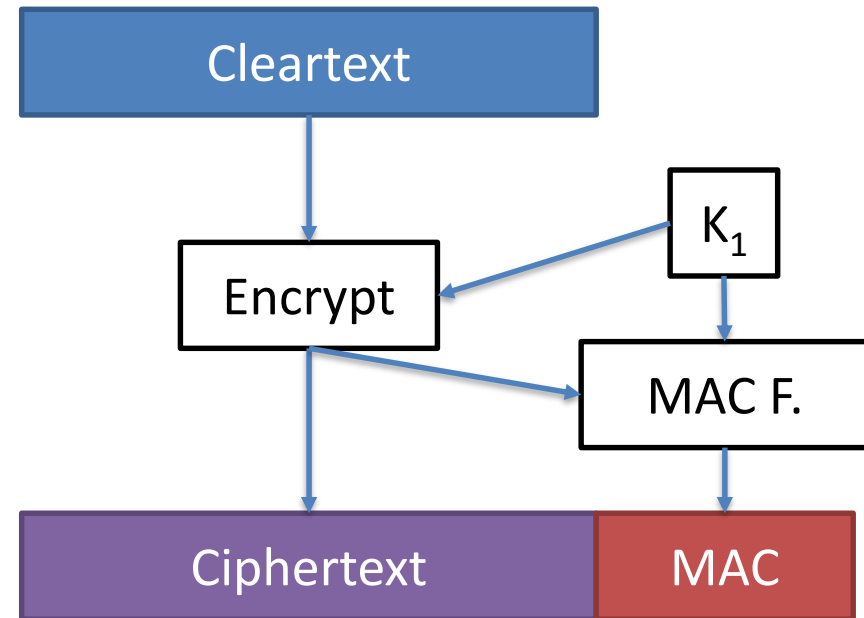


# AUTHENTICATED ENCRYPTION

- Types

- Encrypt-then-MAC

- High security when using an appropriate MAC function



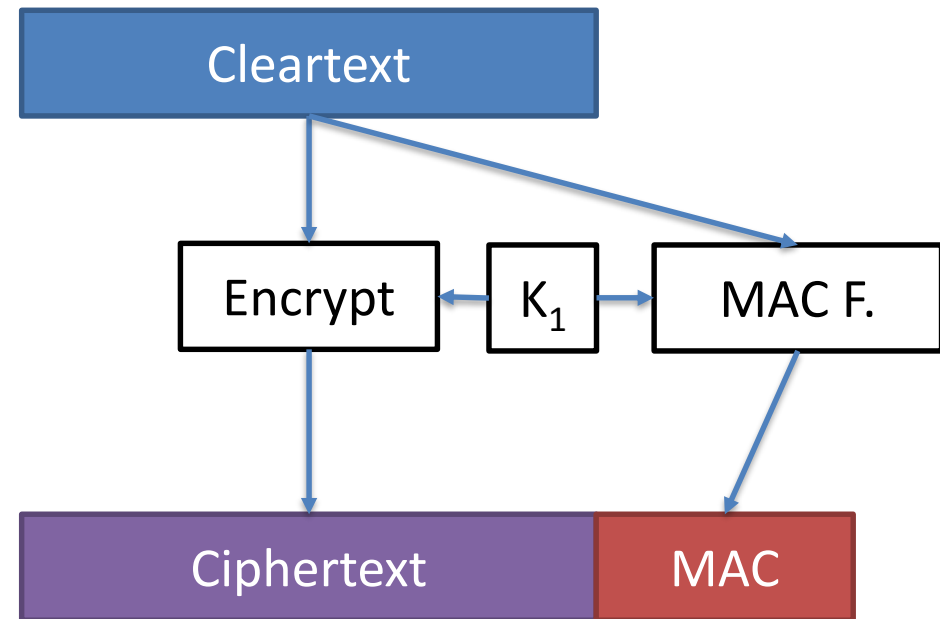
# AUTHENTICATED ENCRYPTION

- Types

- Encrypt-and-MAC

- Possible problem:

- The same text-> the same MAC

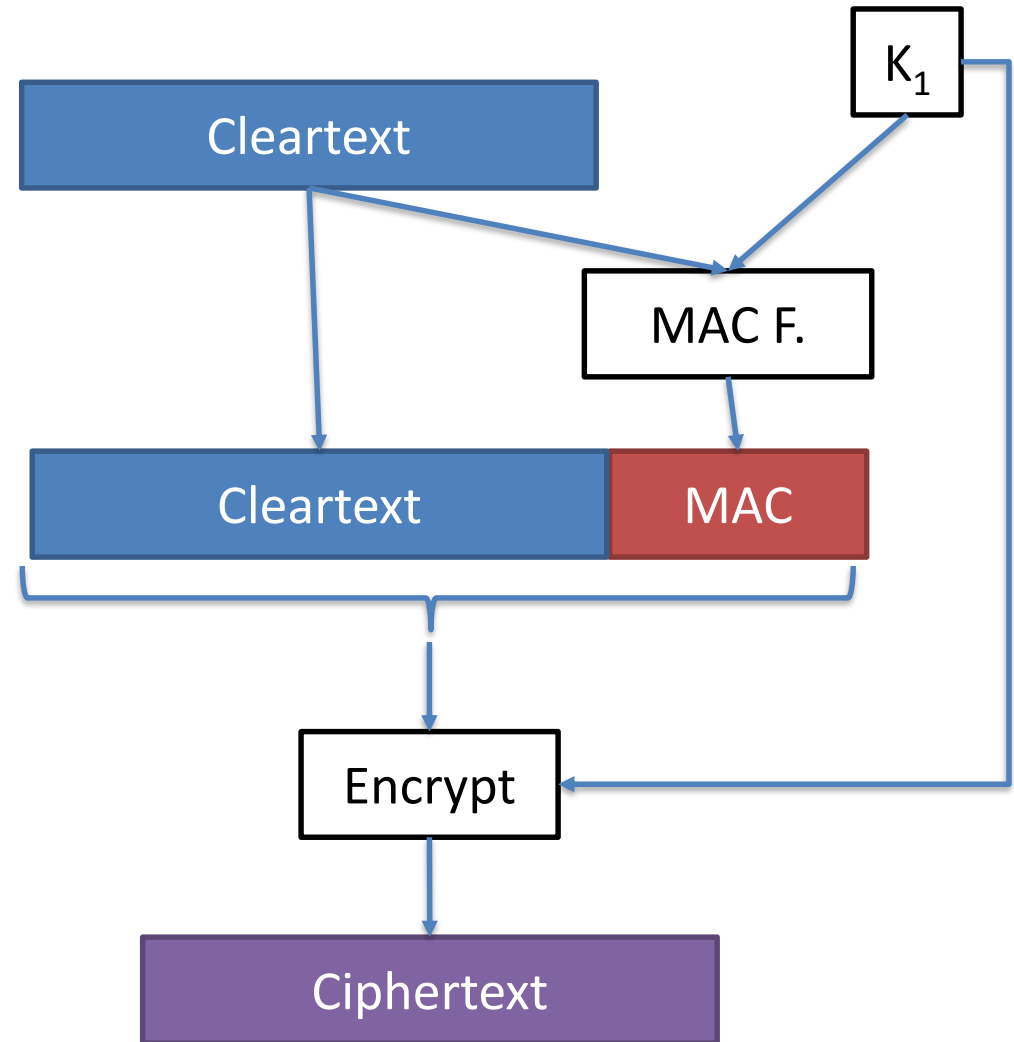


# AUTHENTICATED ENCRYPTION

- Types

- MAC-then-Encrypt

- Decryption should be carried out after verifying integrity and authenticity



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